

Catalyst testing & Kinetic studies

Information wanted

- ☞ Intrinsic reaction rate data
- ☞ Not obscured by parasitic phenomena
 - ↳ reactor characteristics
 - ↳ mass and heat transport phenomena
 - ↳ user manipulations
 - ↳ catalyst misbehaviour
 - ↳ deactivation/fouling

For

- Comparison activities and selectivities
- Kinetic modelling

Catalytic reactor design equation

plug-flow, steady state

$$\frac{dx_i}{d(W/F_i)} = -v_i \cdot \eta \cdot r \cdot \Phi$$

conversion i
‘space time’

stoichiometric coefficient i

catalyst effectiveness

deactivation function

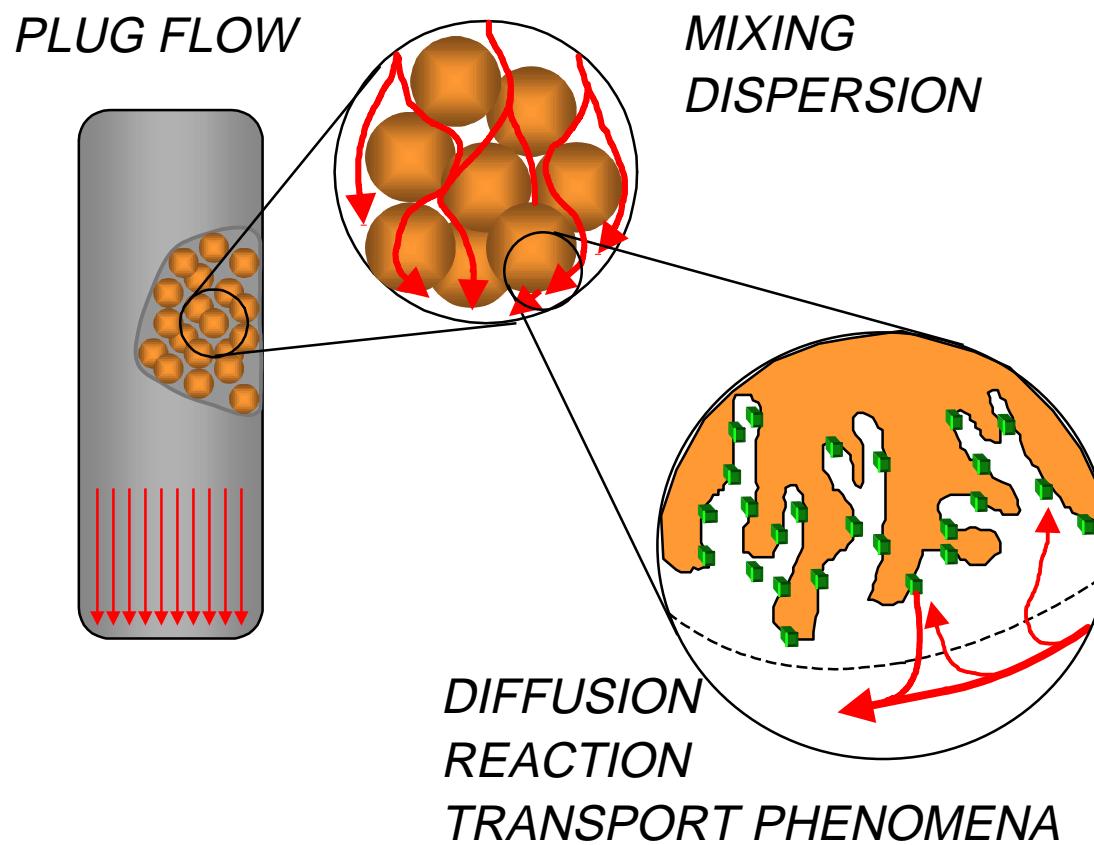
rate expression

The diagram illustrates the catalytic reactor design equation. It features a central equation $\frac{dx_i}{d(W/F_i)} = -v_i \cdot \eta \cdot r \cdot \Phi$. Above the equation, 'conversion i' is labeled with an arrow pointing to the term dx_i . Below the equation, '‘space time’' is labeled with an arrow pointing to the term $d(W/F_i)$. To the right of the equation, 'stoichiometric coefficient i' is labeled with an arrow pointing to the term v_i . Below the equation, 'catalyst effectiveness' is labeled with an arrow pointing to the term Φ . A green circle surrounds the terms $\eta \cdot r \cdot \Phi$, which are grouped together and labeled 'rate expression' in a box. An arrow points from the text 'deactivation function' to the term Φ .

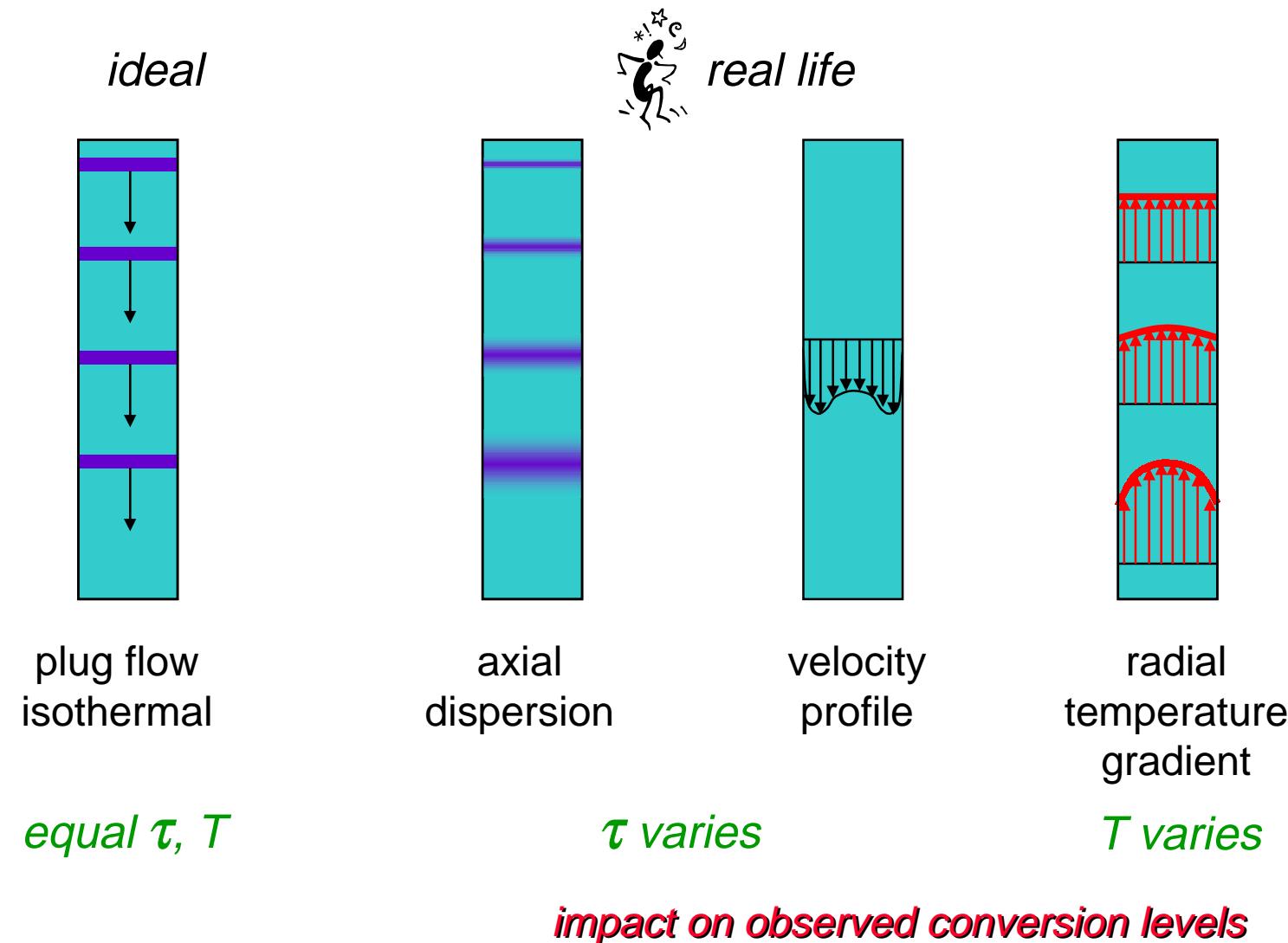
Eliminate deviations ideal reactor behaviour, low catalyst effectiveness and deactivation

