

Introduction to biokinetics

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Delft
University of
Technology

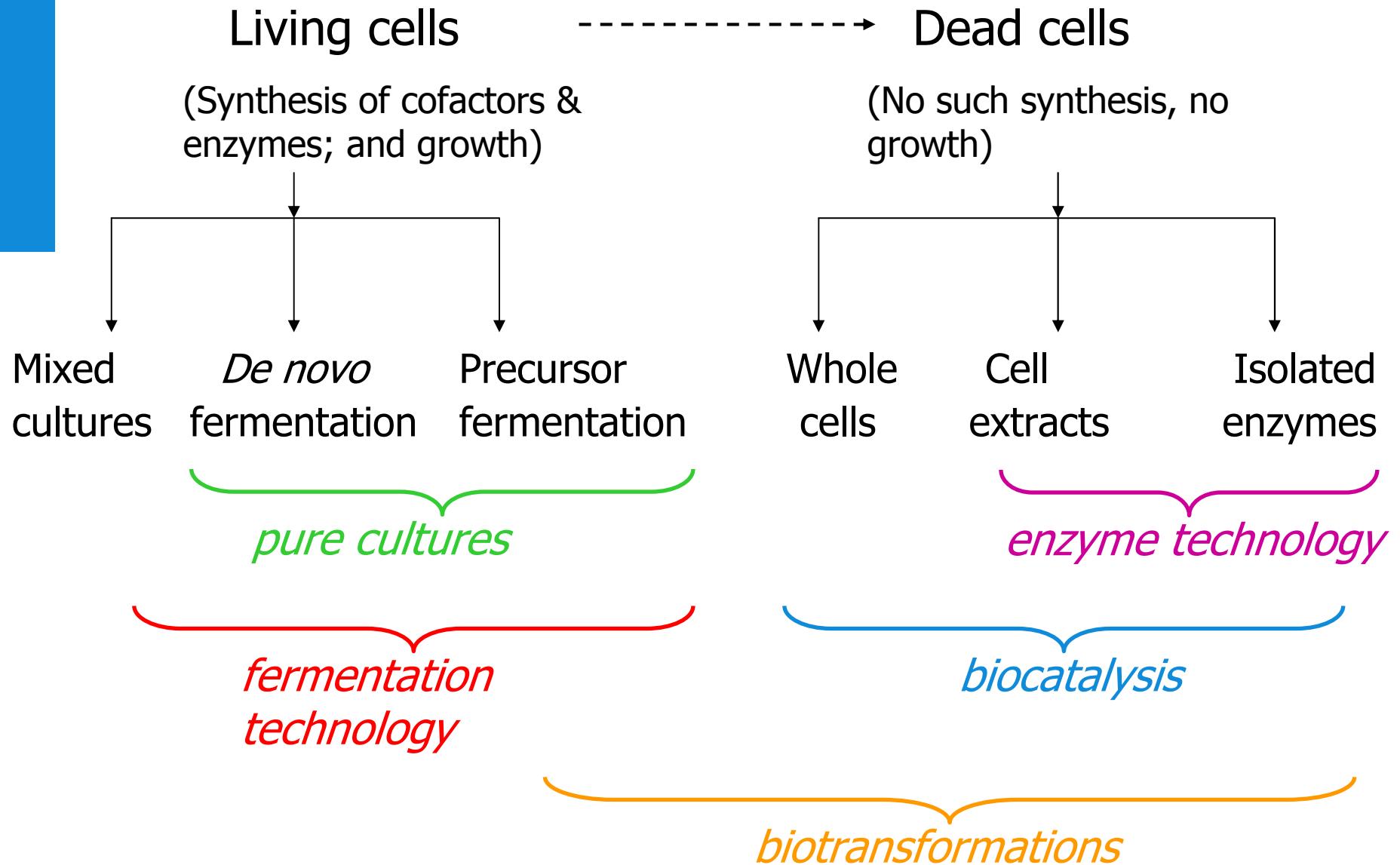
Challenge the future

Research groups at Department of Biotechnology TU Delft

- Analytical Biotechnology
- Biocatalysis and Organic Chemistry
- Bioprocess Technology
- Bioseparation Technology
- Environmental Biotechnology
- Enzymology
- Industrial Microbiology
- Complex Fluids Theory
- Biotechnology and Society



biokinetics is
key expertise

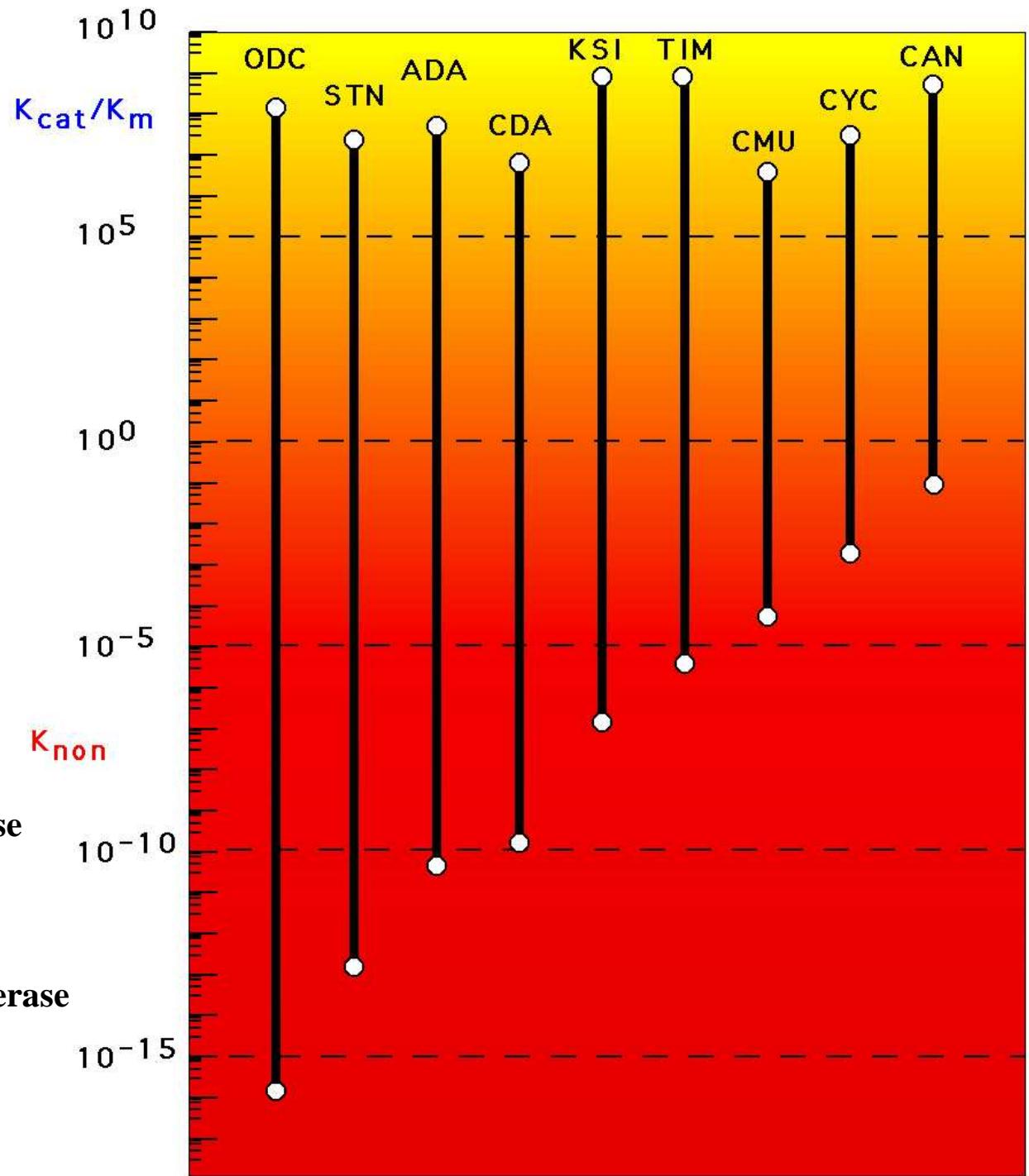


Principles governing kinetics

- Enzymes: catalysis+transport
- Pure microbial cultures: also growth+regulation+evolution
- Mixed cultures: also growth+regulation+evolution
+ecology

Rate enhancement by enzyme catalysis

ODC	OMP decarboxylase
STN	Staphylococcal nuclease
ADA	Adenosine deaminase
CDA	Cytidine deaminase
KSI	Ketosteroid isomerase
TIM	Triosephosphate isomerase
CMU	Chorismate mutase
CYC	Cyclophilin
CAN	Carbonic anhydrase

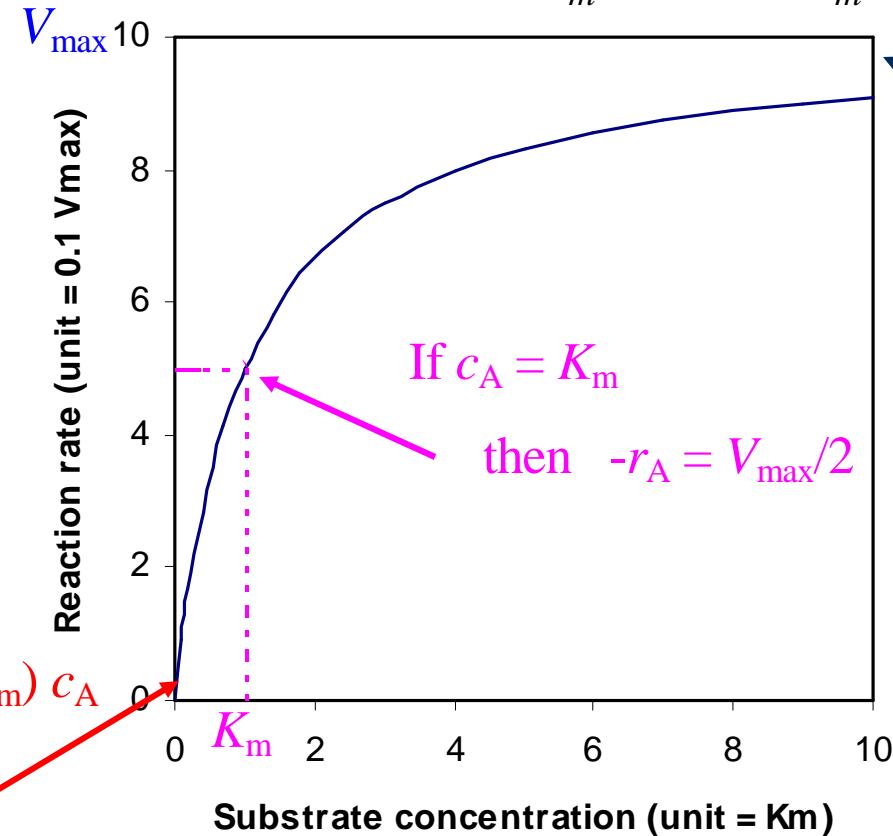


Rate equations

- $-r_A = f(p, T, c_A, c_B, c_P, c_{\text{Enzyme}}, c_{\text{H}^+}, c_{\text{solvent}}, \dots)$
- $-r_{\text{Enzyme}} = f(p, T, c_A, c_B, c_P, c_{\text{Enzyme}}, c_{\text{H}^+}, c_{\text{solvent}}, \dots)$
- Stoichiometry: $-r_A = -r_B = r_P$
- Rates are often studied at fixed p , T , pH; in water.

