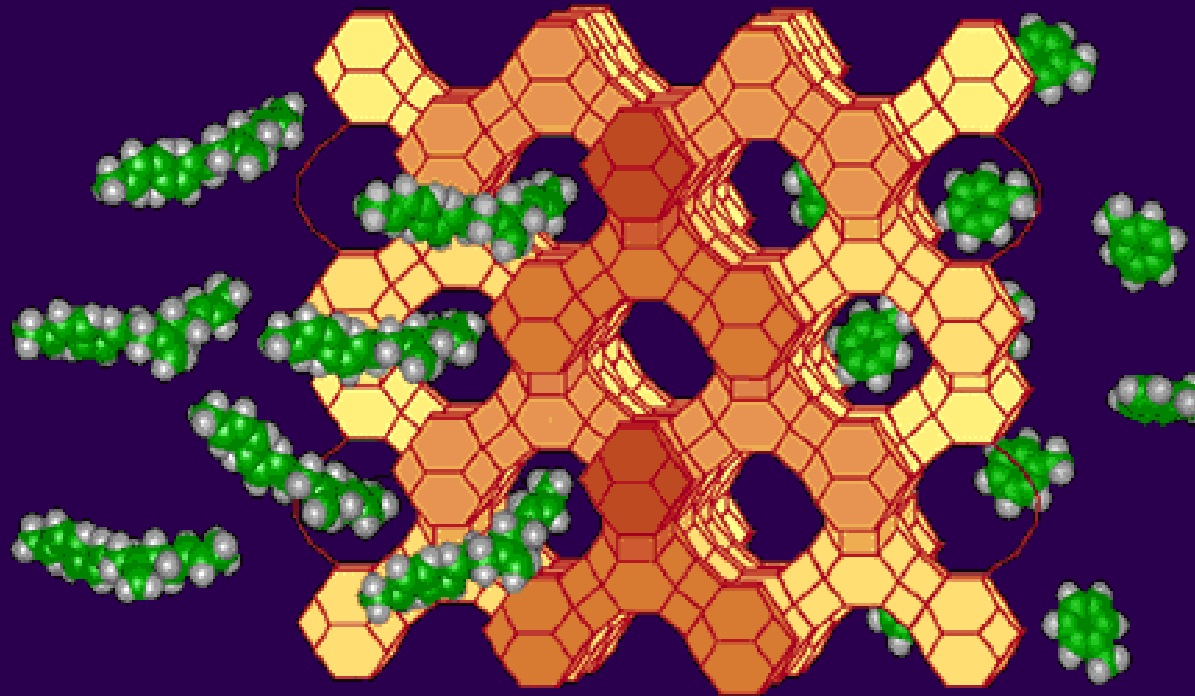


The Importance of Physisorption in Chemical Kinetics : Zeolite Catalyzed Reactions

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Dienst Chemische Ingenieurstechniek,
VUB



Zeolite Catalysis: Diffusion, Adsorption, Reaction



Interference of several adsorption and reaction phenomena

Adsorption effects

Zeolite:

Si/Al, pore diameter,
topology, polarity

Adsorbate:

molecular weight, shape,
polarity

Catalytic effects

Zeolite:

Si/Al, acidity,
structure

Reactant:

molecular weight, shape

Modeling:

Exact adsorption and
reaction parameters

Insight in shape selective
and catalytic effects

K' , q_{sat}

ΔH_0 , ΔS_0 ,

Interaction-
parameters

k_{isom} ,

k_A , k_{B1} , ...

E_{act}

Overview

✓ Adsorption

- Low zeolite coverage
- Intermediate coverage
- Complete coverage

✓ Reaction

- Hydrocracking of alkanes on Y zeolites
 - Vapor phase
 - Liquid phase

Adsorption

- **Chromatographic techniques**
- **C5 - C12 linear and branched alkanes, alkenes, ...**
- **20 - 400 °C**
- **Gas, vapor and liquid phase**
- **Series of zeolites**

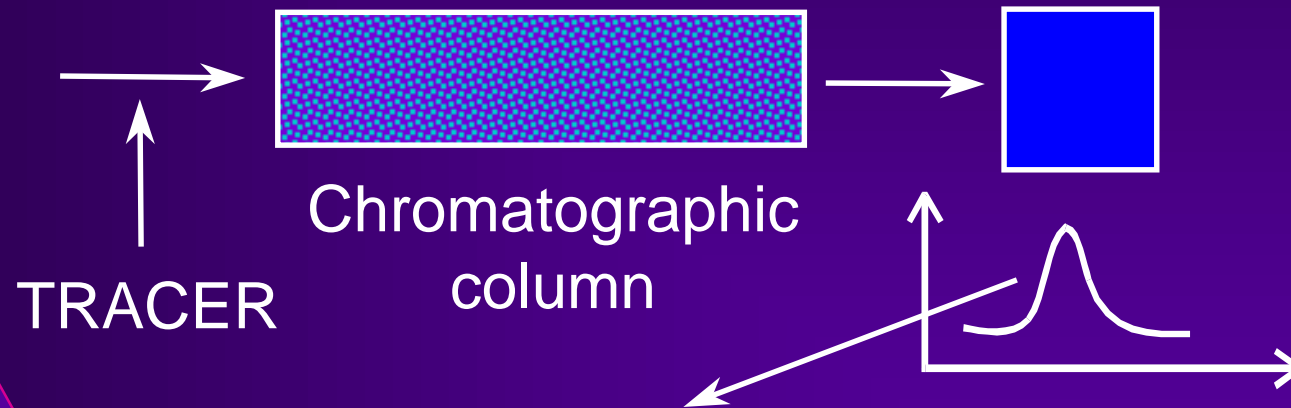
⇒ rational relationships between system parameters and adsorption properties ???