Phenomena in catalytic reactor

(two-phase: fluid-solid)

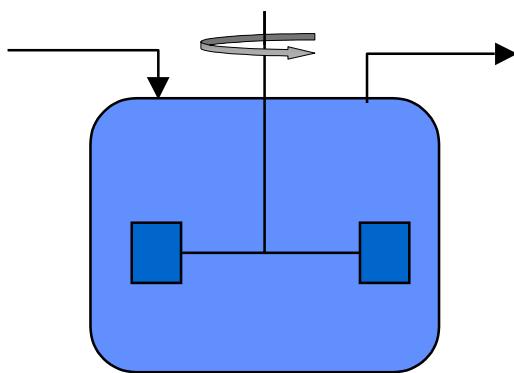


Packed bed reactor - assumptions



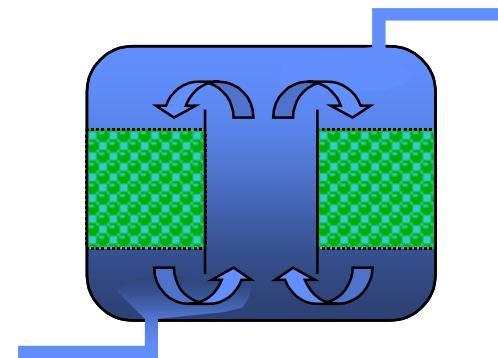
CSTR - assumptions

ideal



well mixed
isothermal

reality



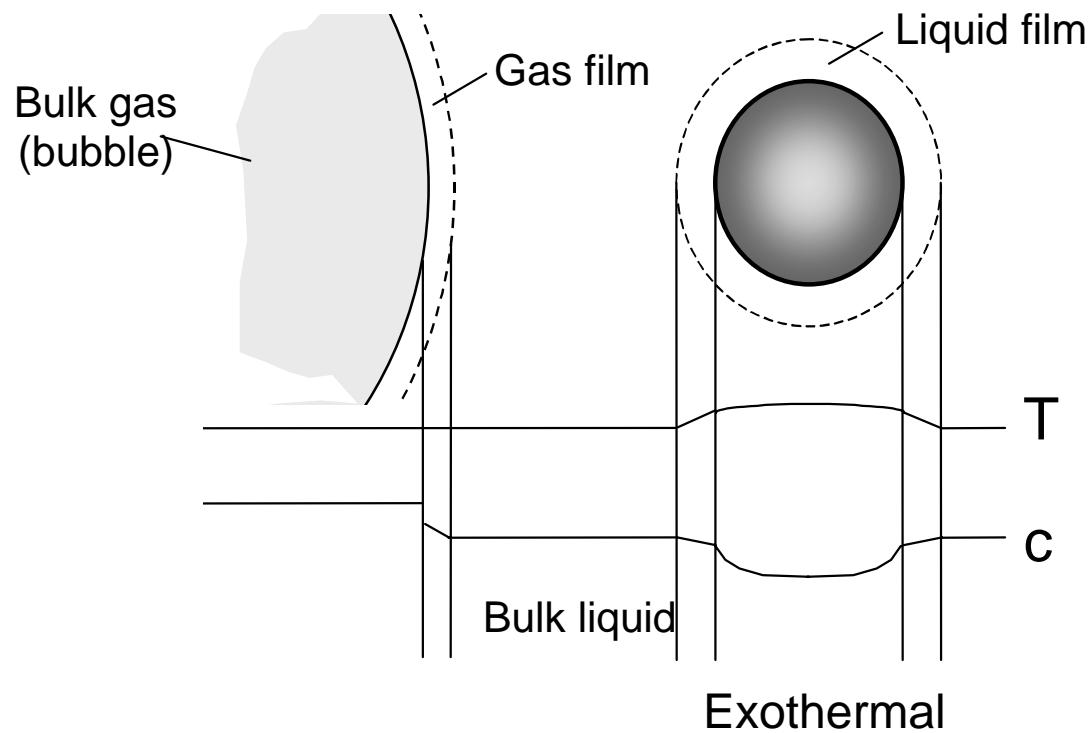
recirculation

- *instantaneous mixing*
- *equal conditions*

- *local concentration gradients*
- *conversion over bed*

Gradients at Particle Scale

Gas/liquid/solid Slurry Reactor

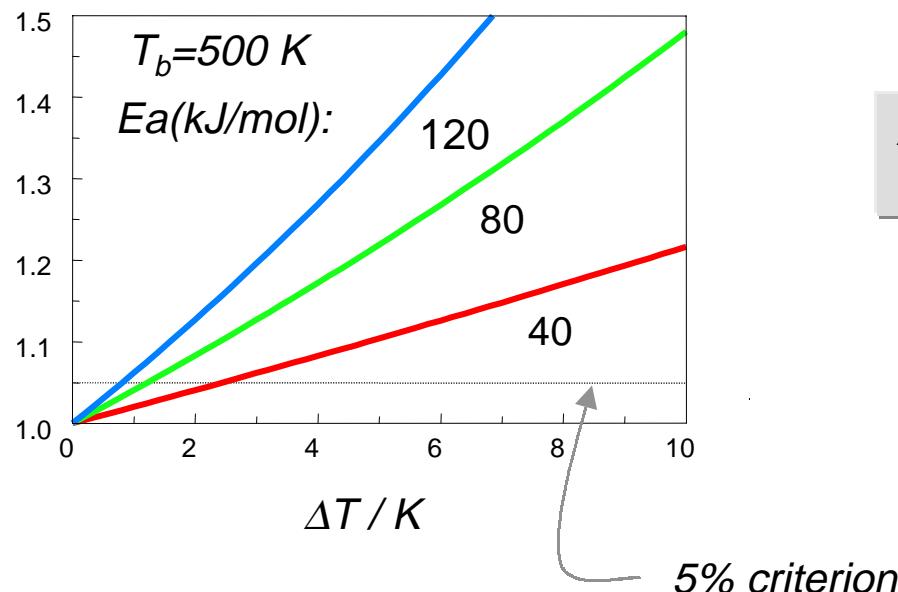


Effect temperature rise

How much increases rate constant ?