Michaelis-Menten equation

$$-r_A = \frac{V_{\max} c_A}{K_m + c_A} = \frac{V_{\max} \frac{c_A}{K_m}}{1 + \frac{c_A}{K_m}} = \frac{k_{cat} \frac{c_A}{K_m}}{1 + \frac{c_A}{K_m}} c_{Etot}$$



If $c_A \rightarrow 0$

then $-r_A \rightarrow (V_{\max}/K_m) c_A$
(1st order range)

If $c_A \rightarrow \infty$
then $-r_A \rightarrow V_{\max}$
(0th order range)

Stoichiometry

most enzymatic reactions include up to 2 substrates and 2 products

- | | |
|--------------------|--------------------------|
| 1. Oxidoreductases | bi-bi, ter-bi (or other) |
| 2. Transferases | bi-bi |
| 3. Hydrolases | bi-bi |
| 4. Lyases | uni-bi (usually) |
| 5. Isomerases | uni-uni |
| 6. Ligases | ter-ter (or more) |

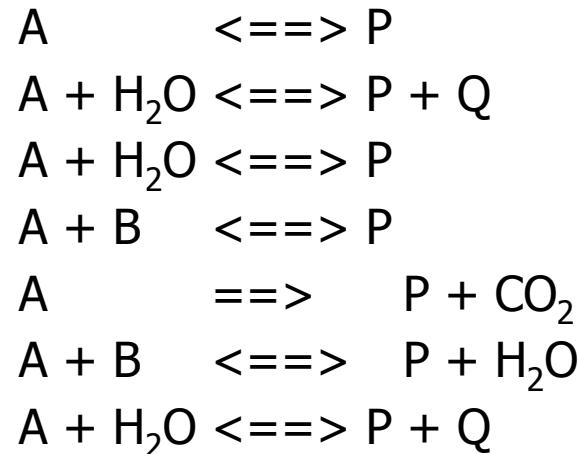
Difficult example (E.C. 6.3.1.14):



<http://www.expasy.org/enzyme/>

Michaelis-Menten: $A \rightleftharpoons P$

- Glucose isomerase
- glucoamylase
- fumarase
- aspartase
- aspartate decarboxylase
- thermolysin
- penicillin acylase



B, P and Q will influence the rate

Laboratory conditions

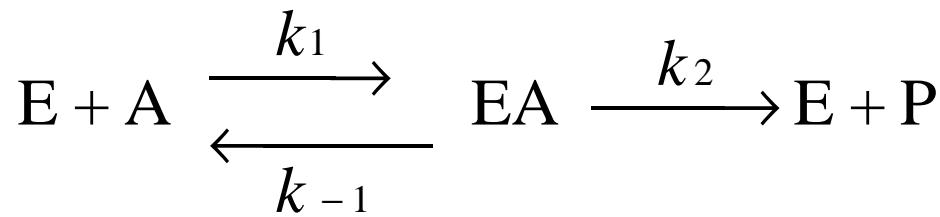
- $c_A \ll c_{\text{water}}$
- $c_A \gg c_P, c_Q$

\Rightarrow (pseudo) Michaelis-Menten suited

Industrial conditions

- c_A = initially as high as possible
 - $c_A \ll c_P, c_Q$ at the end of the reaction
- \Rightarrow Michaelis-Menten equation unsuited

Simplest reaction scheme:



- 4 species involved: E, A, EA and P
- 2 conservation equations; in batch with constant volume:

$$C_{\text{Etot}} = C_E + C_{\text{EA}}$$
$$C_{\text{A0}} = C_A + C_P + C_{\text{EA}}$$

- $4 - 2 = 2$ macroscopic balances needed; in batch with constant volume:

$$-\frac{dc_A}{dt} = k_1 c_E c_A - k_{-1} c_{\text{EA}}$$
$$-\frac{dc_E}{dt} = k_1 c_E c_A - k_{-1} c_{\text{EA}} + k_2 c_{\text{EA}}$$

- Can hardly be solved analytically without any assumption

Simplifying assumptions

1. $c_A \gg c_{E\text{tot}}$

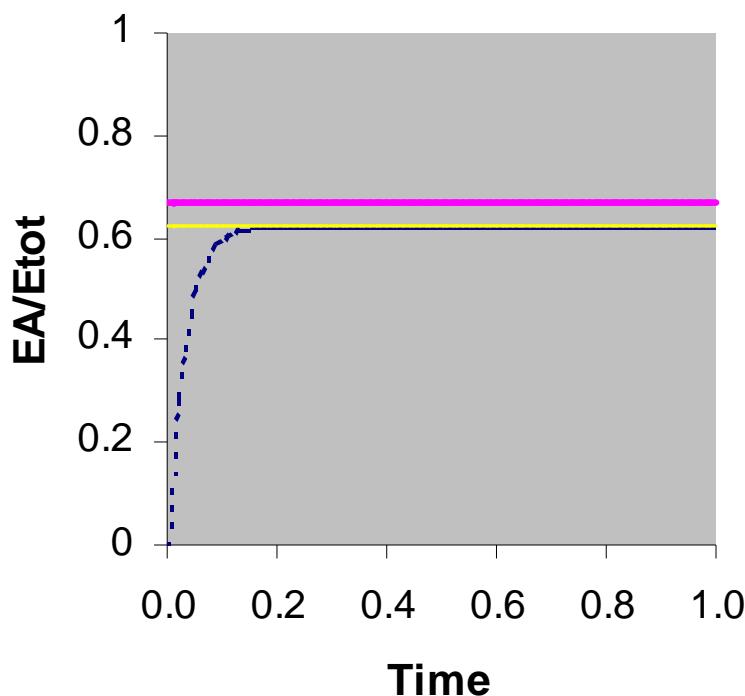
2a. $k_1 \gg k_2$ pseudo-equilibrium assumption
(EA is almost at equilibrium with E and A)

2b. $dc_E/dt = 0$ pseudo-steady state assumption
(the change in concentration of E is much smaller than the change in concentration of A)

Result for 2a and also for 2b: Michaelis-Menten type of equation

Comparison of approaches 1

(pre-steady state situation; no product formation yet)



exact solution
pseudo-equilibrium
pseudo-steady state

$$c_{A0} = 1$$
$$c_{E\text{tot}} = 0.001$$

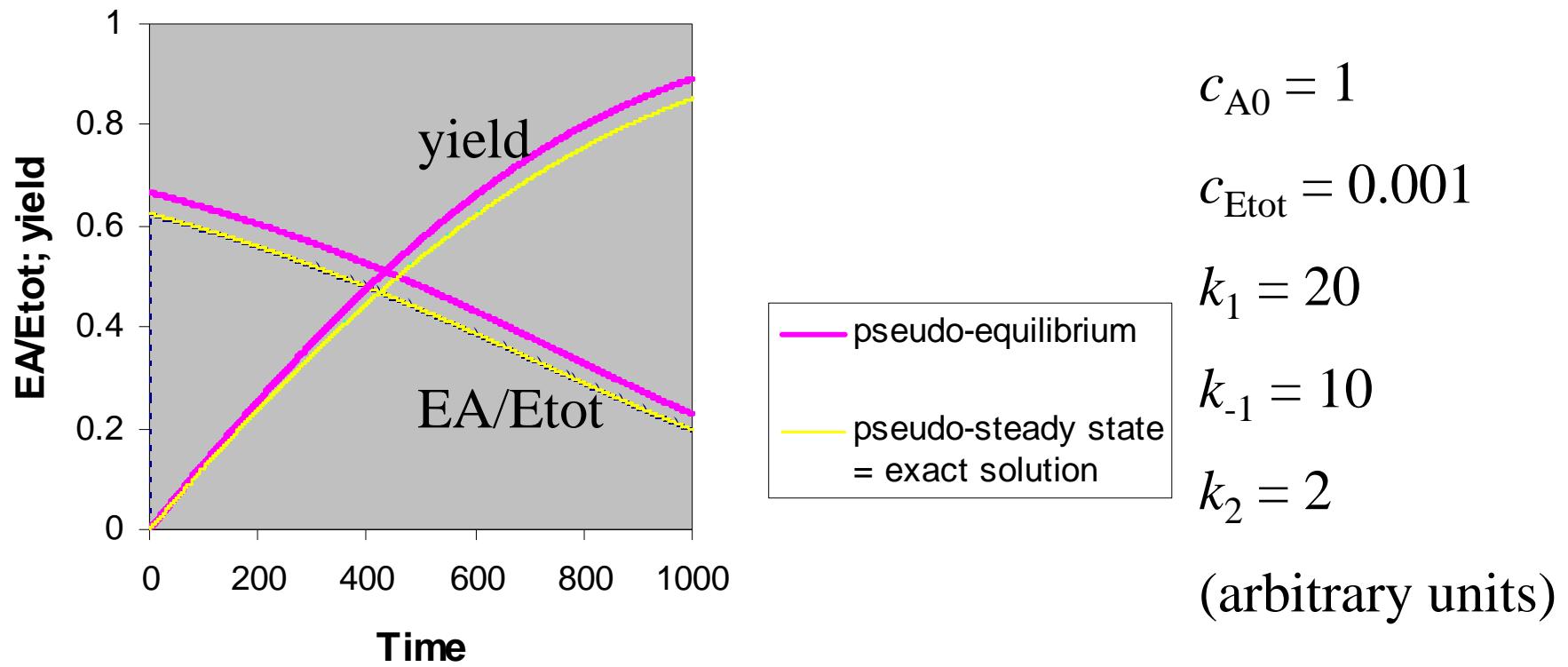
$$k_1 = 20$$
$$k_{-1} = 10$$

$$k_2 = 2$$

(arbitrary units)

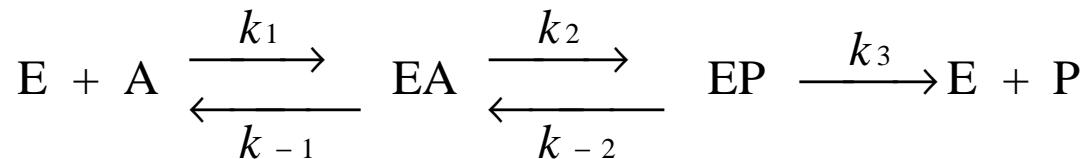
Comparison of approaches 2

(steady-state situation; product formation)



PROCEDURES FOR DERIVATION OF RATE EQUATIONS

What is the rate equation for the following mechanism?



1. Write down the conservation balance for the n enzyme species involved (1 balance equation).

$$c_{E\text{tot}} = c_E + c_{EA} + c_{EP}$$

2. Use the pseudo-steady state approach for each but one of the enzyme species

$$\frac{dc_{EA}}{dt} = k_1 c_E c_A + k_{-2} c_{EP} - (k_{-1} + k_2) c_{EA} = 0$$

$$\frac{dc_{EP}}{dt} = k_2 c_{EA} - (k_{-2} + k_3) c_{EP} = 0$$

3. Sum the rates of substrate formation and conversion

$$-r_A = k_3 c_{EP}$$

4. Solve the set of $n + 1$ equations

Symbolic solution with Mathcad

Given

$$c_{Etot} = c_E + c_{EA} + c_{EP}$$

$$k_1 \cdot c_E \cdot c_A + k_2 \cdot c_{EP} - (k_1 + k_2) \cdot c_{EA} = 0$$

$$k_2 \cdot c_{EA} - (k_2 + k_3) \cdot c_{EP} = 0$$

$$-r_A = k_3 \cdot c_{EP}$$

Find(r_A, c_E, c_{EA}, c_{EP}) \Rightarrow

$$\left[\begin{array}{l} -k_3 \cdot c_{Etot} \cdot k_2 \cdot k_1 \cdot \frac{c_A}{(k_1 \cdot k_2 + k_1 \cdot k_3 + k_2 \cdot k_3 + k_2 \cdot k_1 \cdot c_A + k_2 \cdot k_1 \cdot c_A + k_3 \cdot k_1 \cdot c_A)} \\ c_{Etot} \cdot \frac{(k_1 \cdot k_2 + k_1 \cdot k_3 + k_2 \cdot k_3)}{(k_1 \cdot k_2 + k_1 \cdot k_3 + k_2 \cdot k_3 + k_2 \cdot k_1 \cdot c_A + k_2 \cdot k_1 \cdot c_A + k_3 \cdot k_1 \cdot c_A)} \\ (k_2 + k_3) \cdot c_A \cdot k_1 \cdot \frac{c_{Etot}}{(k_1 \cdot k_2 + k_1 \cdot k_3 + k_2 \cdot k_3 + k_2 \cdot k_1 \cdot c_A + k_2 \cdot k_1 \cdot c_A + k_3 \cdot k_1 \cdot c_A)} \\ c_{Etot} \cdot k_2 \cdot k_1 \cdot \frac{c_A}{(k_1 \cdot k_2 + k_1 \cdot k_3 + k_2 \cdot k_3 + k_2 \cdot k_1 \cdot c_A + k_2 \cdot k_1 \cdot c_A + k_3 \cdot k_1 \cdot c_A)} \end{array} \right]$$

5. Simplify the rate equation by replacing the groups of rate constants (k_1 , k_2 , etc.) that appear in the solution by kinetic parameters (K_m , V_{max} , etc.) according to Cleland (1963).

$$V_{max} = \lim_{A \rightarrow \infty} (-r_A) = \frac{k_2 k_3}{(k_2 + k_{-2} + k_3)} c_{Etot}$$

so

$$k_{cat} = \frac{V_{max}}{c_{Etot}} = \frac{k_2 k_3}{(k_2 + k_{-2} + k_3)}$$

$$\frac{V_{max}}{2} = \lim_{A \rightarrow K_m} (-r_A)$$

so

$$K_{mA} = \frac{k_{-1}(k_{-2} + k_3) + k_2 k_3}{k_1(k_2 + k_{-2} + k_3)}$$

$$-r_A = \frac{\frac{k_1 k_2 k_3}{k_{-1}(k_{-2} + k_3) + k_2 k_3} c_A c_{Etot}}{1 + \frac{k_1(k_2 + k_{-2} + k_3)}{k_{-1}(k_{-2} + k_3) + k_2 k_3} c_A}$$