Gas and liquid chromatography

MOBILE PHASE

- inert gas
- inert gas + component
- mixture
- liquid

DETECTOR: TCD,
MS, Refractometer



K' , q_{sat}
 ΔH_0 , ΔS_0 ,
Interaction-
parameters

$$\mu_i = \frac{L}{v_f} \left[\varepsilon + \varepsilon(1-x) \frac{\partial q_1}{\partial p_i} \right]$$

Methods of moments: adsorption constants

$$v_f p \frac{\partial x_i}{\partial z} + (\varepsilon_{ext} + \varepsilon_{macr}) p \frac{\partial x_i}{\partial t} + (1 - \varepsilon_{ext} - \varepsilon_{macr}) \left(\frac{\partial q_i}{\partial t} \right) = 0 \quad i = 1 \dots 3 \quad \varphi_i = \frac{K'_i p x_i}{1 + L_1 p x_1 + L_2 p x_2}$$

- **component 1 in inert carrier**

$$\mu = \frac{L}{v_f} \left[(\varepsilon_{ext} + \varepsilon_{macr}) + (1 - \varepsilon_{ext} - \varepsilon_{macr}) (K'_1 \rho_{crys} RT) \right]$$

- **component 2 in adsorbing carrier 2**

$$\mu_2 = \frac{L}{v_f} \left[(\varepsilon_{ext} + \varepsilon_{macr}) + (1 - \varepsilon_{ext} - \varepsilon_{macr}) \left(\frac{K'_2 \rho_{crys} RT}{(1 + L_2 p x_2)^2} \right) \right]$$

- **component 1 in adsorbing carrier 2**

$$\mu_1 = \frac{L}{v_f} \left[(\varepsilon_{ext} + \varepsilon_{macr}) + (1 - \varepsilon_{ext} - \varepsilon_{macr}) \left(\frac{K'_1 \rho_{crys} RT}{1 + L_2 p x_2} \right) \right]$$

Mass transfer

Method of moments

$$\frac{\sigma^2}{2\mu^2} = \frac{L}{v_f} \frac{(1 - \varepsilon_{ext} - \varepsilon_{macr})(RT\rho_c K'_i)}{\mu^2} \left(\frac{r_c^2}{15D_{micr}} + \frac{R_p^2 \left(1 + (RT\rho_c K'_i) \left(\frac{1 - \varepsilon_p}{\varepsilon_p} \right) \right)}{15D_{macr}} \right) + \frac{D_{ax}\varepsilon_{ext}}{v_f L}$$

Fitting of breakthrough curves or pulse responses

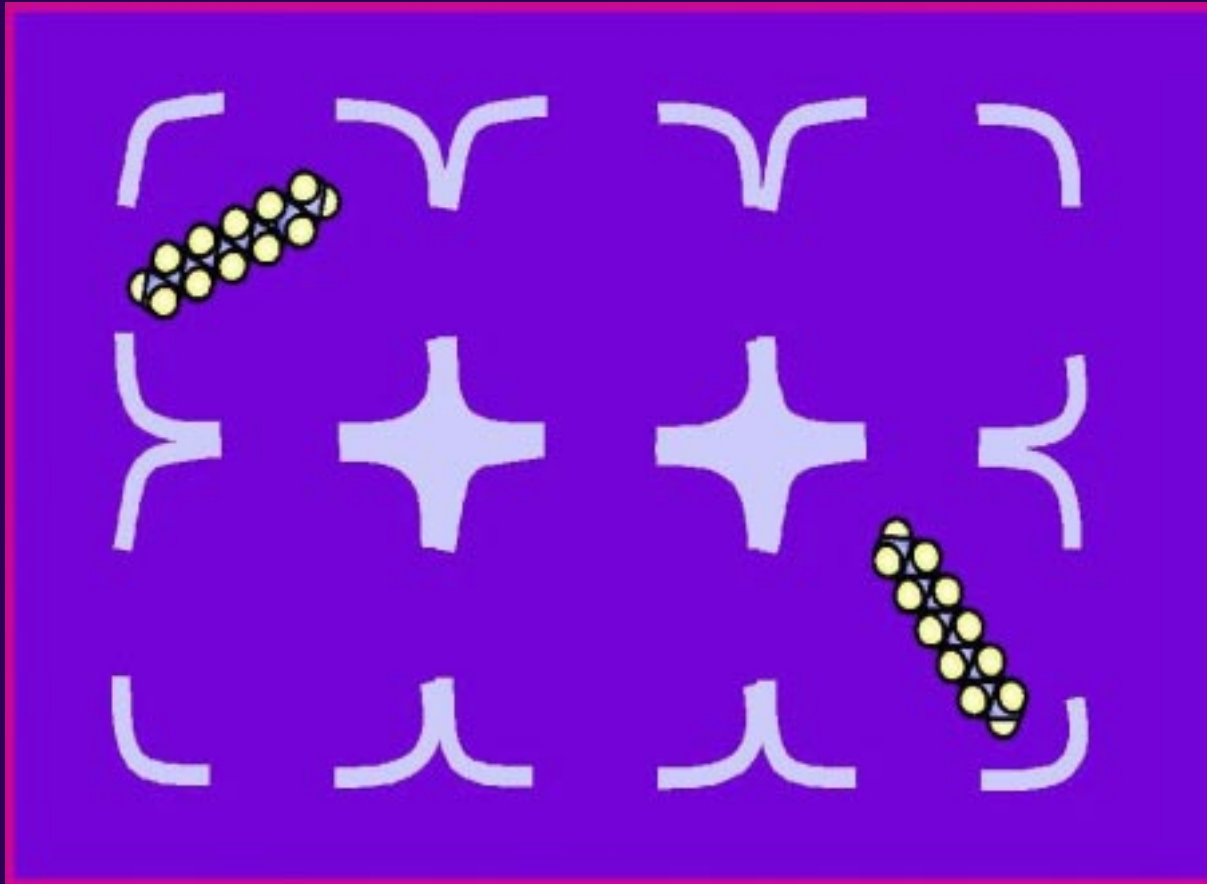
$$-D_{ax}p \frac{\partial^2 x_i}{\partial z^2} - v_f p \frac{\partial x_i}{\partial z} + (\varepsilon_{ext} + \varepsilon_{macr}) p \frac{\partial x_i}{\partial t} + (1 - \varepsilon_{ext} - \varepsilon_{macr}) \left(\frac{\partial q_i}{\partial t} \right) = 0$$