$$\frac{k(T_s)}{k(T_b)} = \exp\left\{-\frac{E_a}{RT} \cdot \left(\frac{T_b}{T_s} - 1\right)\right\} = \exp\left\{\gamma_b \left(\frac{\Delta T}{T_b + \Delta T}\right)\right\}$$

$k(T_s)/k(T_b)$



A few degrees
already critical !

Criteria - experimental verification

Criterion: $\frac{r_{v,obs}}{r_{v,chem}} = 1 \pm 0.05$

5% deviation

observed rate

External transfer: $Ca = \frac{r_{v,obs}}{a' k_f c_b} < \frac{0.05}{n}$

reaction order

$a' = \frac{S_p}{V_p}$

mass transfer coefficient

particle properties

When mass transport limitations?

5%Criterion

Internal transfer: $\Phi = \eta\phi^2\left(\frac{n+1}{2}\right) < 0.15$

$$\eta_i\phi_G^2 = \frac{r_{v,obs}}{a'^2 \cdot D_{eff} \cdot c_b}$$

External transfer: $Ca < \frac{0.05}{n}$

$$Ca = \frac{r_{v,obs}}{a' k_f c_b}$$

Also:

$$\Phi = \frac{Bi_m}{s} \cdot Ca$$



while $Bi_m > \sim 10$
 $s=1,2,3$ (geometry)

Weisz-Prater more severe than
Carberry criterion

When temperature effects?

5%Criterion

Prater numbers

External transfer:

$$|\beta_e| \gamma_b Ca < 0.05$$

$$\beta_e = \frac{(-\Delta H) k_f c_b}{h T_b}$$

Internal transfer:

$$\frac{|\beta_i| \gamma_s (\eta_i \phi^2)}{2} < 0.05$$

$$\frac{\beta_e}{\beta_i} \begin{array}{ll} 10-10^4 & \text{gas-solid} \\ 10^{-4}-0.1 & \text{liquid-solid} \end{array}$$

$$\gamma_b = \frac{E_a}{R T_b}$$

10-20

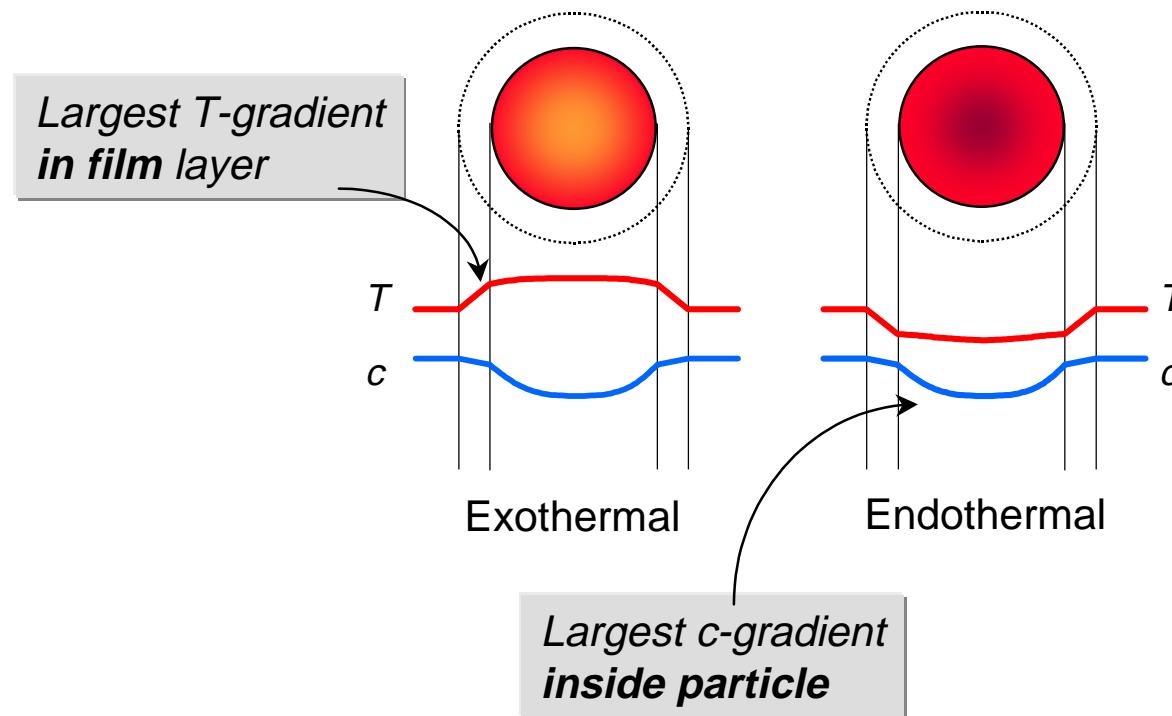
$$\beta_i = \frac{D_e (-\Delta H) c_s}{\lambda_e T_s}$$

0-0.3 (exothermal)



External gradient criterion more severe than internal criterion

Temperature and concentration profiles



Temperature gradient in catalyst bed

$$\frac{E_a}{R T_w} \left| \frac{(-\Delta H_r) r_{v,obs}}{\lambda_{eff,b} T_w} \right| \left(1 - \varepsilon_b \right) \left(1 - b \right) \left(\frac{1}{8} + \frac{1}{Bi_w} \frac{d_p}{d_t} \right) < 0.05$$

$$\frac{\text{criterion bed T - gradient}}{\text{criterion film T - gradient particle}} \approx \left(\frac{r_t}{r_p} \right)^2 \cdot \left(\frac{\lambda_{p,eff}}{\lambda_{b,eff}} \right) \cdot \left(\frac{s^2(1 - \varepsilon_b)}{8} \right) \gg 1$$



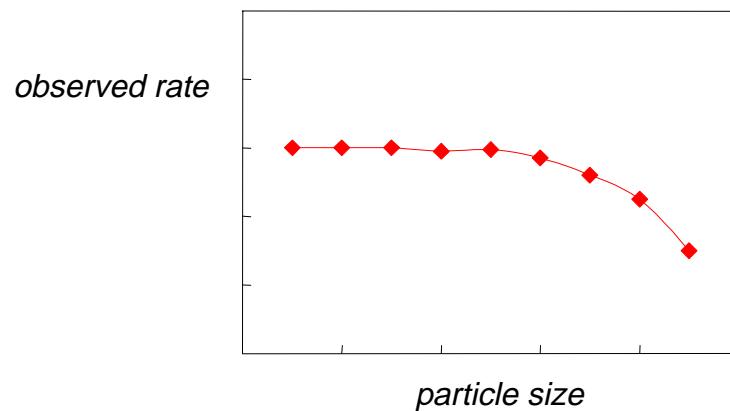
temperature gradient in bed always develops first !