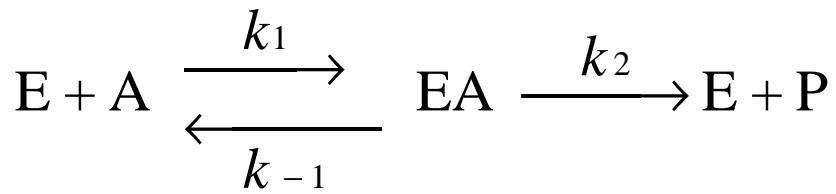
$$-r_A = \frac{V_{max} c_A}{1 + \frac{c_A}{K_m}}$$

5 microscopic
rate constants

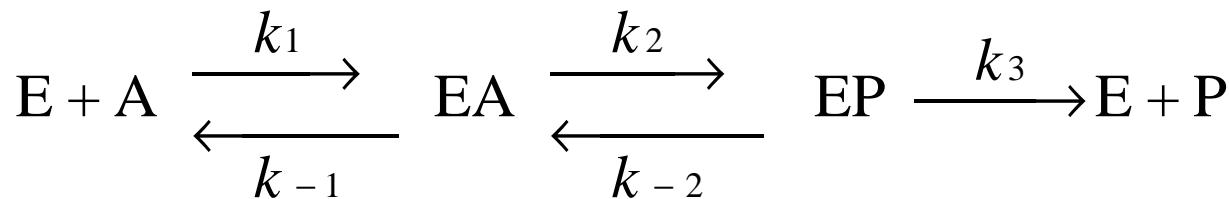


2 macroscopic
(steady-state)
kinetic parameters

Compare the two models that have been derived:



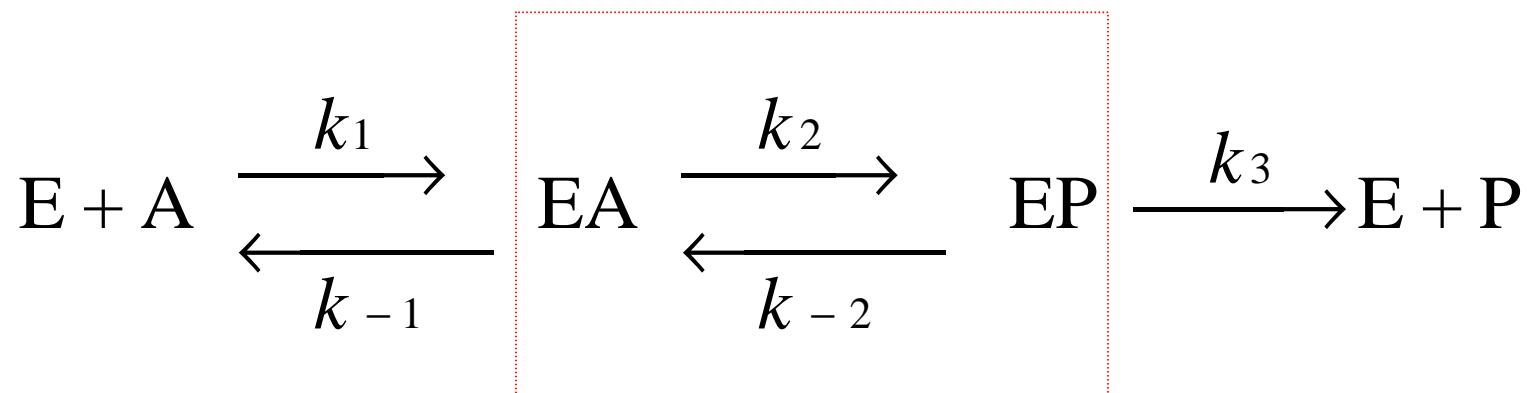
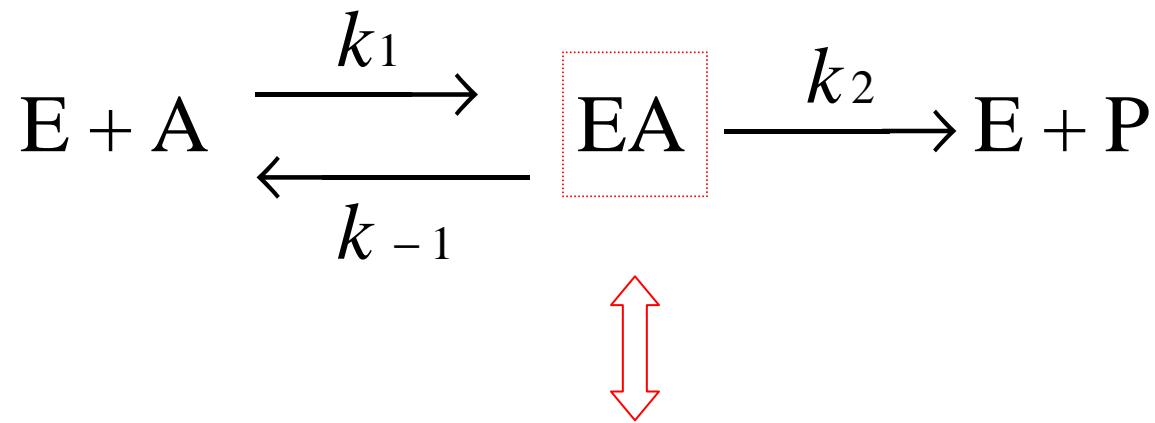
$$-r_A = \frac{\frac{k_1 k_2}{k_{-1} + k_2} c_A c_{Etot}}{1 + \frac{k_1}{k_{-1} + k_2} c_A} = \frac{\frac{V_{\max}}{K_m} c_A}{1 + \frac{c_A}{K_m}}$$



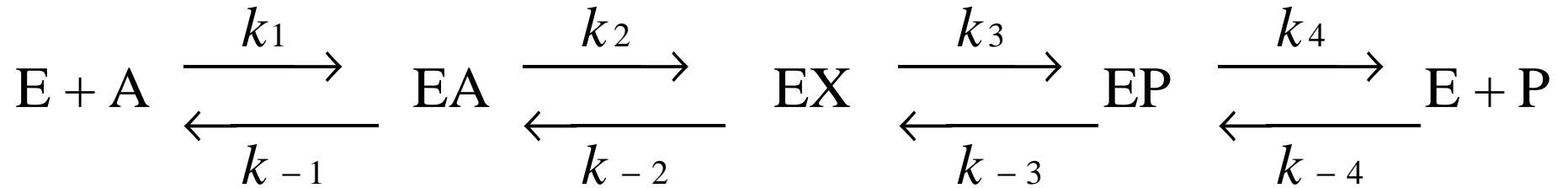
$$-r_A = \frac{\frac{k_1 k_2 k_3}{k_{-1}(k_{-2} + k_3) + k_2 k_3} c_A c_{Etot}}{1 + \frac{k_1(k_2 + k_{-2} + k_3)}{k_{-1}(k_{-2} + k_3) + k_2 k_3} c_A} = \frac{\frac{V_{\max}}{K_m} c_A}{1 + \frac{c_A}{K_m}}$$

Identical model equations result

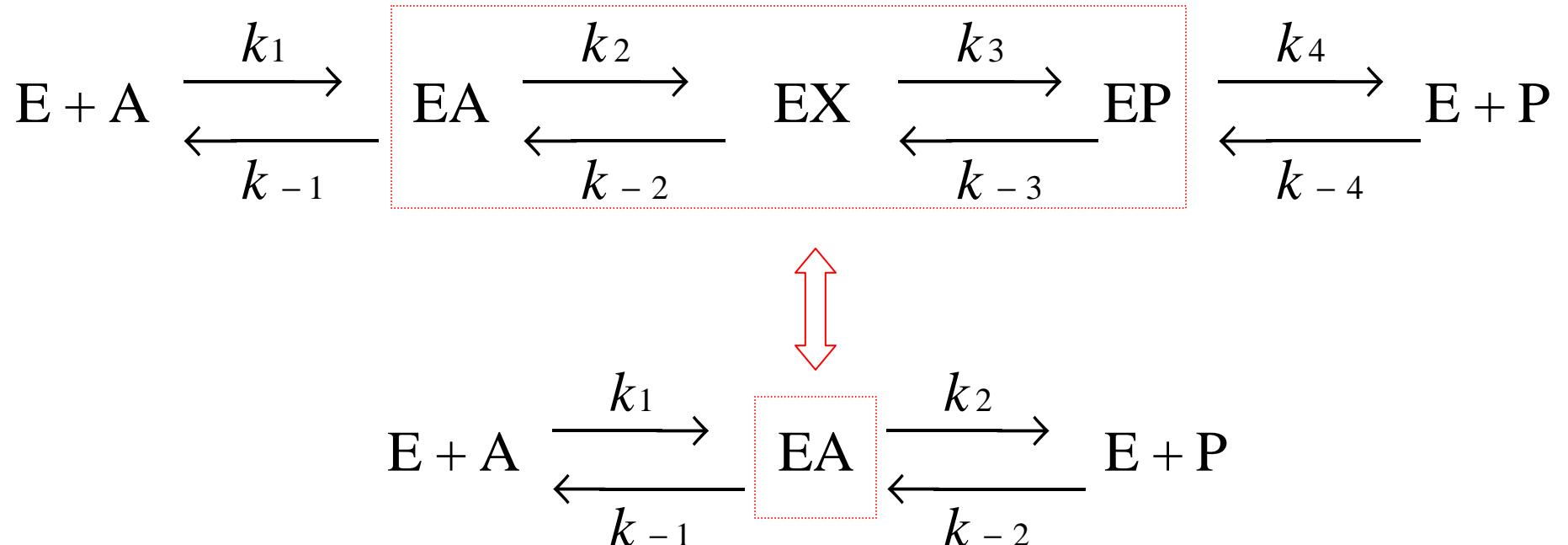
Isomerization steps can be lumped in one enzyme state:



Consider the following mechanism:

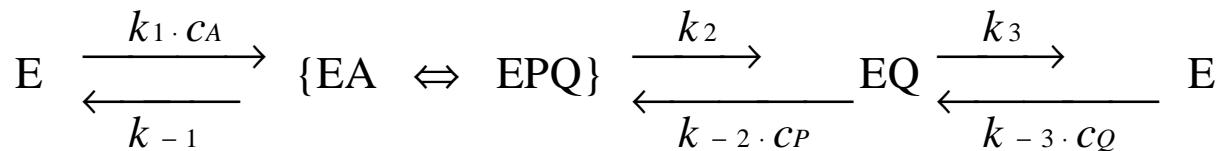


What is the simplest mechanism that will give the same rate equation?



UNI-BI REACTIONS

compulsory order



$$-r_A = \frac{\frac{V_1}{K_{mA}}(c_A - \frac{c_P c_Q}{K_{eq}})}{1 + \frac{c_A}{K_{mA}} + \frac{K_{mQ}}{K_{iQ}} \frac{c_P}{K_{mP}} + \frac{c_Q}{K_{iQ}} + \frac{c_P}{K_{mP}} \frac{c_Q}{K_{iQ}} + \frac{c_A}{K_{mA}} \frac{c_P}{K_{iP}}}$$

random order



Example:

Mandelonitrile lyase

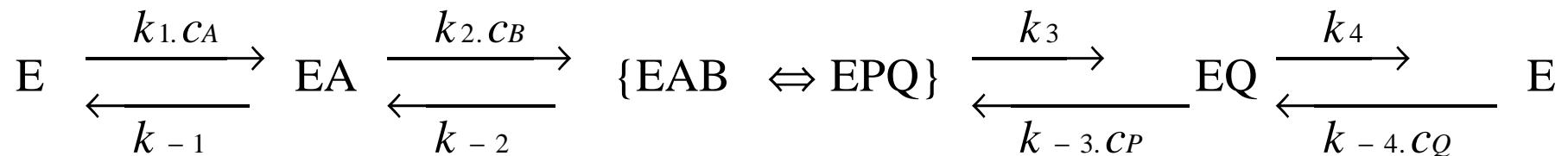
A = mandelonitrile

P = HCN

Q = benzaldehyde

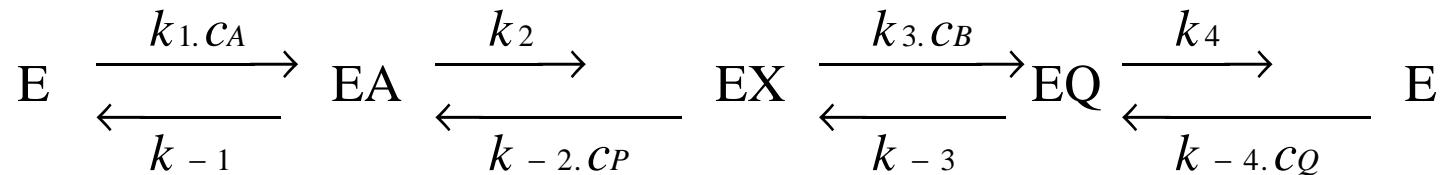
BI-BI REACTIONS

ordered ternary complex mechanism



Example: lactate dehydrogenase
(A = NAD⁺)

ping-pong mechanism



Example: penicillin amidase (A = penicillin)