$$\frac{\partial q}{\partial t} = \frac{1}{R^2} \frac{\partial}{\partial R} \left(D_c R^2 \frac{\partial q}{\partial R} \right) \quad \bar{q} = \frac{3}{R_c^3} \int_0^R q R^2 dR$$

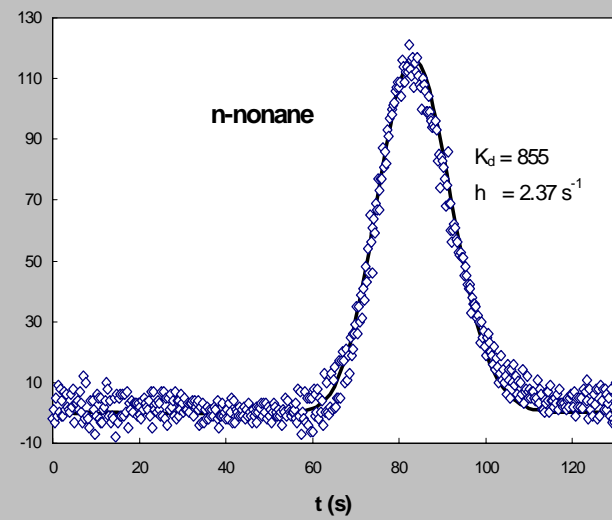
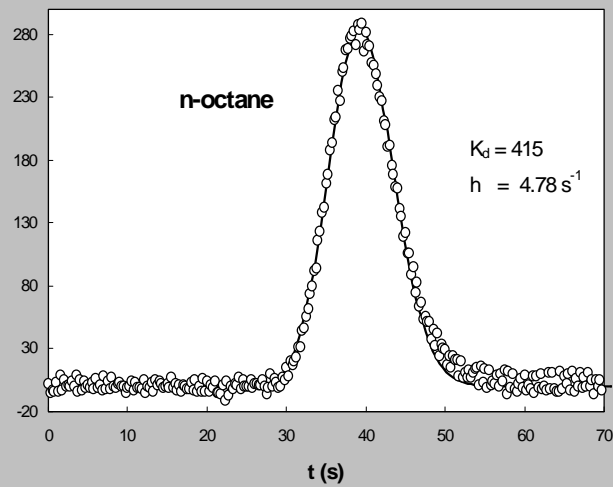
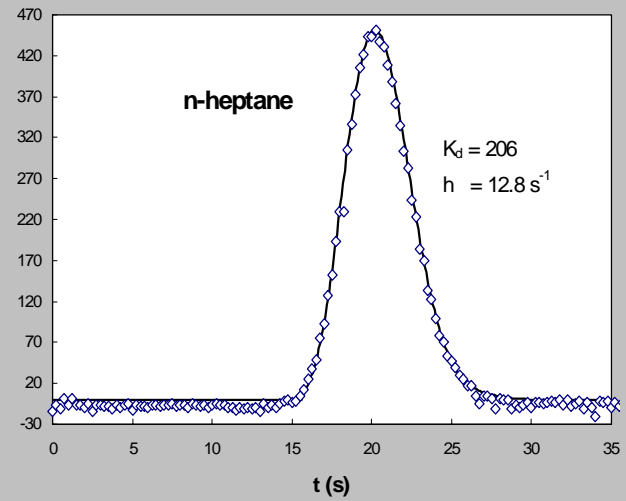
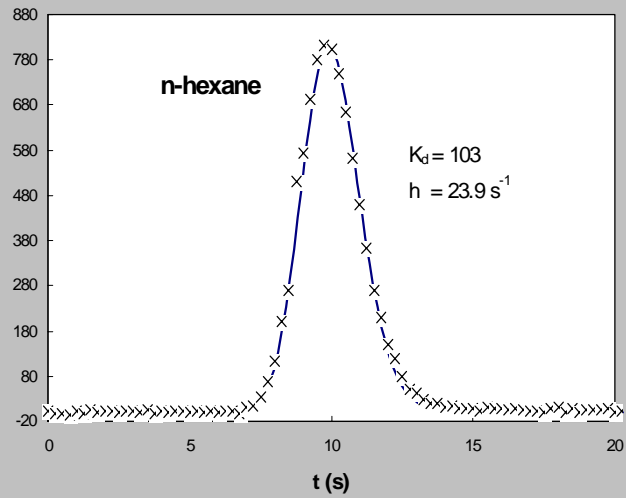
Chromatography: merits

- **Rapid measurement**
- **Broad range of components**
- **Broad range of operating conditions**
- **Simultaneous determination adsorption & diffusion**