Summary:

$$(T - grad)_{bed} > (T - grad)_{ext} > (c - grad)_{int}, (T - grad)_{int} > (c - grad)_{ext}$$

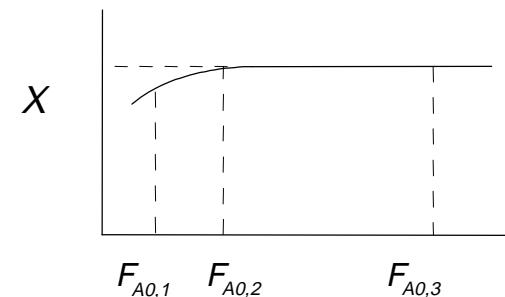
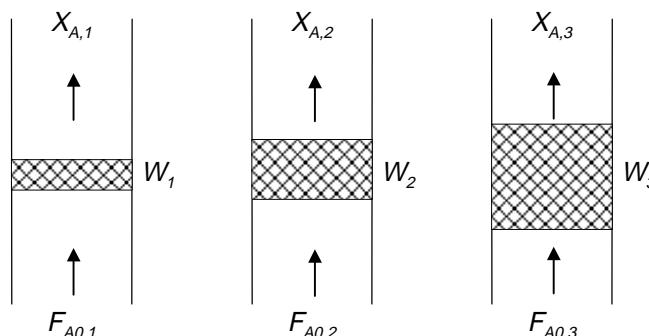
Diagnostic tests mass transport limitations

1. Particle size variation



egg-shell catalysts?

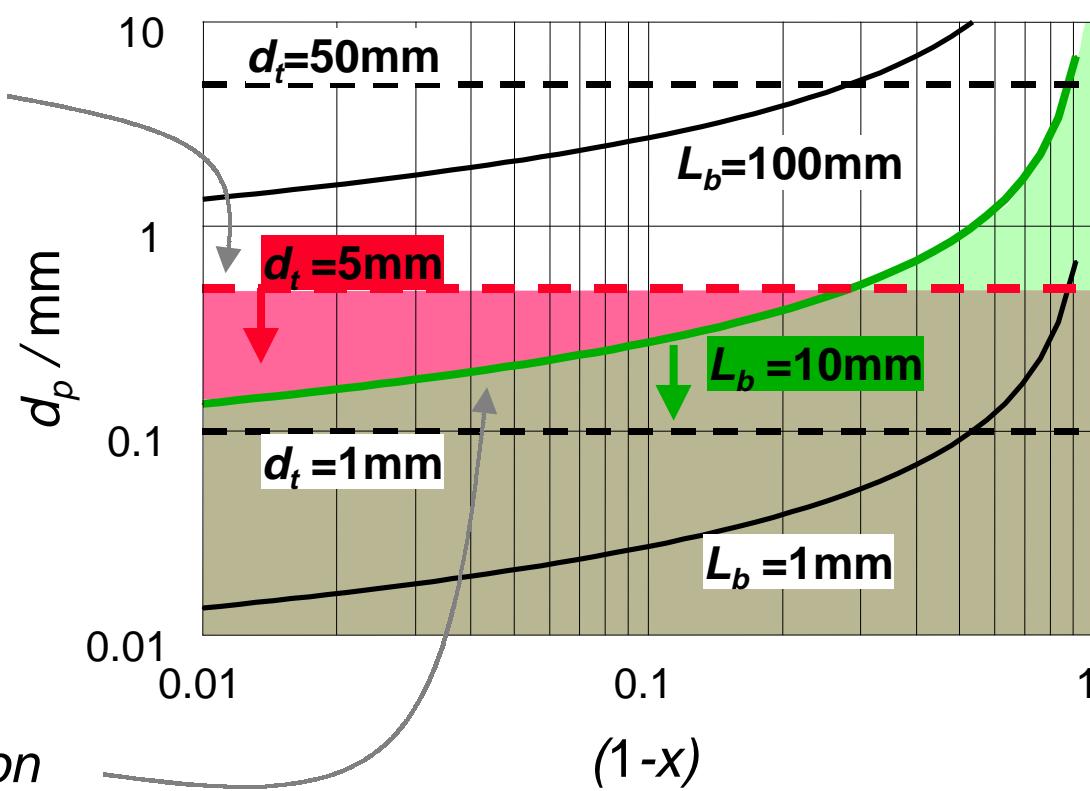
2. Flow rate variation at constant space time!



Nonideal reactor behaviour

$$\frac{d_t}{d_p} > 10$$

velocity profile



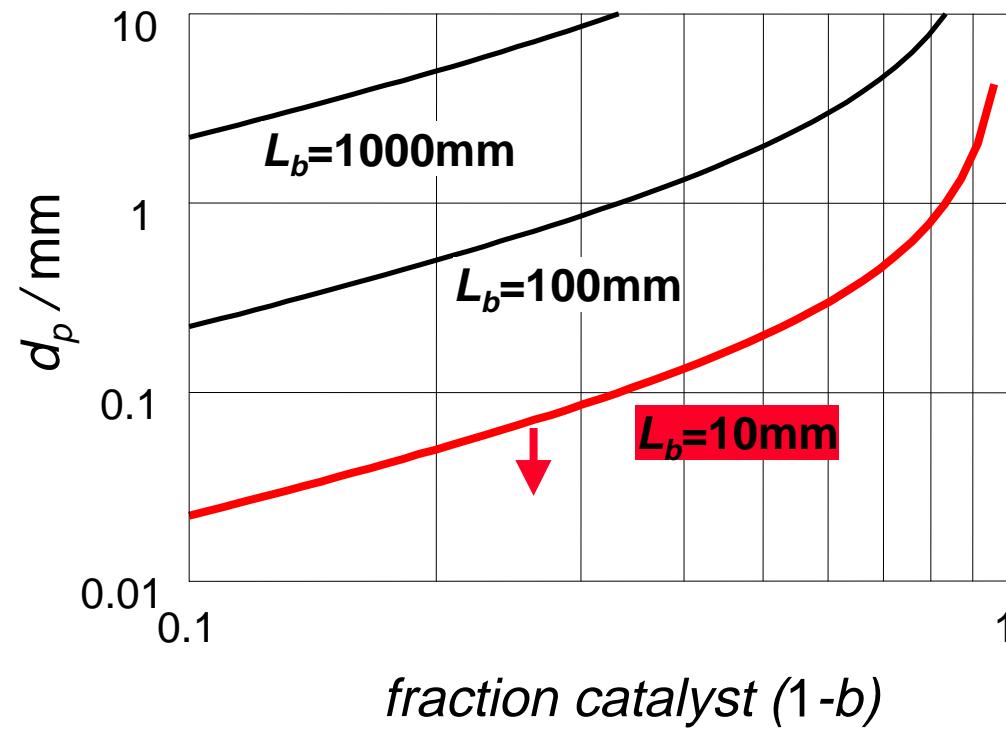
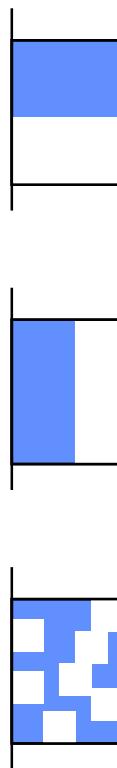
axial dispersion