Table 1. Pseudo-steady state parameters for some kinetic models (Cleland, 1963; Cornish-Bowden, 1995). Bi-uni definitions follow from uni-bi by reversal of A and Q, B and P, and + and -

Par	Uni-uni	Uni-bi ordered	Bi-bi ordered ternary-complex	Bi-bi ping-pong
V_1	$k_2 C_{\text{Etot}}$	$k_2 k_3 C_{\text{Etot}}/(k_2+k_3)$	$k_3 k_4 C_{\text{Etot}}/(k_3+k_4)$	$k_2 k_4 C_{\text{Etot}}/(k_2+k_4)$
V_{-1}	$k_1 C_{\text{Etot}}$	$k_1 C_{\text{Etot}}$	$k_1 k_2 C_{\text{Etot}}/(k_1+k_2)$	$k_1 k_3 C_{\text{Etot}}/(k_1+k_3)$
K_{mA}	$(k_1+k_2)/k_1$	$(k_1+k_2)k_3/[k_1(k_2+k_3)]$	$k_3 k_4/[k_1(k_3+k_4)]$	$(k_1+k_2)k_4/[k_1(k_2+k_4)]$
K_{mB}			$(k_2+k_3)k_4/[k_2(k_3+k_4)]$	$k_2(k_3+k_4)/[(k_2+k_4)k_3]$
K_{mP}	$(k_1+k_2)/k_2$	$(k_1+k_2)/k_2$	$k_1(k_2+k_3)/[(k_1+k_2)k_3]$	$(k_1+k_2)k_3/[(k_1+k_3)k_2]$
K_{mQ}		k_1/k_3	$k_1 k_2/[(k_1+k_2)k_4]$	$k_1(k_3+k_4)/[(k_1+k_3)k_4]$
K_{iA}		k_1/k_1	k_1/k_1	k_1/k_1
K_{iB}			$(k_1+k_2)/k_2$	k_3/k_3
K_{iP}		$(k_2+k_3)/k_2$	$(k_3+k_4)/k_3$	k_2/k_2
K_{iQ}		k_3/k_3	k_4/k_4	k_4/k_4
K_{eq}	$k_1 k_2/(k_1 k_2)$	$k_1 k_2 k_3/(k_1 k_2 k_3)$	$k_1 k_2 k_3 k_4/(k_1 k_2 k_3 k_4)$	$k_1 k_2 k_3 k_4/(k_1 k_2 k_3 k_4)$

ordered ternary complex mechanism

$$-r_A = \frac{\frac{V_1}{K_{iA} K_{mB}} (c_A c_B - c_P c_Q / K_{eq})}{(1 + \frac{c_A}{K_{iA}} + \frac{K_{mA}}{K_{iA}} \frac{c_B}{K_{mB}} + \frac{c_A}{K_{iA}} \frac{c_B}{K_{mB}} + \frac{K_{mQ}}{K_{iQ}} \frac{c_P}{K_{mP}} + \frac{c_Q}{K_{iQ}} + \frac{c_P}{K_{mP}} \frac{c_Q}{K_{iQ}} + \frac{K_{mQ}}{K_{iQ}} \frac{c_A}{K_{iA}} \frac{c_P}{K_{mP}} + \frac{K_{mA}}{K_{iA}} \frac{c_B}{K_{mB}} \frac{c_Q}{K_{iQ}} + \frac{c_A}{K_{iA}} \frac{c_B}{K_{mB}} \frac{c_P}{K_{iP}} + \frac{c_B}{K_{iB}} \frac{c_P}{K_{mP}} \frac{c_Q}{K_{iQ}})}$$

Suppose $c_P = 0$

$$-r_A = \frac{\frac{V_1}{K_{iA} K_{mB}} c_A c_B}{1 + \frac{c_A}{K_{iA}} + \frac{K_{mA}}{K_{iA}} \frac{c_B}{K_{mB}} + \frac{c_A}{K_{iA}} \frac{c_B}{K_{mB}} + \frac{c_Q}{K_{iQ}} + \frac{K_{mA}}{K_{iA}} \frac{c_B}{K_{mB}} \frac{c_Q}{K_{iQ}}}$$

Also suppose $c_B \rightarrow \infty$

$$-r_A = \frac{\frac{V_1}{K_{iA} K_{mB}} c_A c_B}{\frac{K_{mA}}{K_{iA}} \frac{c_B}{K_{mB}} + \frac{c_A}{K_{iA}} \frac{c_B}{K_{mB}} + \frac{K_{mA}}{K_{iA}} \frac{c_B}{K_{mB}} \frac{c_Q}{K_{iQ}}} = \frac{V_1 c_A}{K_{mA} + c_A + K_{mA} \frac{c_Q}{K_{iQ}}}$$

competitive inhibition

$$-r_A = \frac{V_{\max} c_A / K_m}{1 + c_A / K_m + c_I / K_i}$$

→ Inhibition type follows from the mechanism (and vice versa)

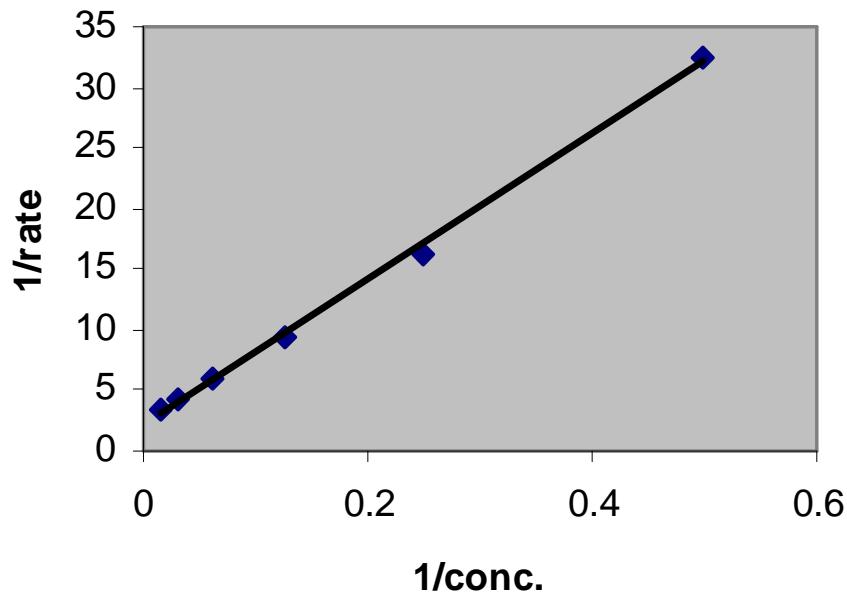
→ Mechanistic information can directly be used for process simulation

Estimation of steady-state kinetic parameters

- Simply measuring substrate consumption/product formation
- Popular on-line analyses: UV / fluorescence / pH stat
- Initial rate analysis or Progress curve analysis

Initial rate analysis

Lineweaver-Burk plot



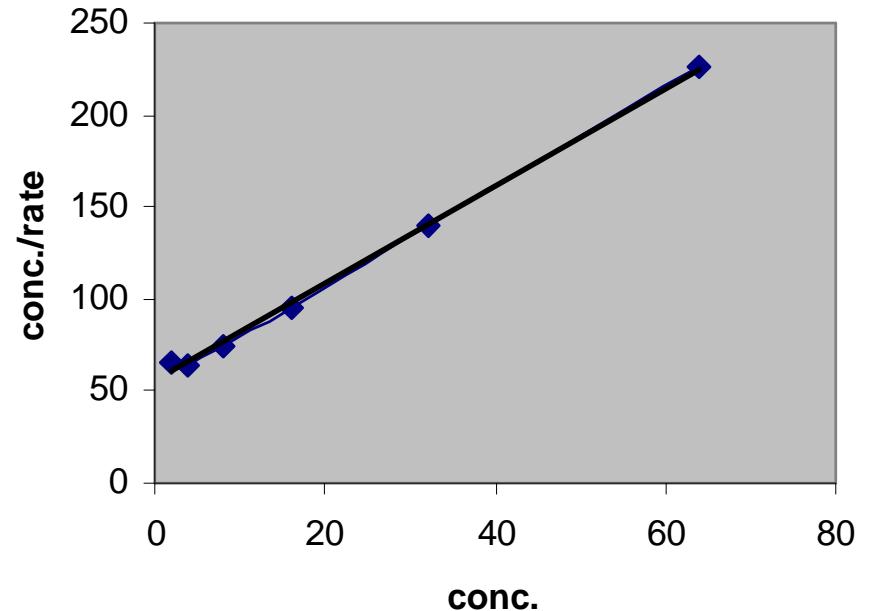
$$\frac{1}{r} = \frac{1}{V_{\max}} + \frac{K_m}{V_{\max}} \frac{1}{c_A}$$

$$V_{\max} = \frac{1}{\text{intercept}}$$

$$K_m = \text{slope} \cdot V_{\max}$$

Hanes plot

(more even error distribution)