Adsorption at low coverage



No interactions between adsorbed molecules



Gas phase diffusion

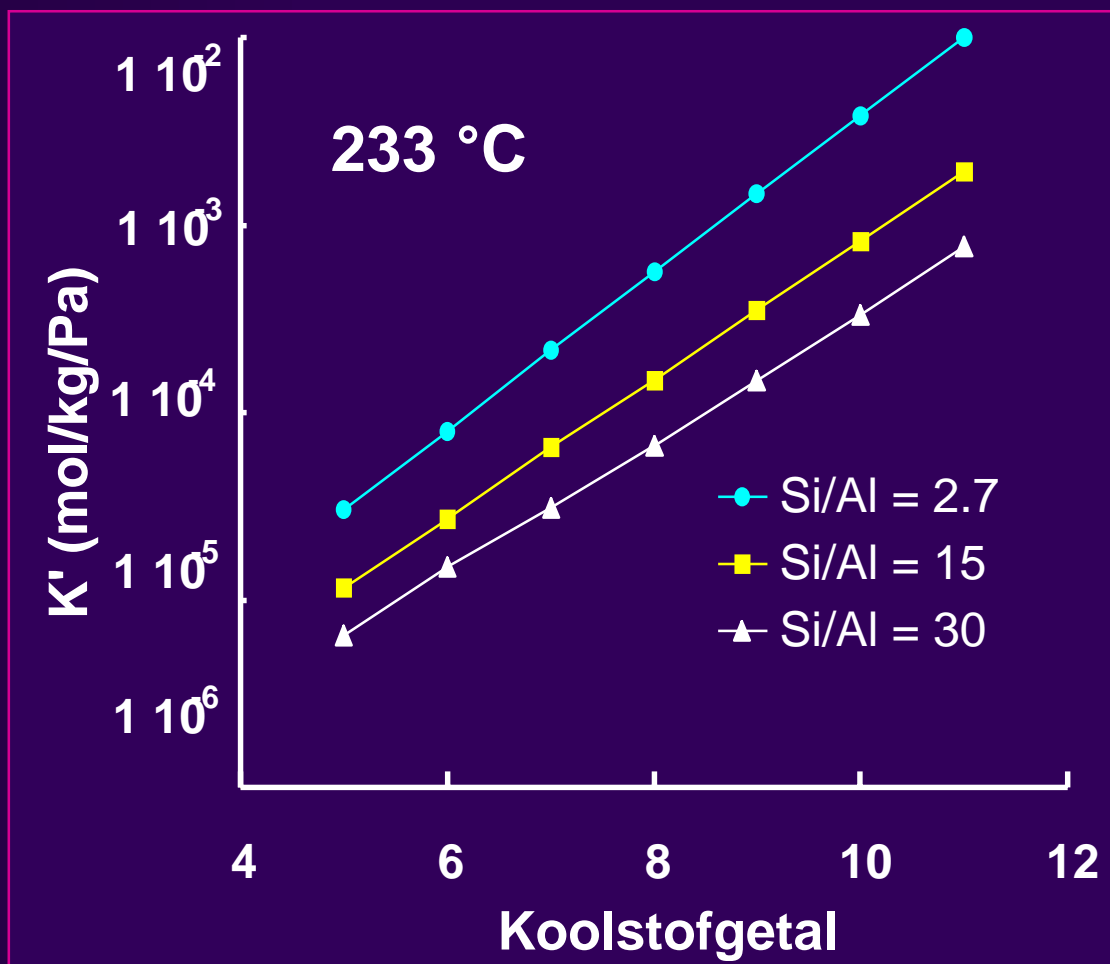
Macropore diffusion model:

$$D_{\text{macr}} \cong \frac{D_{\text{mol}} \cdot \varepsilon}{\tau} \quad \begin{array}{l} \text{pellet porosity} = 0.3 \\ \text{tortuosity factor} = 3 \end{array} \quad \Rightarrow D_{\text{macr}} = D_{\text{mol}}/10$$

sorbate	D_{mol} (m^2/s)	D_{macr} (m^2/s)
n-hexane	$5.1 \cdot 10^{-5}$	$3.8 \cdot 10^{-6}$
n-heptane	$4.7 \cdot 10^{-5}$	$4.8 \cdot 10^{-6}$
n-octane	$4.4 \cdot 10^{-5}$	$4.8 \cdot 10^{-6}$
n-nonane	$4.1 \cdot 10^{-5}$	$6.4 \cdot 10^{-6}$
n-decane	$3.8 \cdot 10^{-5}$	$2.4 \cdot 10^{-6}$
n-undecane	$3.6 \cdot 10^{-5}$	$4.8 \cdot 10^{-6}$
n-dodecane	$3.4 \cdot 10^{-5}$	$6.2 \cdot 10^{-6}$