$$\frac{L_b}{d_p} > \frac{20 n}{Bo} \ln\left(\frac{1}{1-x}\right)$$

Bed dilution

*inhomogeneous distribution
catalyst by-passing*

$$\frac{2.5 b d_p}{(1-b) L_b} < 0.05$$



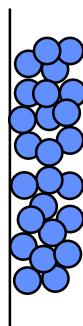
Small tube diameters

Sie 1996

$$\frac{L_b \cdot D_{rad}}{r_t^2 \cdot u} > 8 \cdot (\kappa/\varepsilon) \cdot n \cdot \ln\left(\frac{1}{1-x}\right)$$

$$SV(gas) = 10000 \text{ h}^{-1}$$

$$SV(liquid) = 1 \text{ h}^{-1}$$

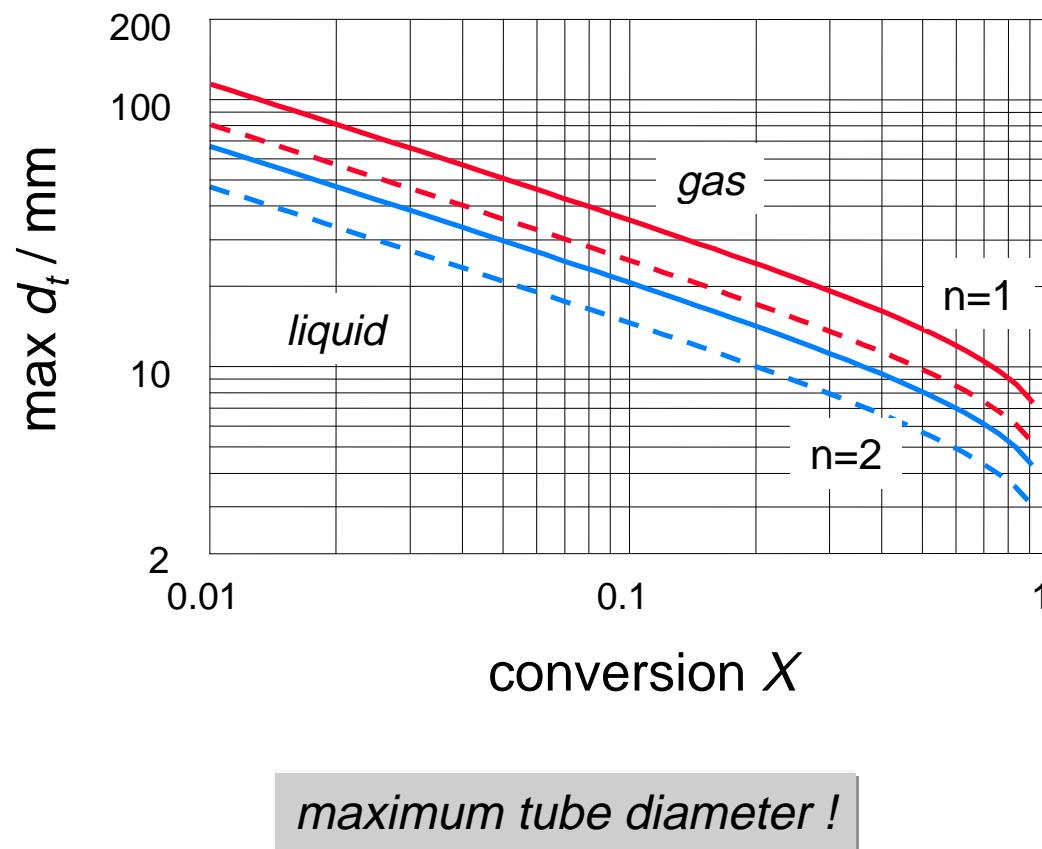


$$d_t/d_p < 5:$$

$$\kappa = 0.04$$

$$\varepsilon_b = 0.4$$

$$d_t^2 < \frac{5D_{rad}}{SV \cdot n \cdot \ln\left(\frac{1}{1-x}\right)}$$



maximum tube diameter !

Criteria recirculation reactors

rate over bed changes less than 5%

- Concentration effects

$$\frac{x}{(1-x)(1+R_c)} < \frac{0.05}{n}$$

- Temperature effects

$$\frac{E_a}{RT_b} \cdot \left| \frac{r_{obs} \cdot (-\Delta H_r)}{\tilde{C}_{pf} T_b} \right| \cdot \frac{W}{F_{tot}} = \gamma_b \cdot \left| \frac{(-\Delta H_r)}{\tilde{C}_{pf} T_b} \right| \cdot \frac{y_0 \cdot x}{(R_c + 1)} < 0.05$$