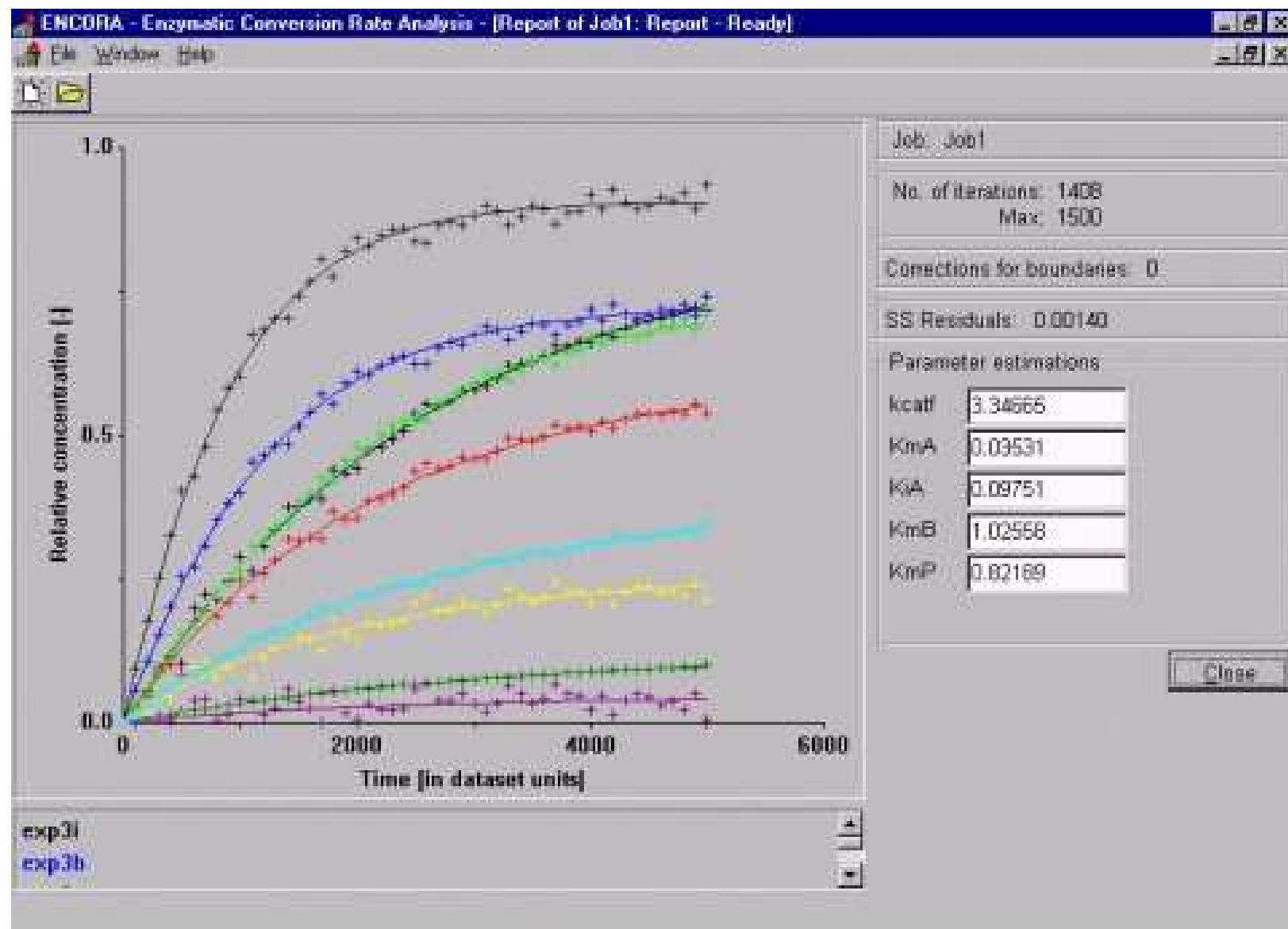


$$\frac{c_A}{r} = \frac{c_A}{V_{\max}} + \frac{K_m}{V_{\max}}$$

$$V_{\max} = \frac{1}{\text{slope}}$$

$$K_m = \text{intercept} \cdot V_{\max}$$

Progress curve analysis



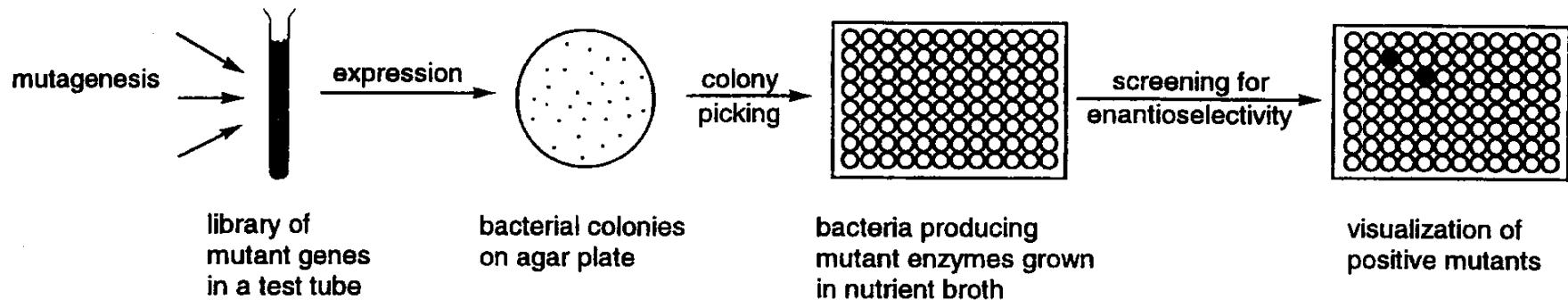
Comparision of methods

Method	Initial rate	Progression curve
# of samples	>5 up to 5-10% conversion	>20 up to full conversion
Analytical requirement	Higher sensitivity, also off-line	Lower sensitivity, only on-line
# of experiments	5 for k_{cat} and K_m ; +20 per K_i	3 for k_{cat} and K_m ; +3 per K_i
Product concentration	$c_P \approx c_{P0}$; $c_Q \approx c_{Q0}$	According to full rate equation
Product degradation	No	Yes
Enzyme degradation	No	Yes
Regression method	Linear possible (Lineweaver-Burk, Hanes)	Non-linear (Sophisticated software)
Calculations	Easy	Difficult
Results	Key parameters	All parameters
Application area	Basic kinetic studies	Process development

High-throughput methods



Screening for more active/selective/stable enzymes

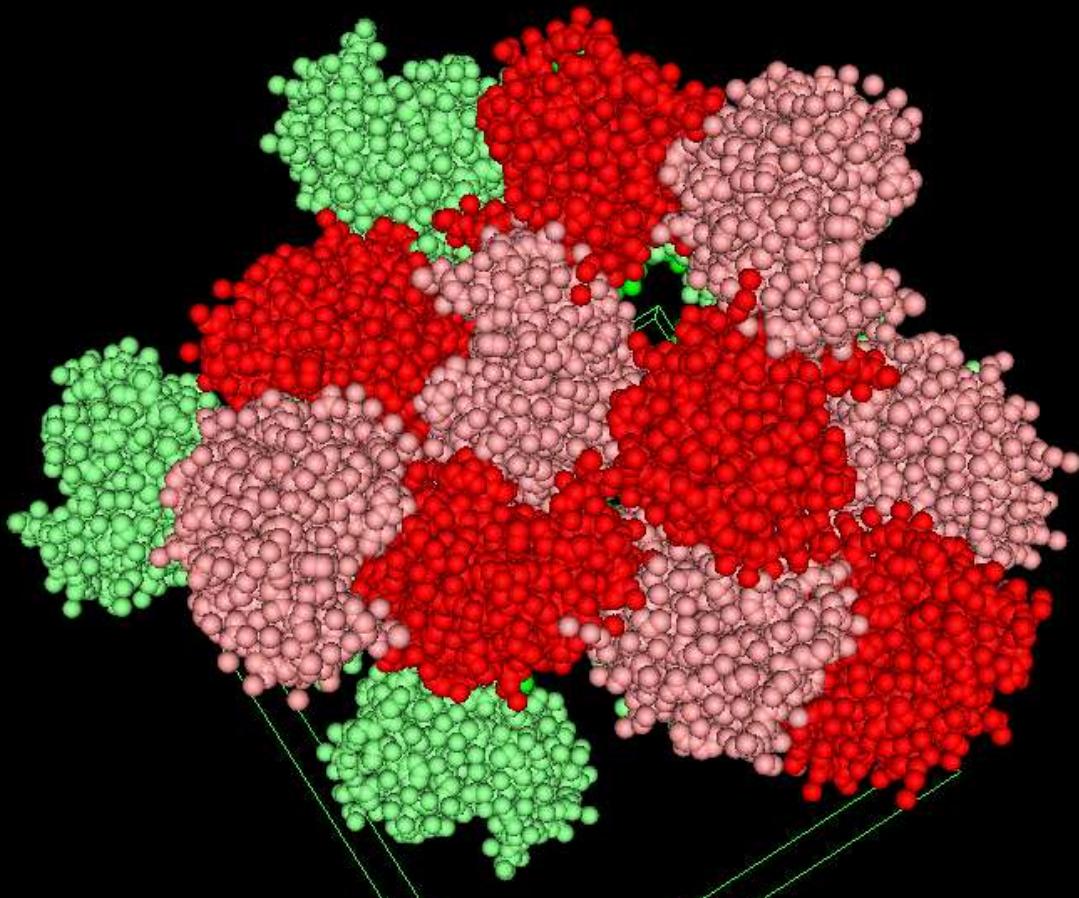


- Generation of improved enzymes has become highly sophisticated
- Kinetic assays are the usual bottleneck

Immobilized enzymes

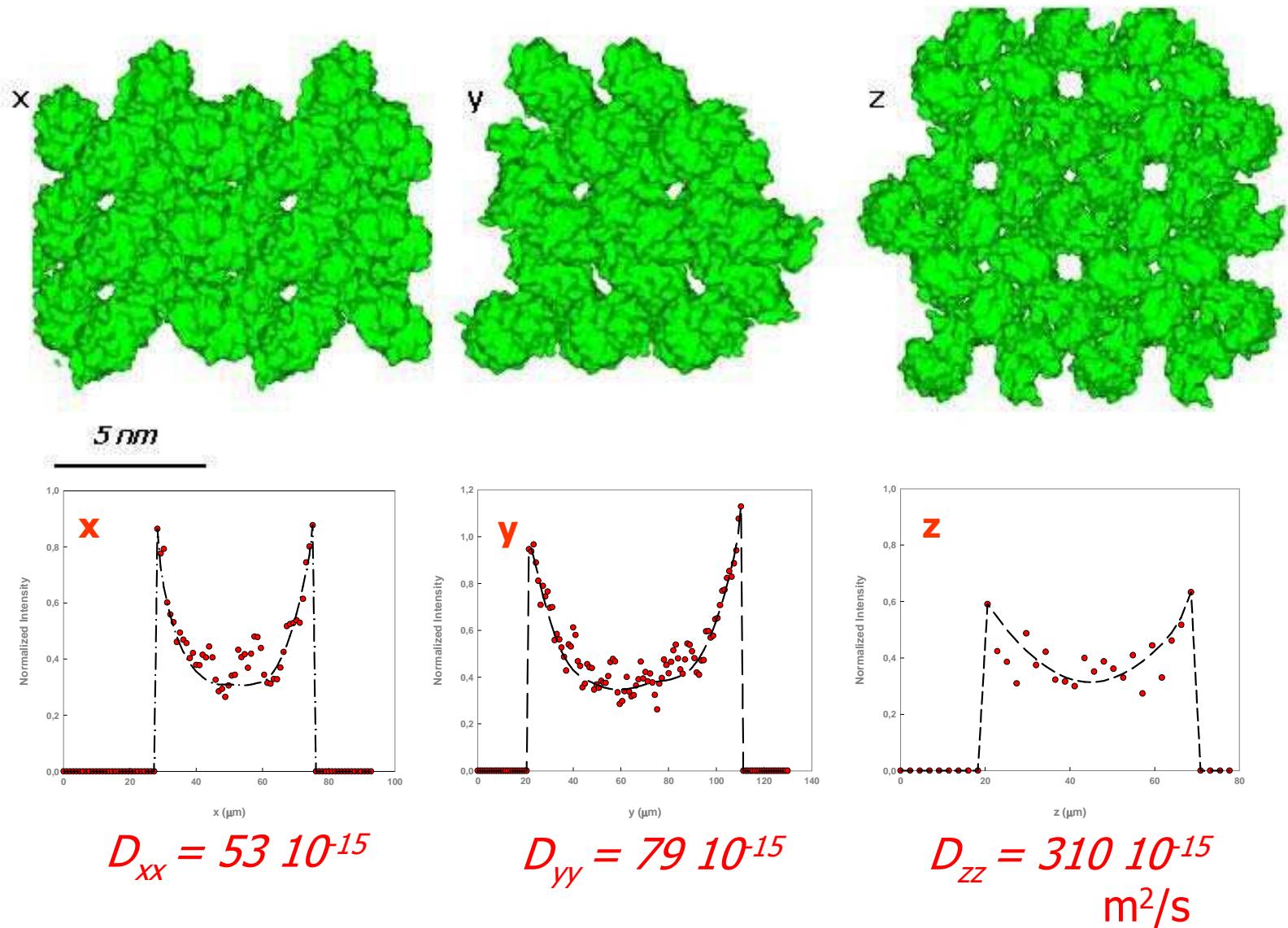
- Usually measurement of dissolved substrate/product; reaction-diffusion model → intrinsic kinetic parameters
- In some cases on-line measurement of adsorbed solute concentration (see next sheets)

Porous crystal of lysozyme



Picture made with software from <http://pymol.sourceforge.net/>

Diffusion visualization by 3-D laser scanning confocal microscopy



Other issues in enzyme kinetics

- Variable temperature or pH; inactivating enzyme
- Parallel or consecutive reactions catalyzed by the same enzyme (depolymerizations; kinetic resolutions)
- Parallel or consecutive reactions catalyzed by other enzymes (lignocellulose hydrolysis)

How to get the microscopic constants?

$$-r_A = \frac{\frac{k_1 k_2 k_3}{k_{-1}(k_{-2} + k_3) + k_2 k_3} c_A c_{Etot}}{1 + \frac{k_1(k_2 + k_{-2} + k_3)}{k_{-1}(k_{-2} + k_3) + k_2 k_3} c_A}$$