⇒ Mass transfer is dominated by macropore diffusion

Influence Si/Al - Y zeolites

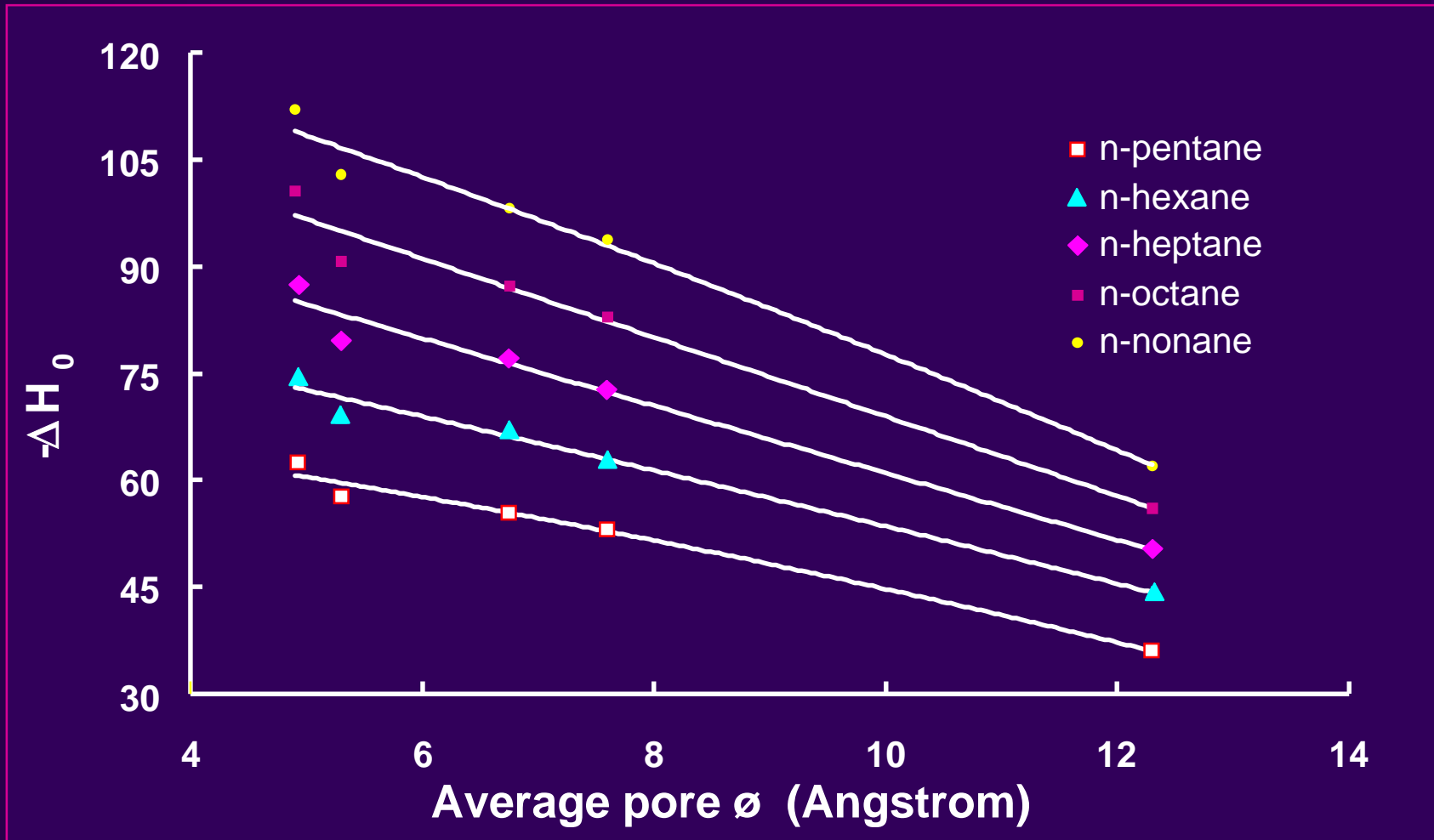


$$K' = A \cdot \exp(B \cdot CM)$$

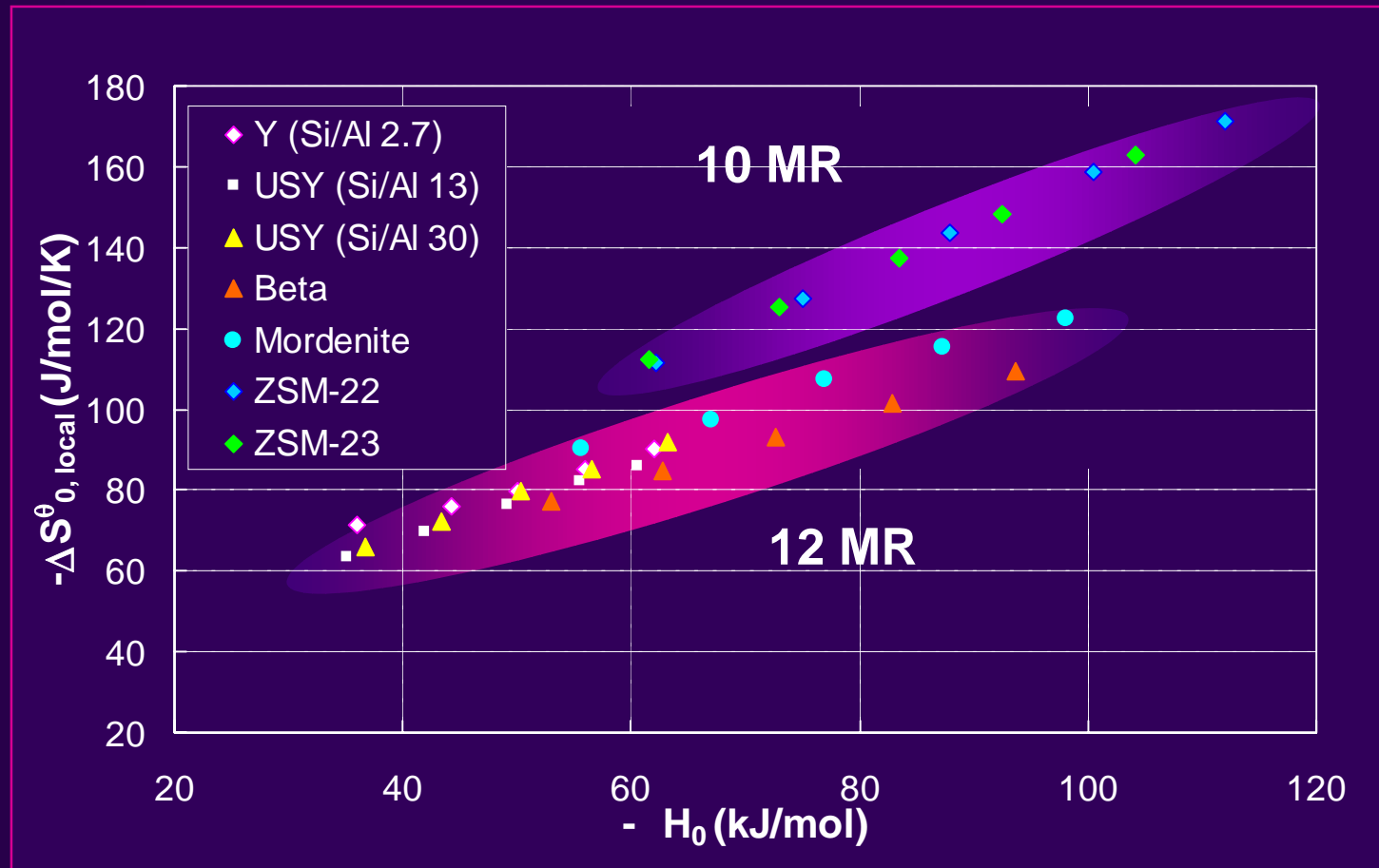
Si/Al	A	B
2.7	$2.41 \cdot 10^{-7}$	0.97
15	$1.64 \cdot 10^{-7}$	0.85
30	$1.25 \cdot 10^{-7}$	0.79