Reaction order - Activation energy

rate expression $r = \frac{k_2 N_T K_A p_A}{(1 + K_A p_A + K_B p_B)}$

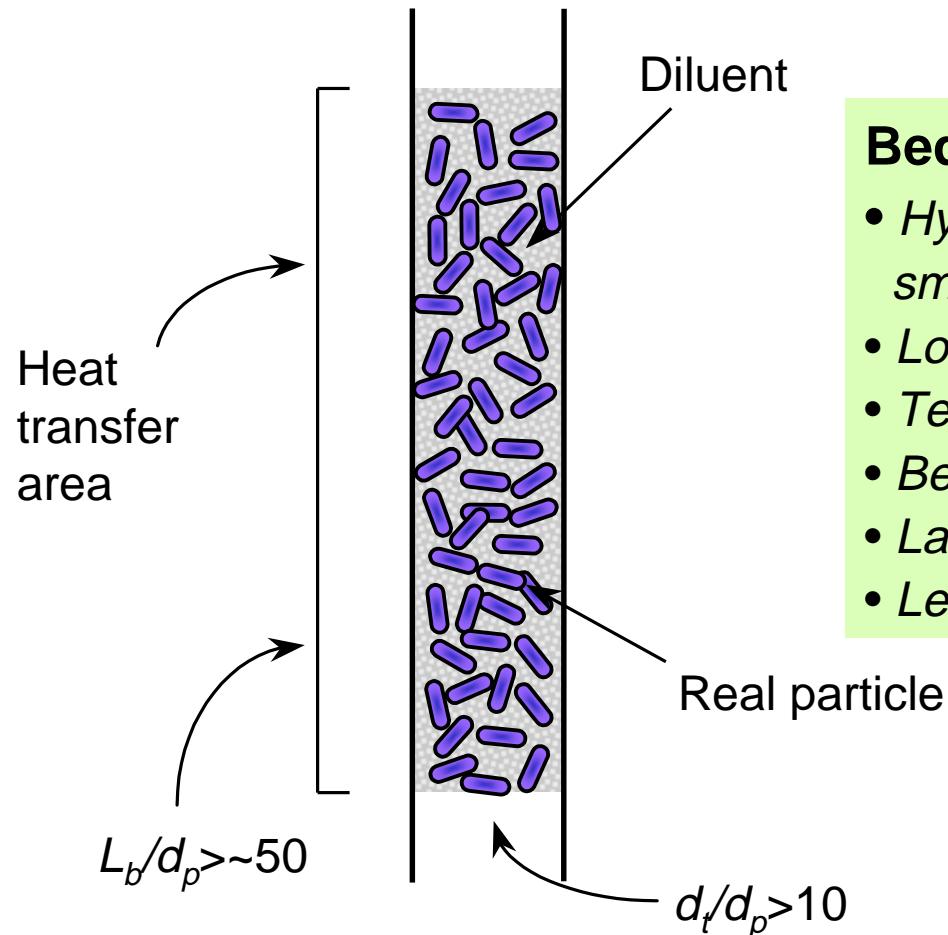
Reaction order	$n_A = 1 - \theta_A$	0 - 1
	$n_B = -\theta_B$	(-1) - 0

Activation energy $E_a^{obs} = E_{a2} + (1 - \theta_A) \Delta H_A - \theta_B \Delta H_B$

*depend strongly on occupancy!
vary during reaction*

Catalyst testing - Bed dilution

decoupling hydrodynamics and kinetics

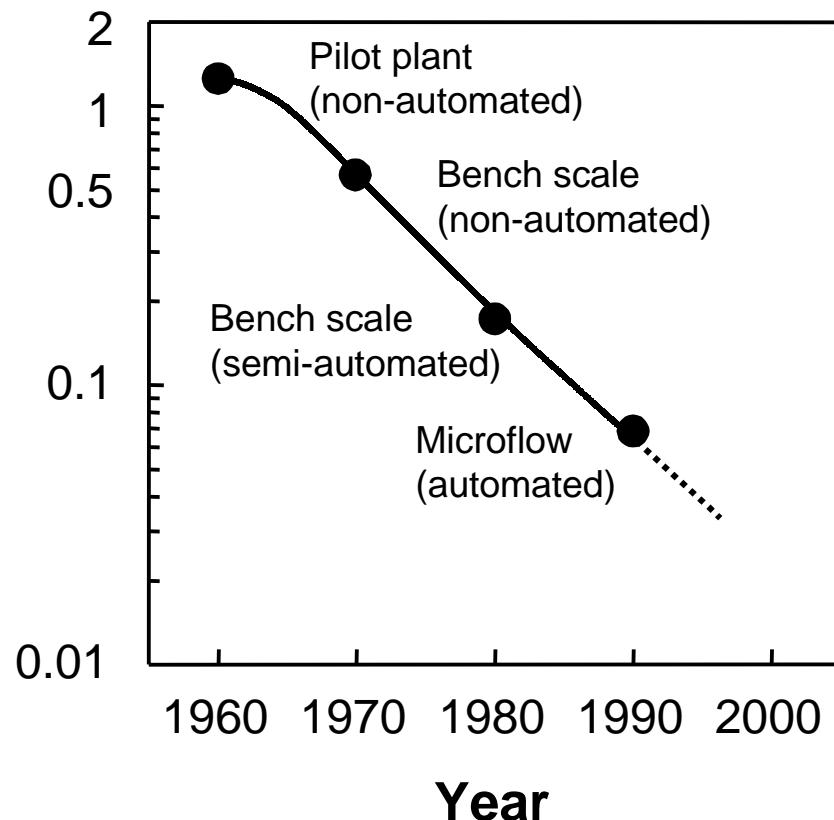


Bed dilution (e.g. SiC)

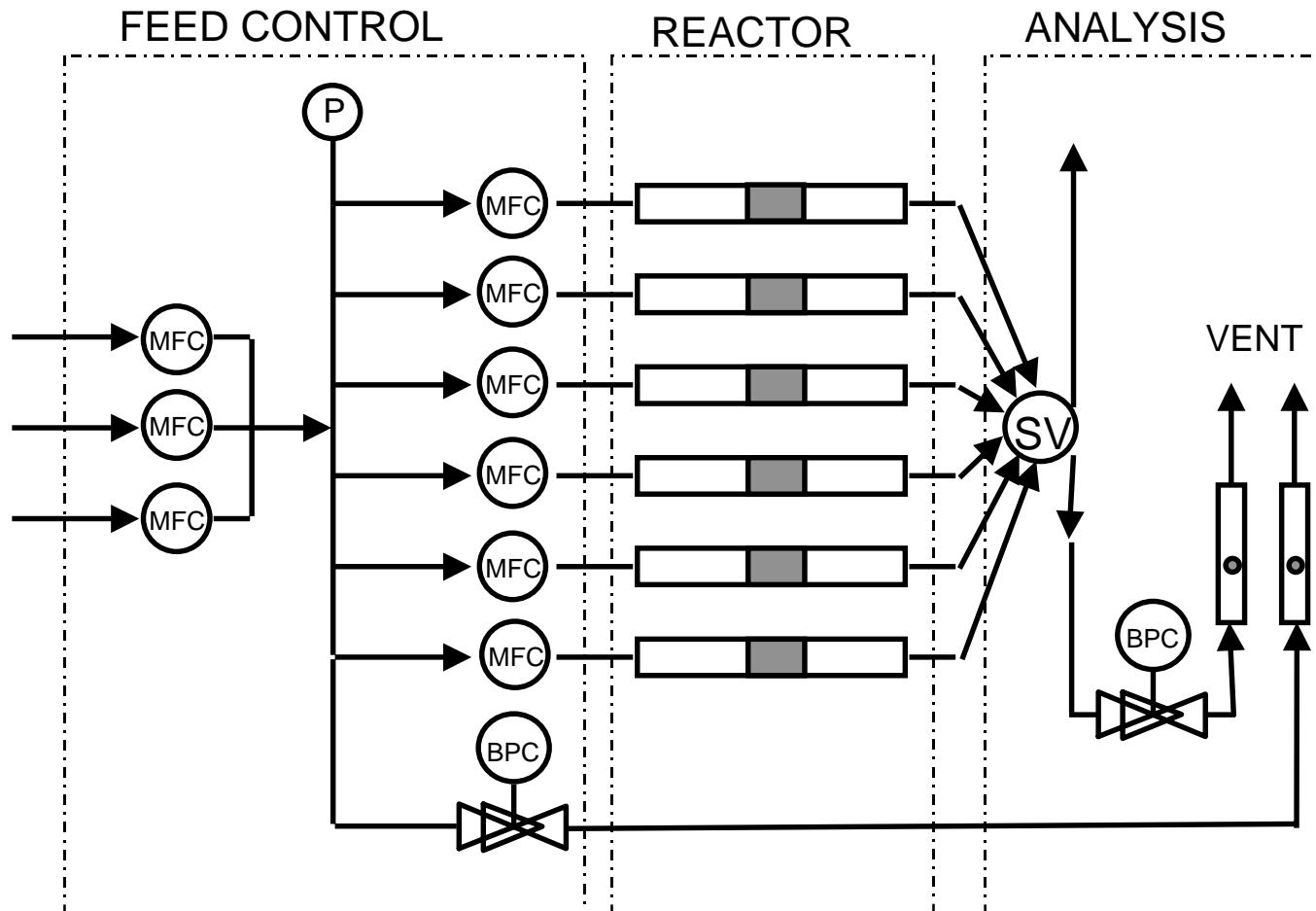
- *Hydrodynamics determined by small particles (wetting, velocity)*
- *Longer bed, larger L/d_p*
- *Testing of real catalyst particles*
- *Better heat conduction*
- *Larger heat transfer area*
- *Less heat produced per volume*