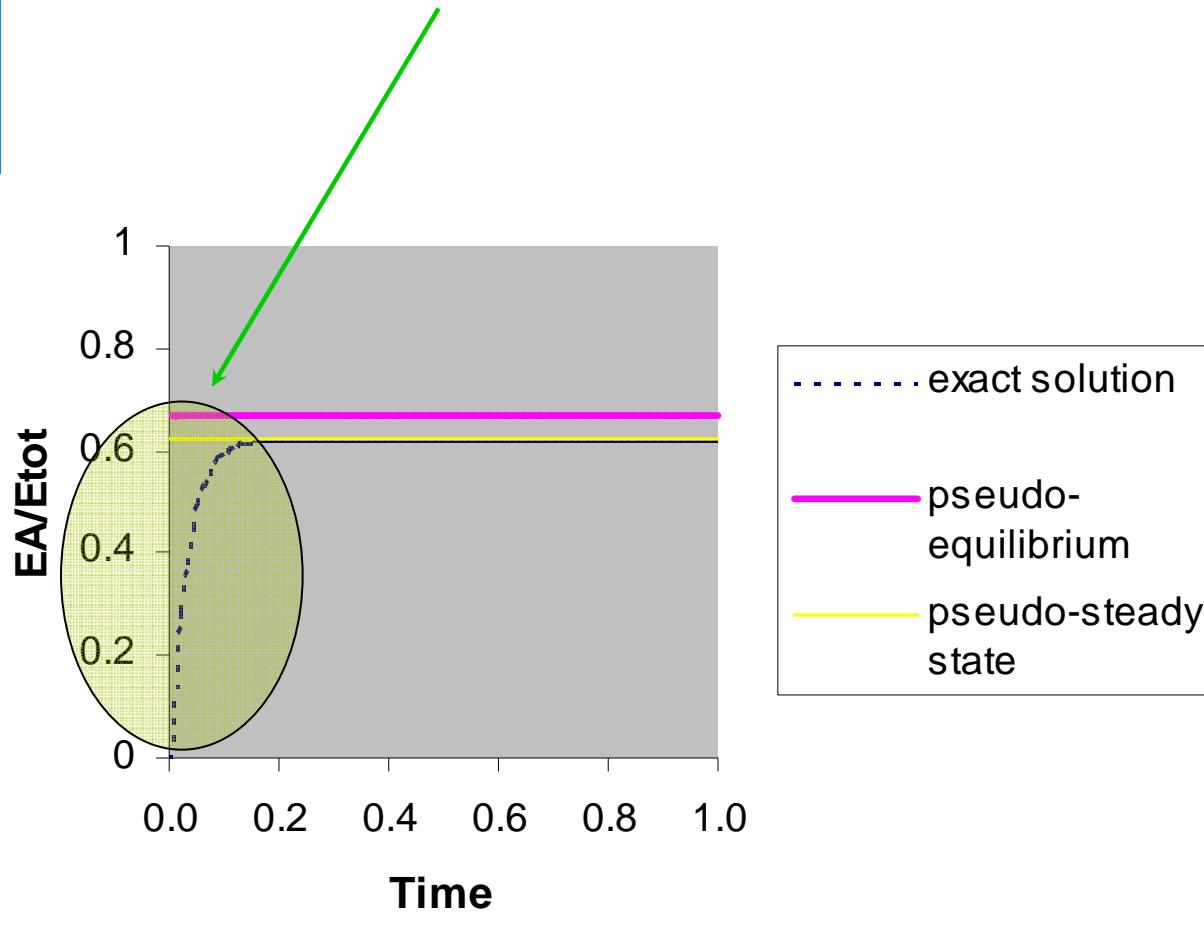
$$-r_A = \frac{V_{max} c_A}{1 + \frac{c_A}{K_m}}$$

5 microscopic
rate constants



2 macroscopic
(steady-state)
kinetic parameters

Pre-steady-state kinetics



$$c_{A0} = 1$$

$$c_{E_{\text{tot}}} = 0.001$$

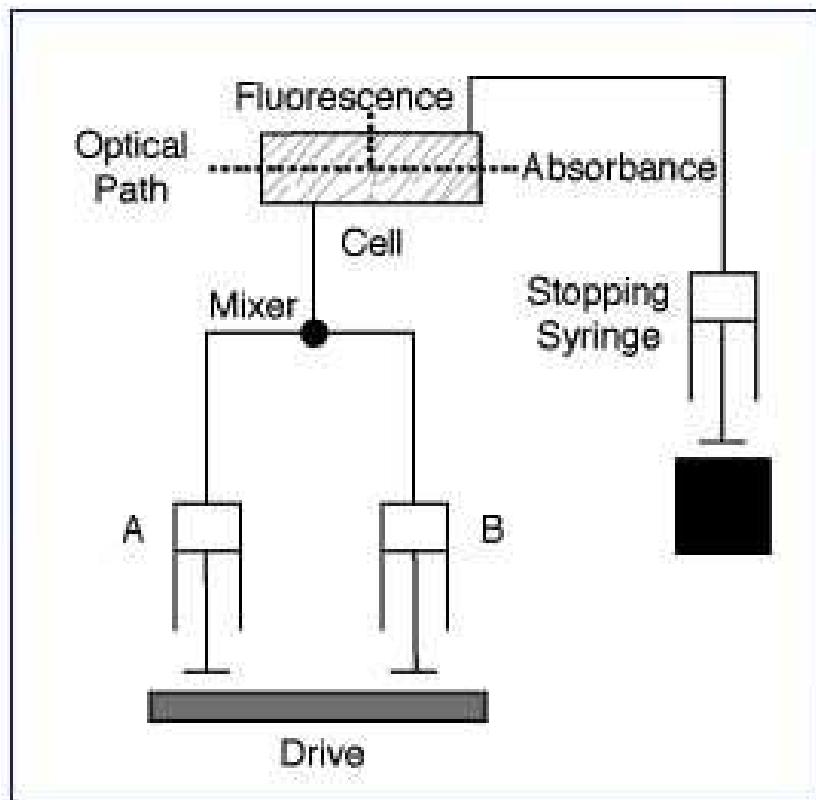
$$k_1 = 20$$

$$k_{-1} = 10$$

$$k_2 = 2$$

(arbitrary units)

Stopped flow equipment

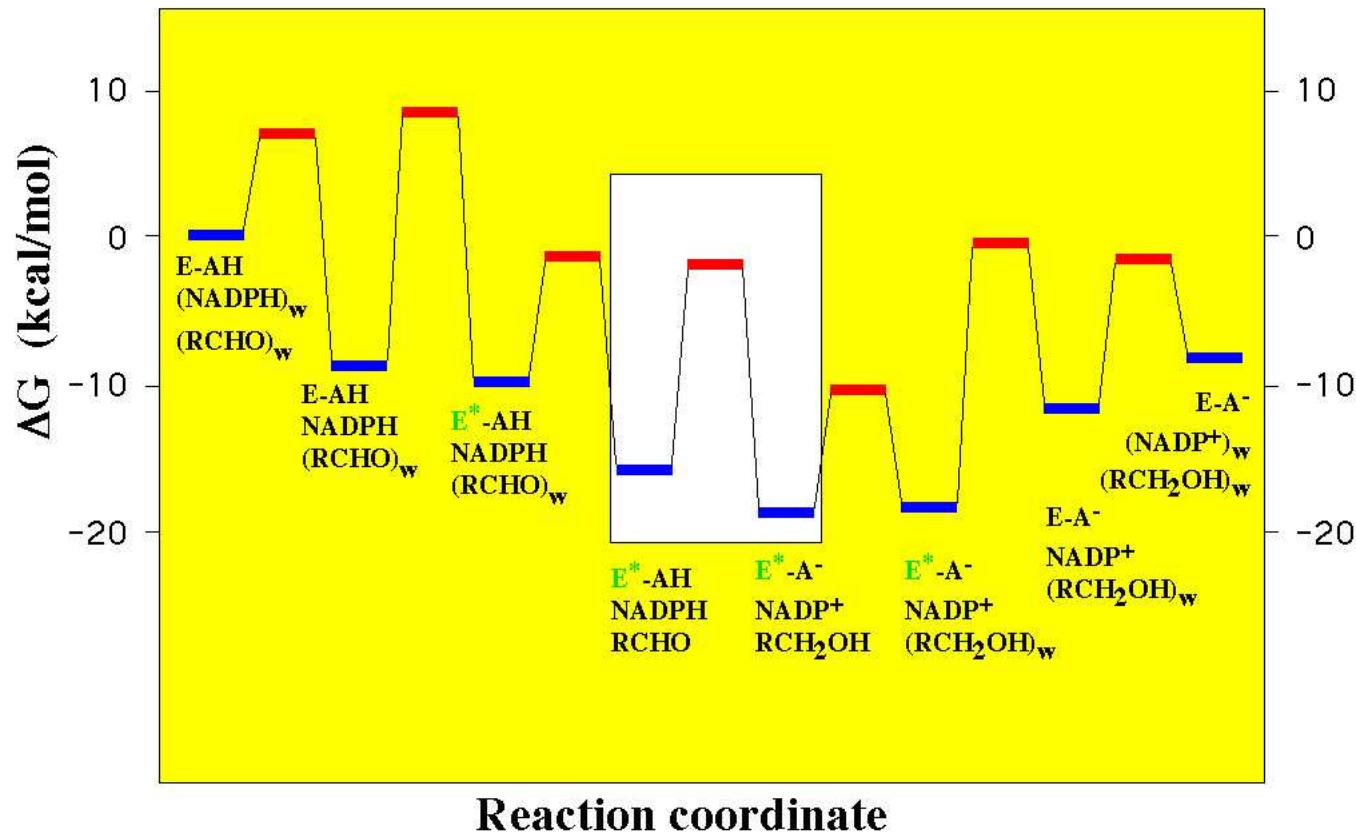


Lisbet S. Christensen, lsm@life.ku.dk

Applied Photophysics, Inc.

(Human) Aldose reductase

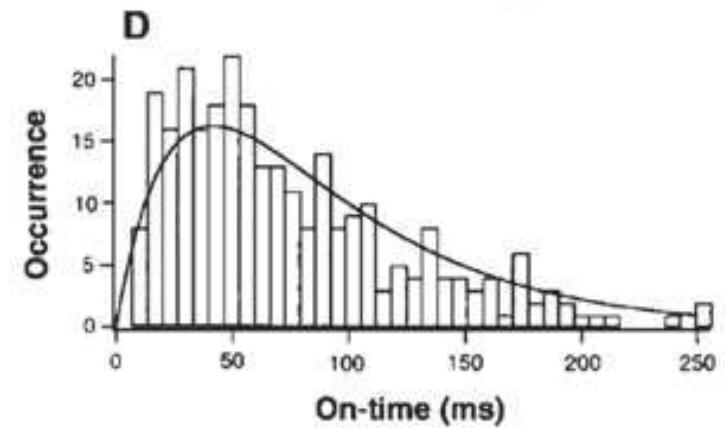
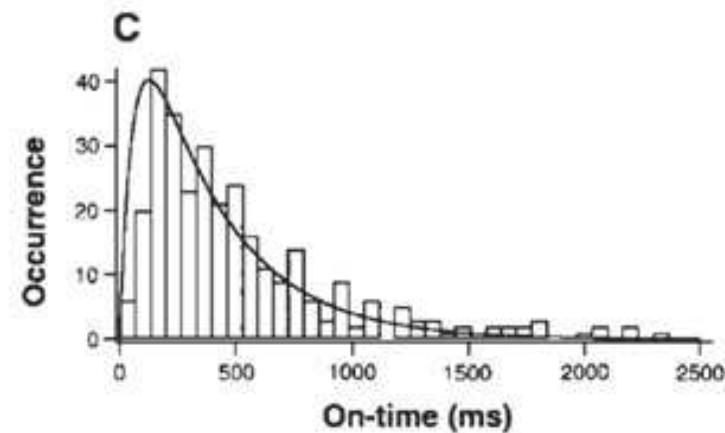
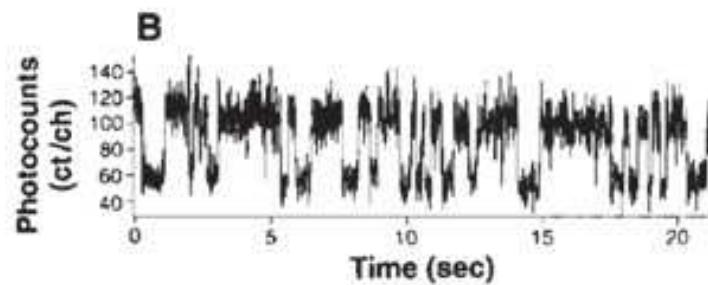
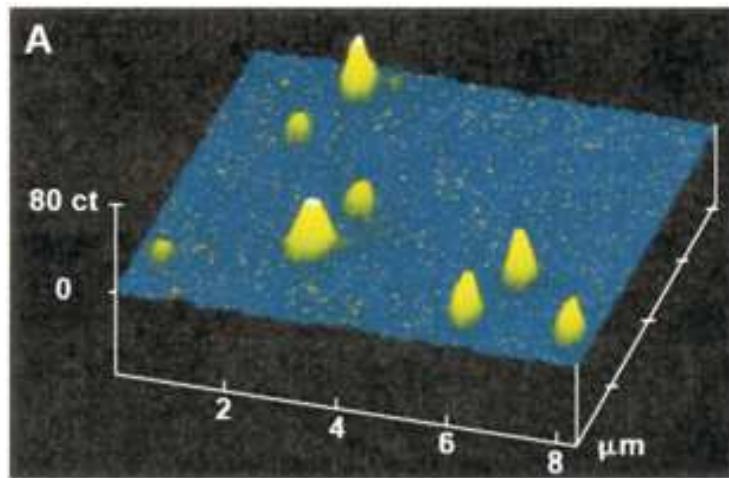
Free energy profile