⇒ Exponential factor B decreases with Al content

Influence pore diameter



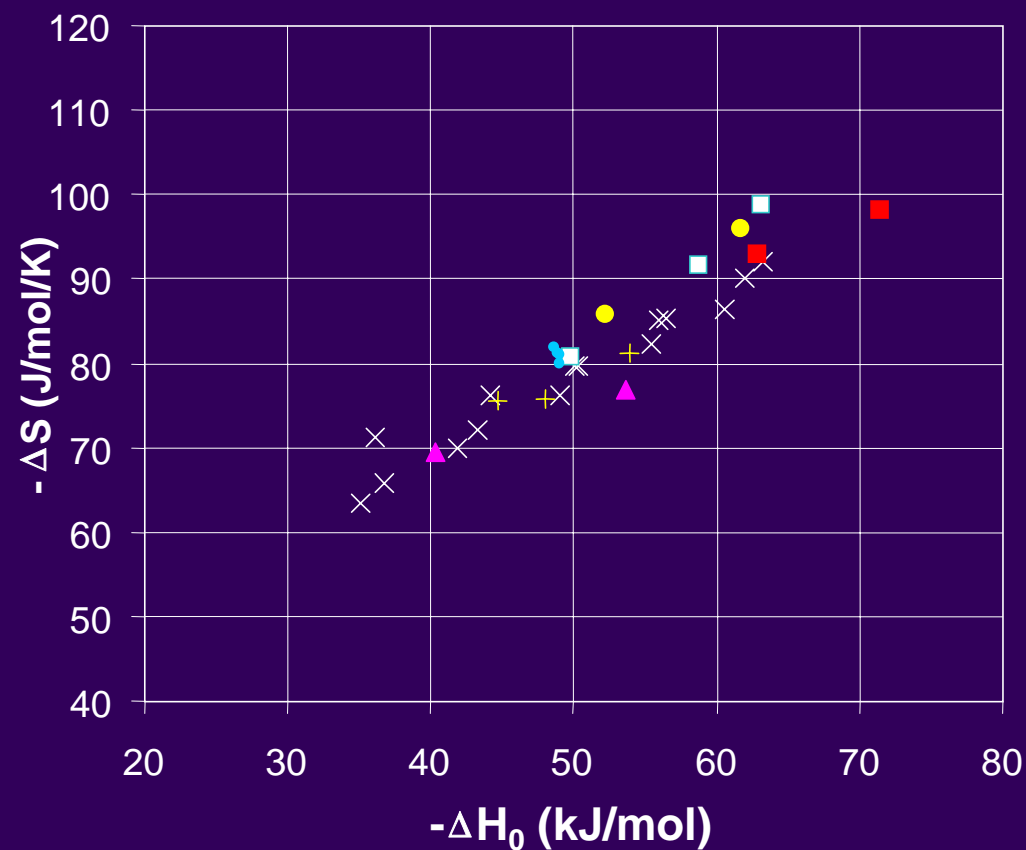
Compensation – effect : influence pore size



⇒ Compensation between adsorption entropy and enthalpy

⇒ All 12 MR and 10 MR zeolites same characteristic curve

Compensation – effect : influence molecule type



× Alkanes Y - USY

■ Aromatics NaY (Si/Al 2.7)

■ Aromatics H-USY (Si/Al 30)

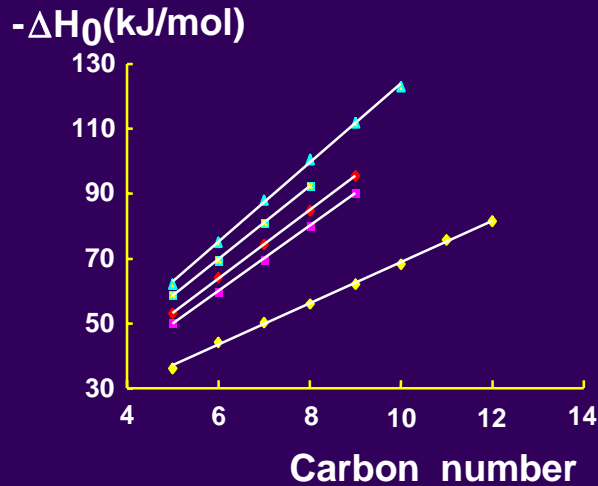
▲ Cyclo-alkanes NaY (Si/Al 2.7)

● Butene isomers NaY (Si/Al 3.8)