Sie, AIChE-J. 1996

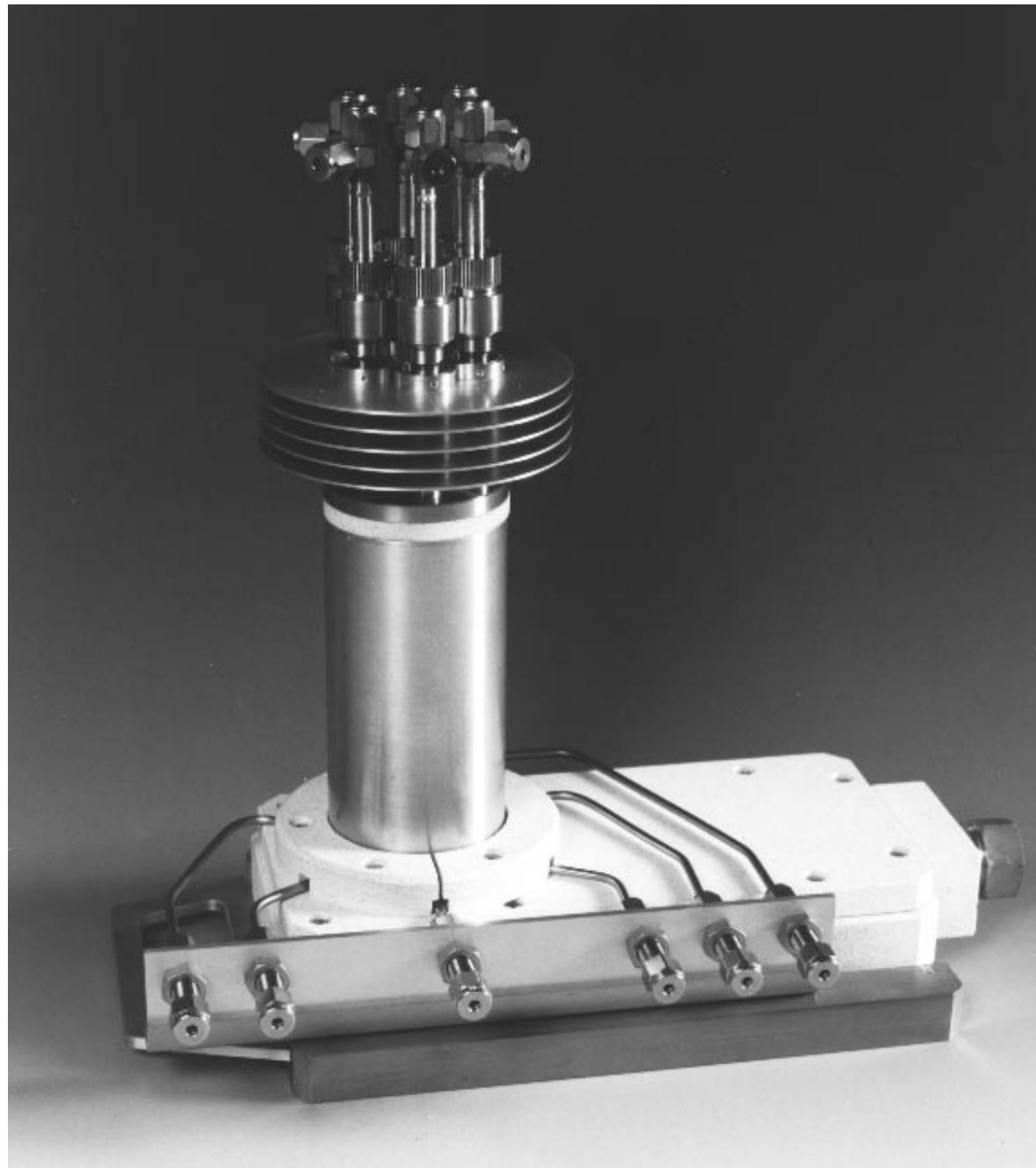
Manhour per reactor hour

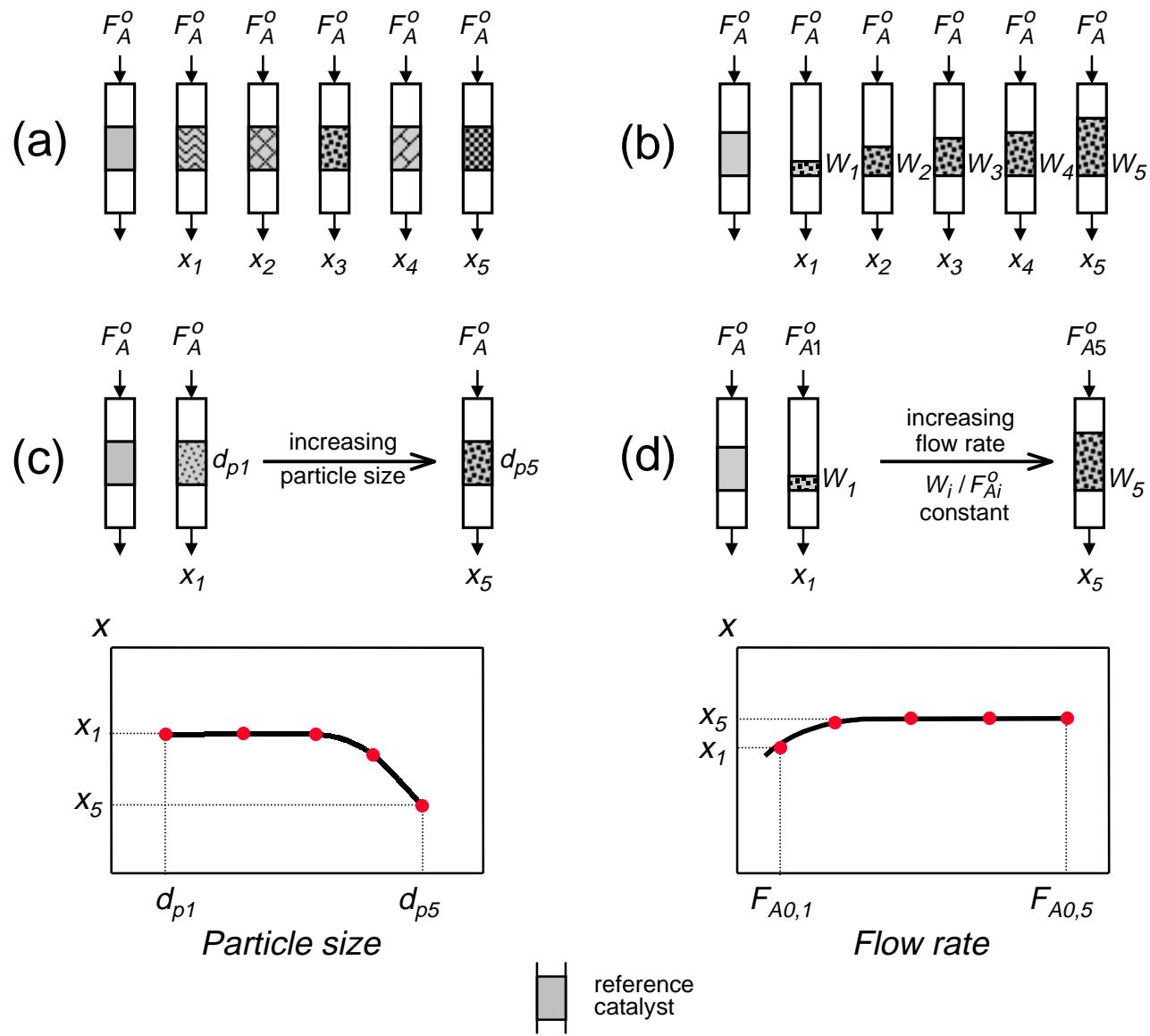


Parallelization catalyst testing



Six-flow reactor





Kinetics

Procuring rate data laborious task

*conversion vs. space time W/F
temperature
partial pressures / concentrations*

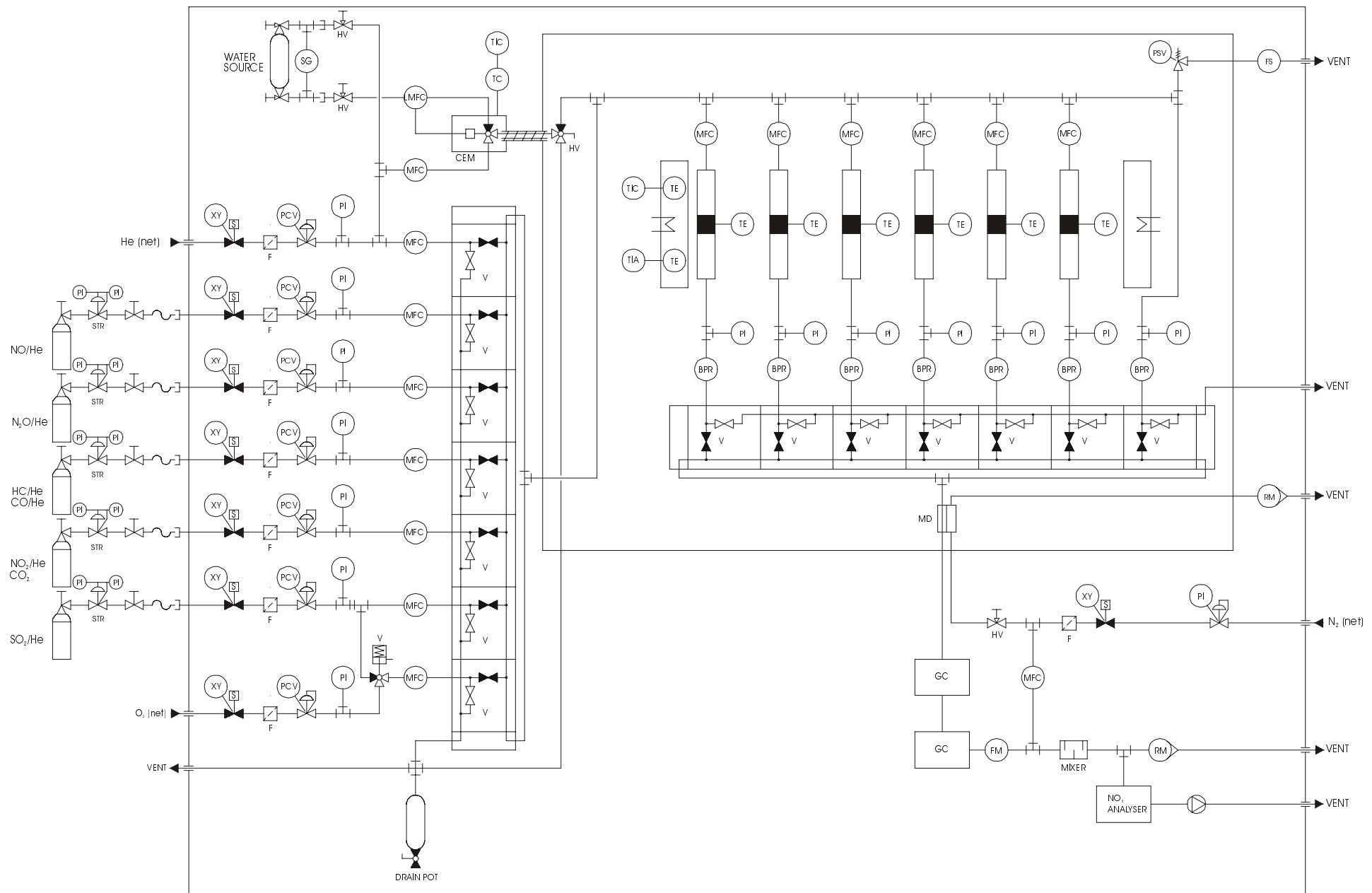
Improve speed:

- *PC controlled equipment*
- *Six-flow set-up (parallel reactors)*
- *Temperature scanning*
- *Sequential experimental design*



*Don't forget: stable catalyst, blank runs, duplicates
check criteria*

Set-up Six-flow reactor



Useful references

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