Varnai, P. and Warshel, A. (2000) *J. Am. Chem. Soc.*, 122, 3849-3860

Single enzyme kinetics

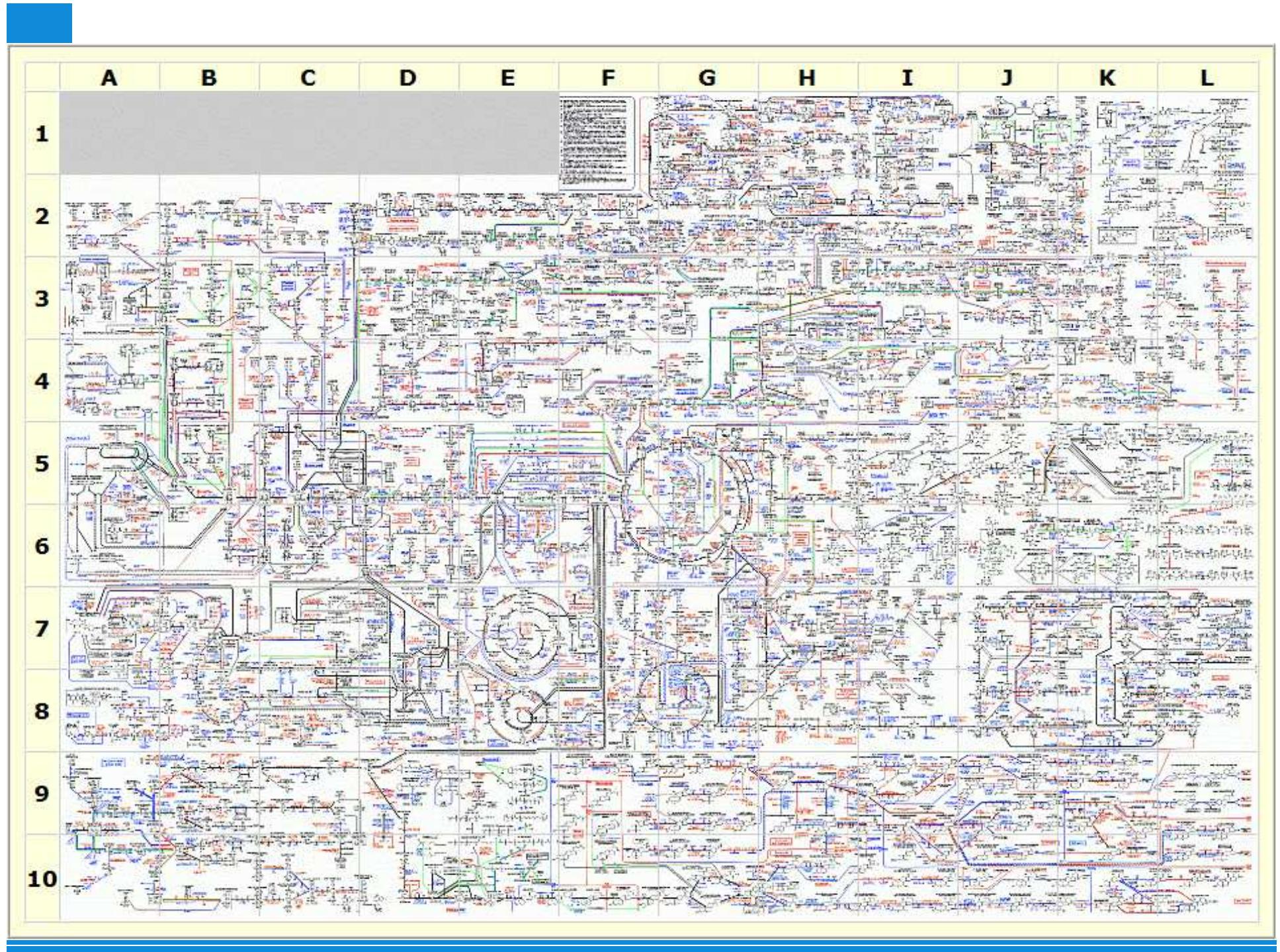
Because different enzyme molecules have different conformations



Kinetics of microbial cells

- Thousands of regulated reactions (from DNA level to metabolite level)
 - Regulation leads to continuous fast changes of rates → chemostats (CSTRs) to obtain reproducible steady states
 - Conventionally 5-10 overall rates externally measured (C-source, N-source, O₂, CO₂, H⁺, product, cell mass, ...)
- All reactions lumped in 2-3 overall reactions (~6 kinetic parameters)
- Unsatisfactory understanding, so empirical genetic engineering

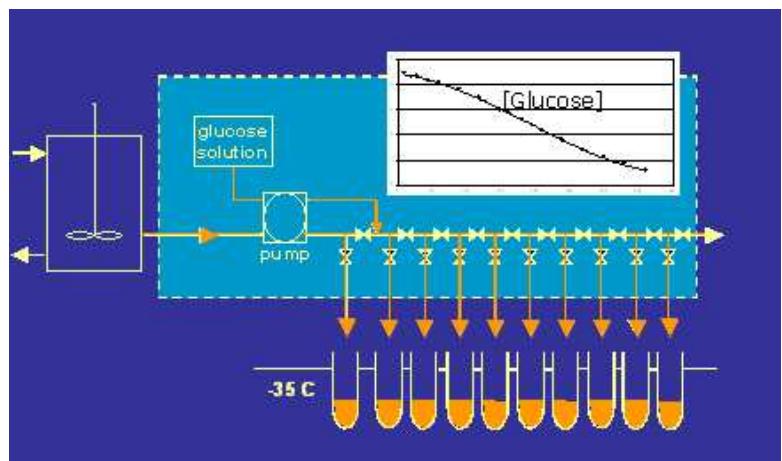
NEW: Systems biology approach: measure and model *a//* rates



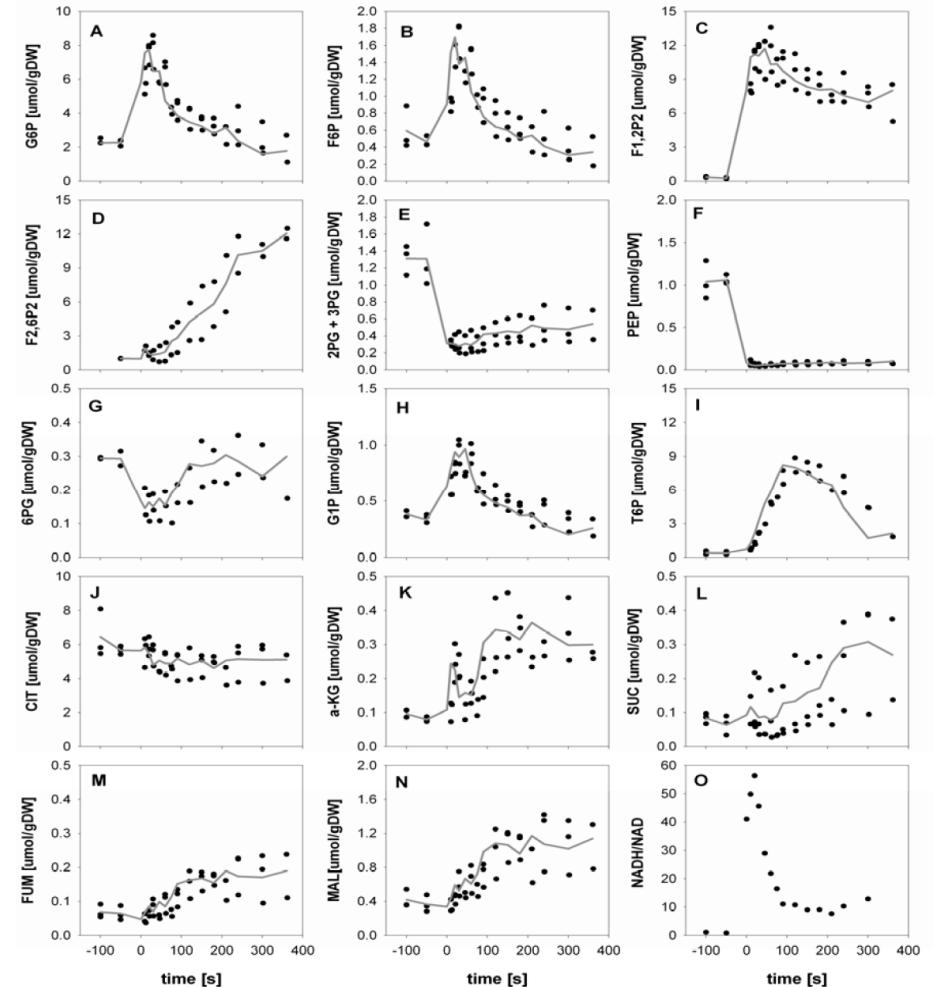
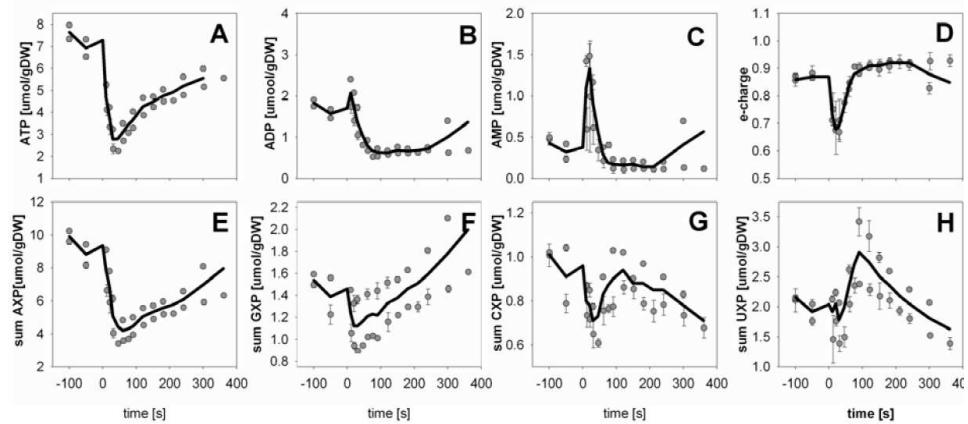
BioScope

- 0-500 s stimulus-response of cells growing in a steady-state chemostat
- Rapid sampling, quenching, metabolite extraction, isotope dilution LC/MS for ~200 intracellular metabolites.
- Genome wide transcript levels are measured with Affymetrix chips
- Protein level measurements: in progress
- Dynamic simulations to model the metabolic rates (using phenomenological enzyme kinetics)