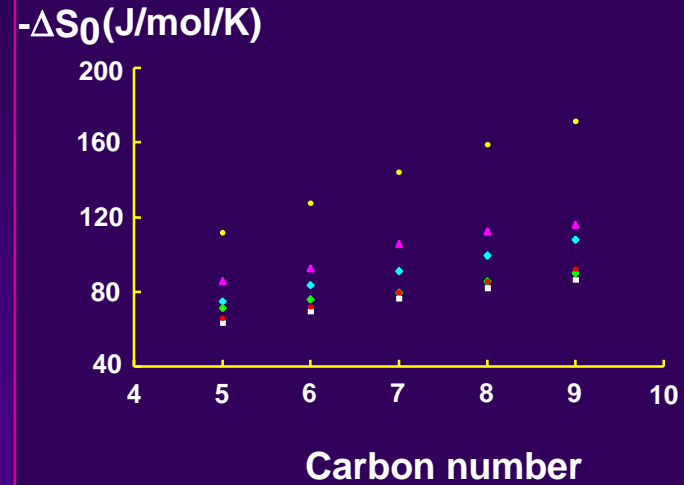
● C6-C7 alkenes NaY (Si/Al 2.7)

+ C6-C8 alkenes H-USY (Si/Al 30)

General correlation for the Henry constants



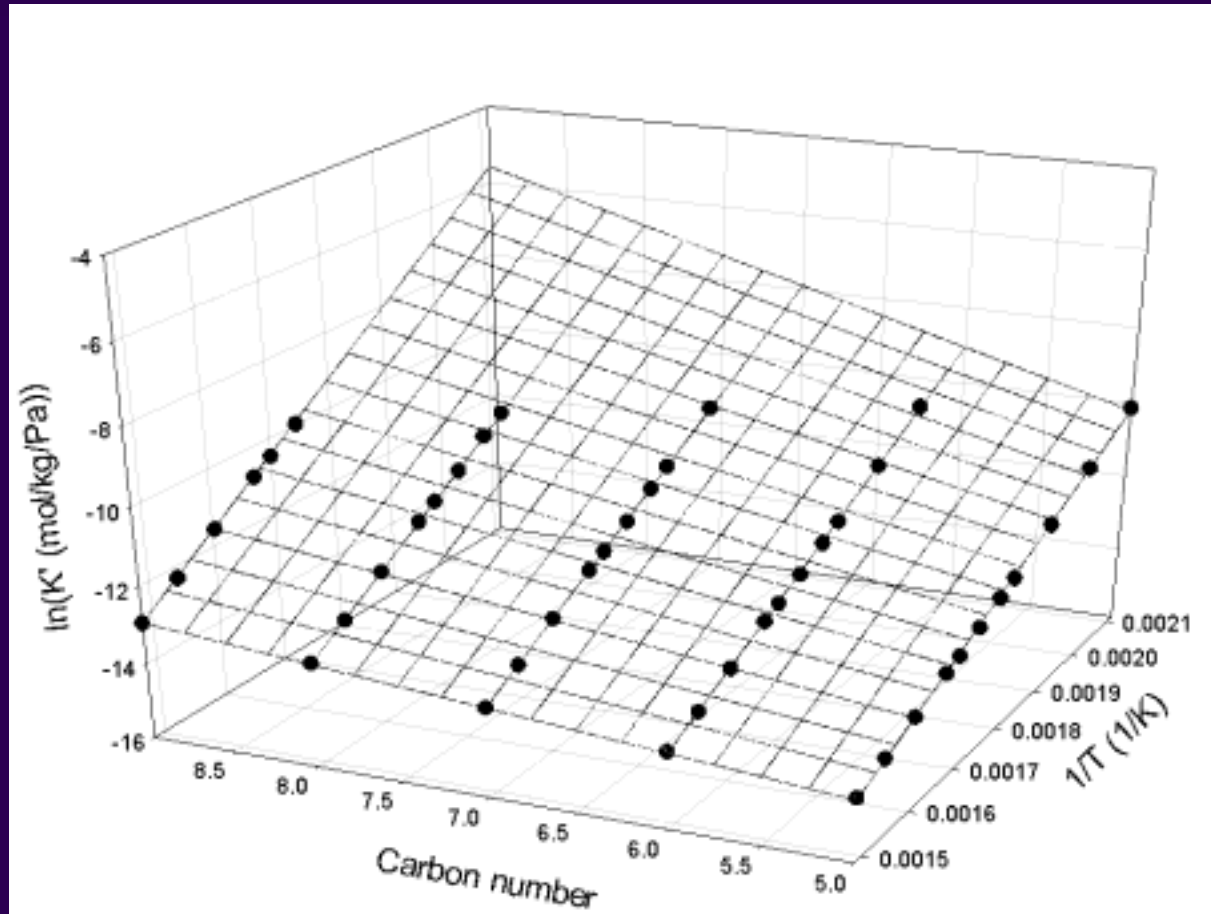
$$-\Delta H_0 = \alpha CN + \beta$$



$$-\Delta S_{0,\text{local}}^\theta = \gamma CN + \delta$$

$$\ln K' = \left(\frac{\alpha}{RT} - \frac{\gamma}{R} \right) CN + \left[\ln \left(\frac{n_T}{2p^\theta} \right) + \frac{\beta}{RT} - \frac{\delta}{R} \right]$$