Heijnen group, Biotechnology, TU Delft



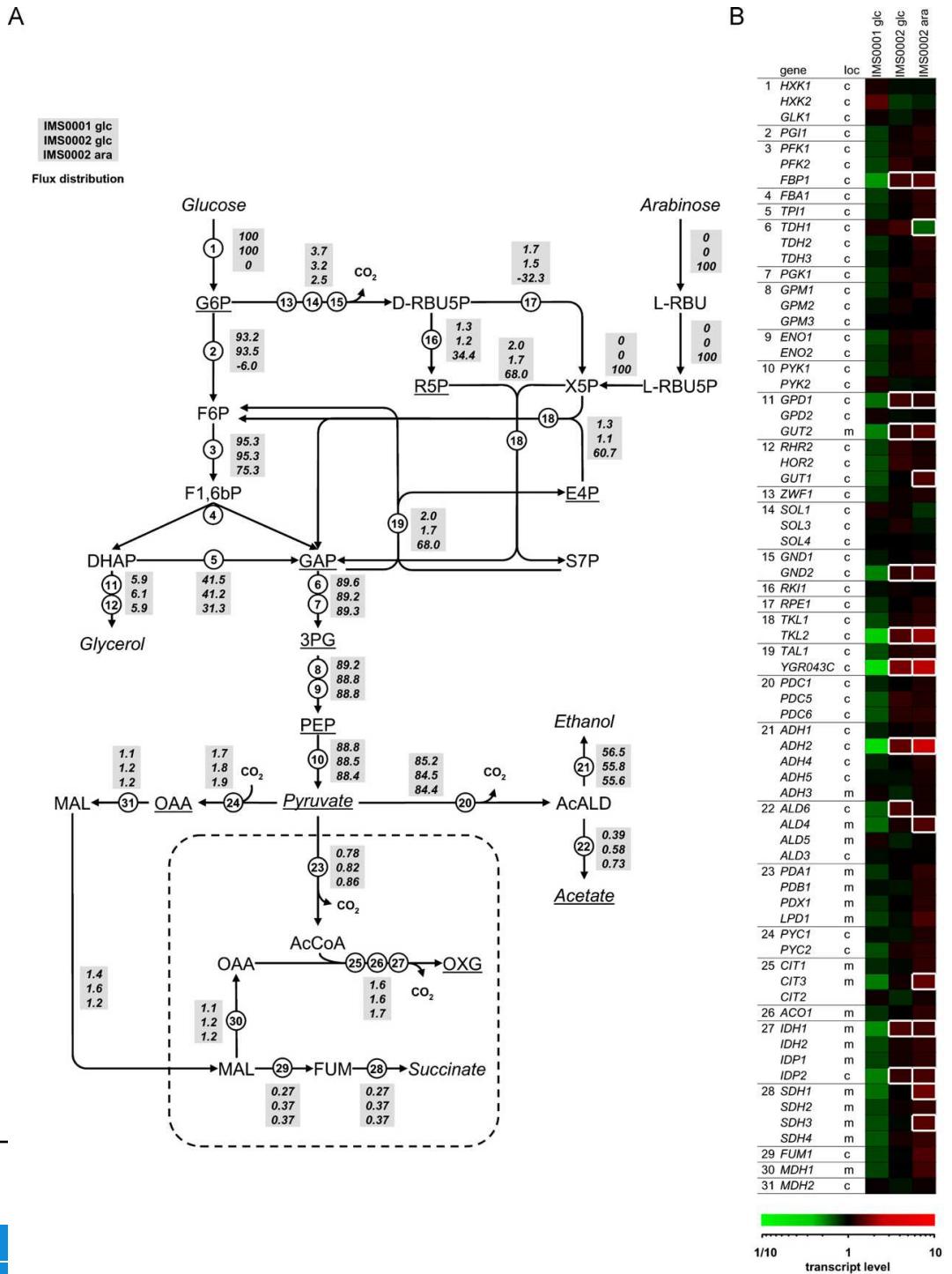
Example results 1



Example results 2

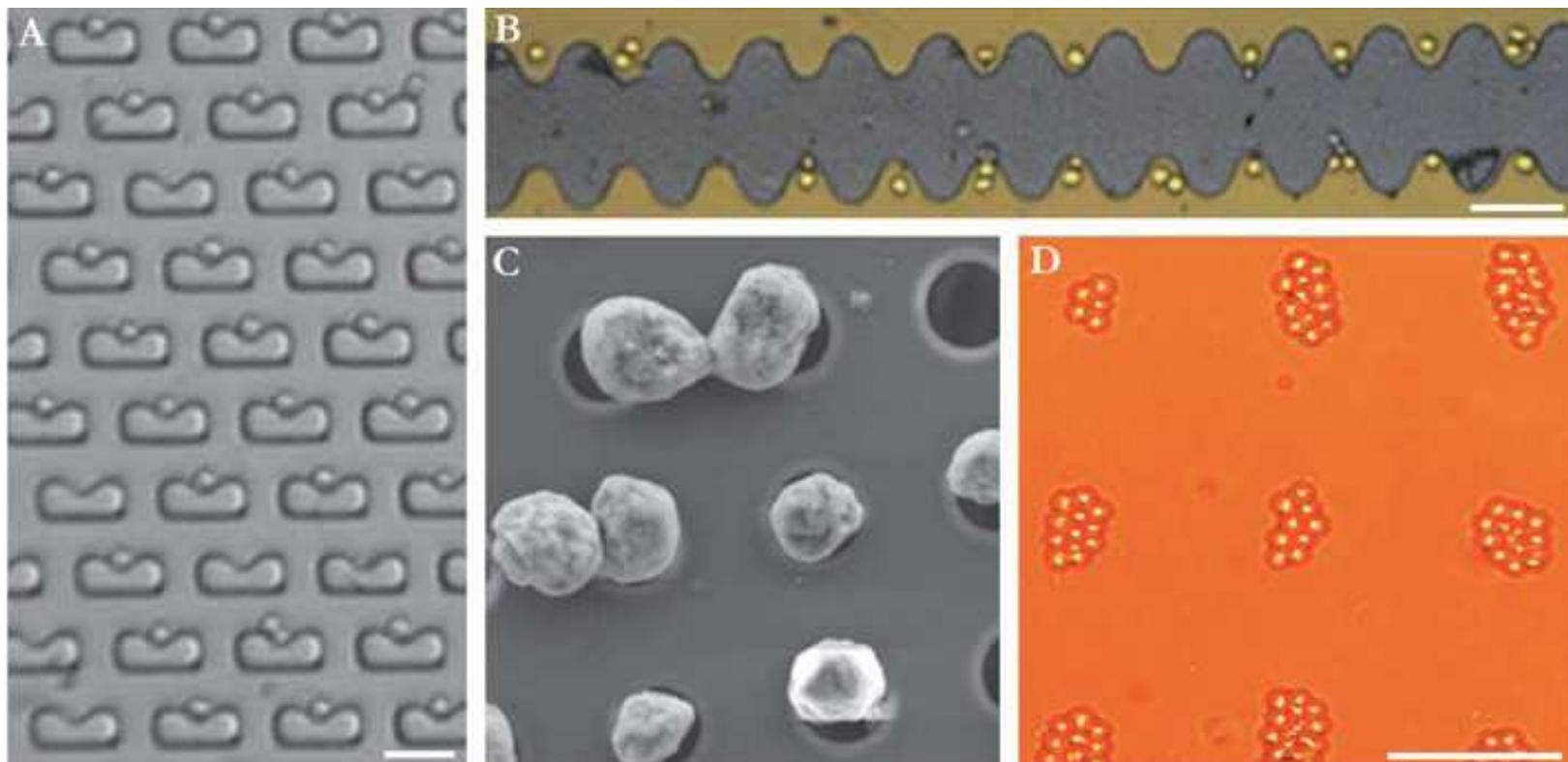
- Metabolic flow rates in ethanol fermentation
- Explains results of genetic engineering
- Provides new genetic engineering targets

Wisselink et al., Metabolic Eng. 2010



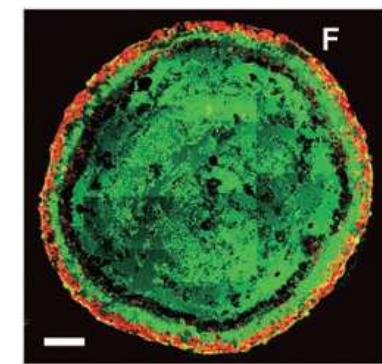
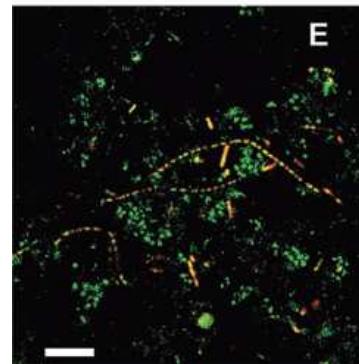
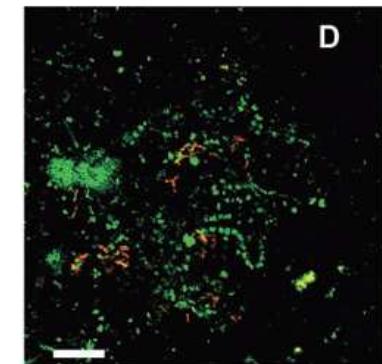
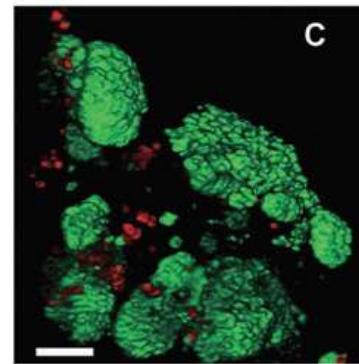
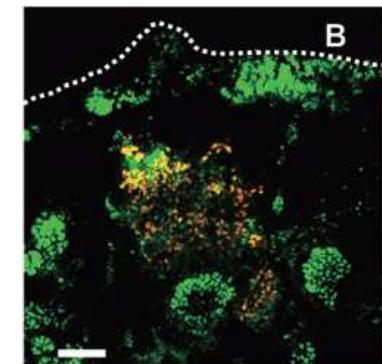
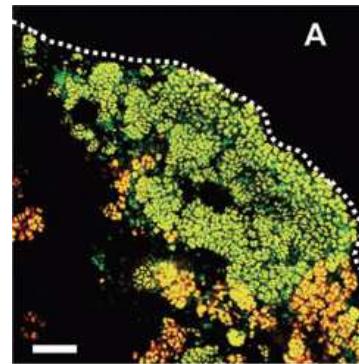
Single cell kinetics (Microfluidics)

Because different cells behave differently – especially temporally

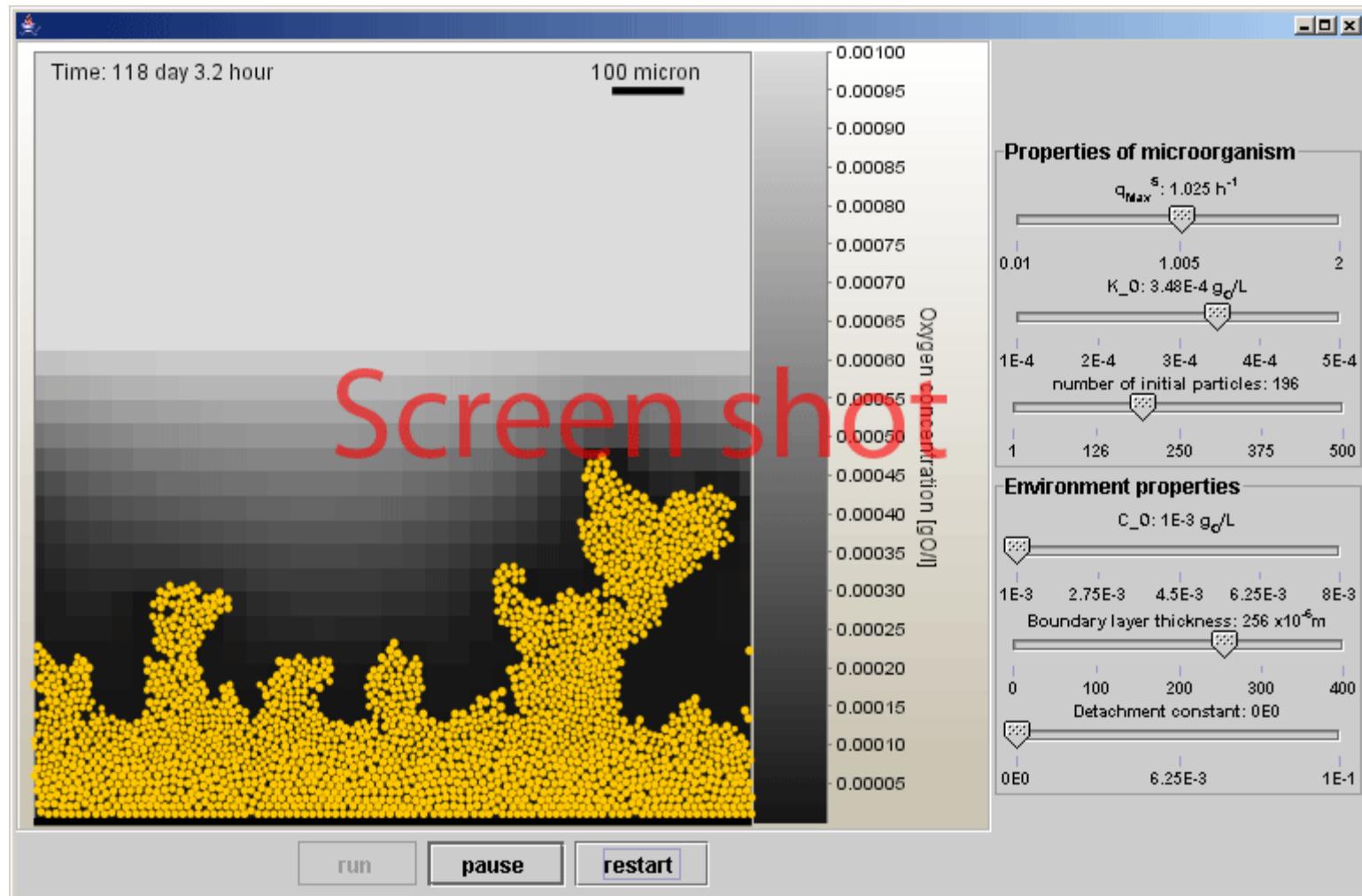


Mixed cultures

- Traditionally: Overall rates measured, black block model
- Fluorescent probes to differentiate populations of microorganisms
- Biofilms: reaction-diffusion



Monospecies 2D biofilm model



Conclusions

- Steady-state enzyme kinetics are mature; used in biochemistry just like in bioprocess development
- Pre-steady state and single enzyme methods are used for advanced enzymology
- High-throughput assays are bottlenecks in development of biocatalytic processes
- Monitoring individual cells is becoming important
- Numerous new methods to determine intracellular rates drive the field of Systems Biology