3D fitting of experimental data



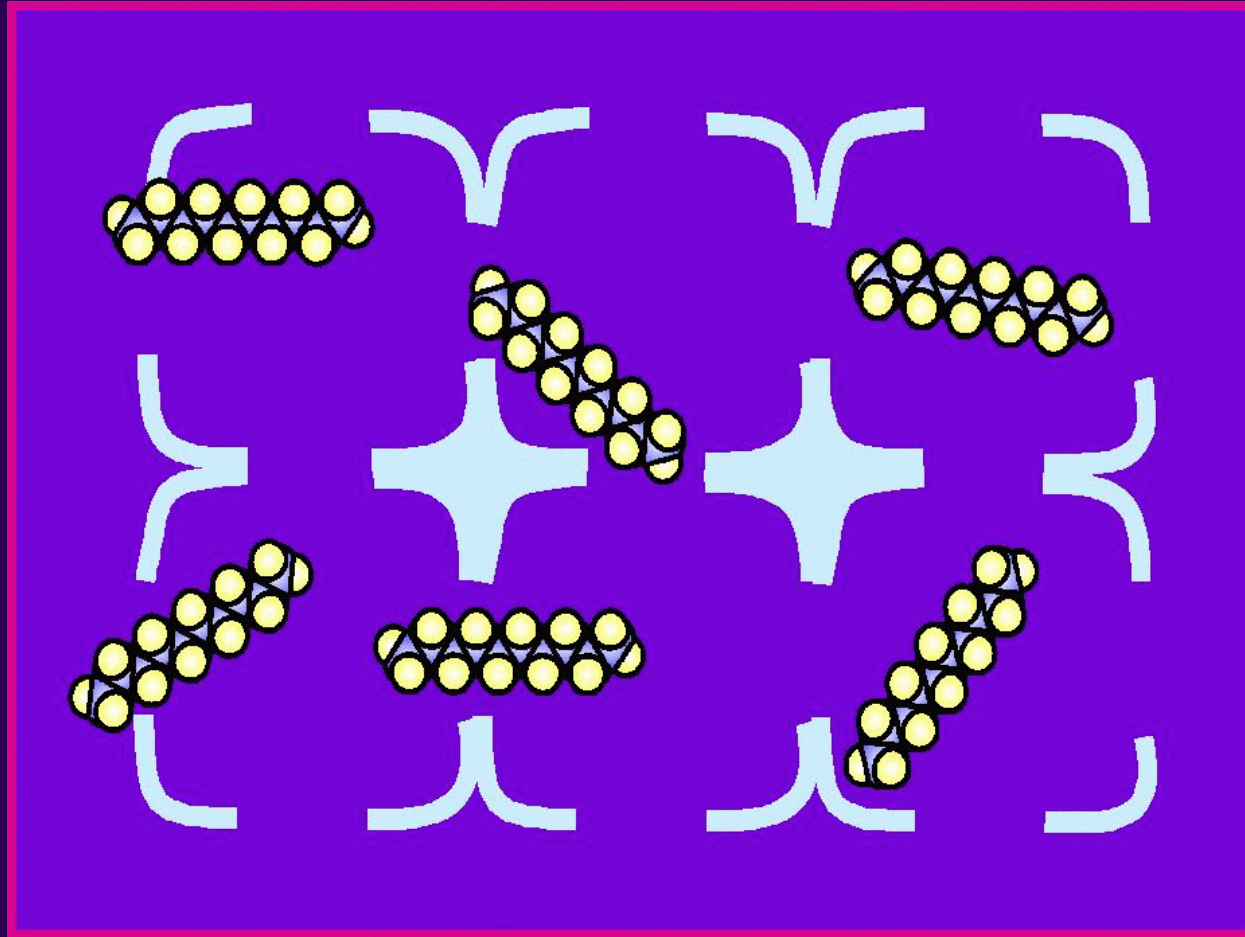
$$\alpha = 11.0 \text{ kJ/mol}$$

$$\beta = 1.3 \text{ kJ/mol}$$

$$\gamma = 13.3 \text{ J/mol/K}$$

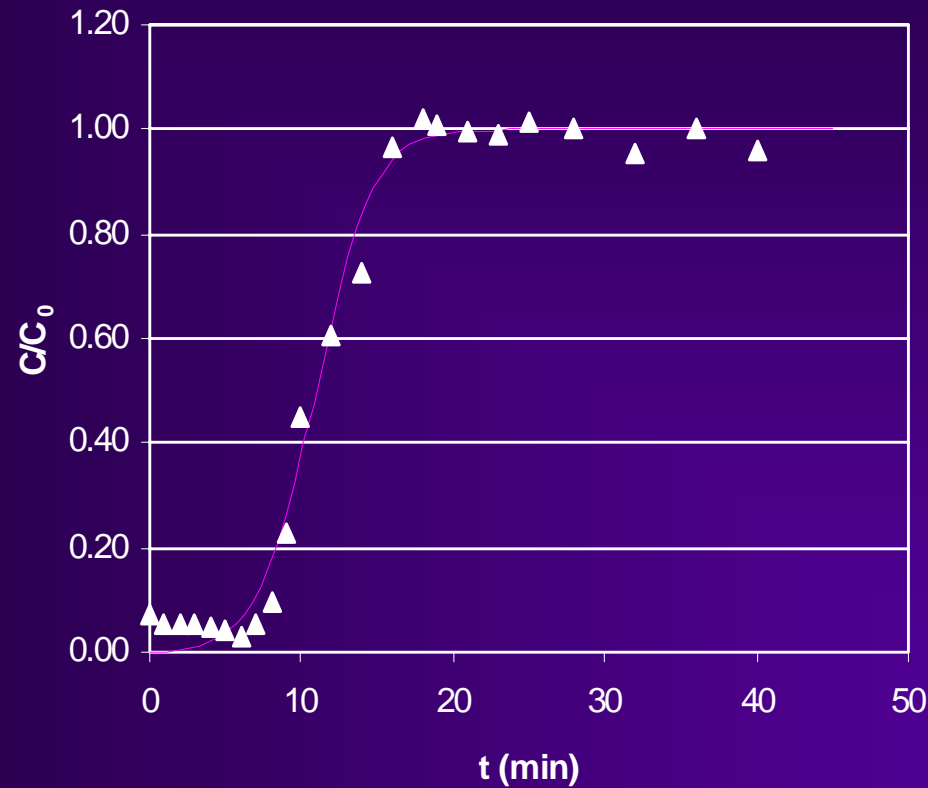
$$\delta = 14.8 \text{ J/mol/K}$$

Adsorption at intermediate coverage



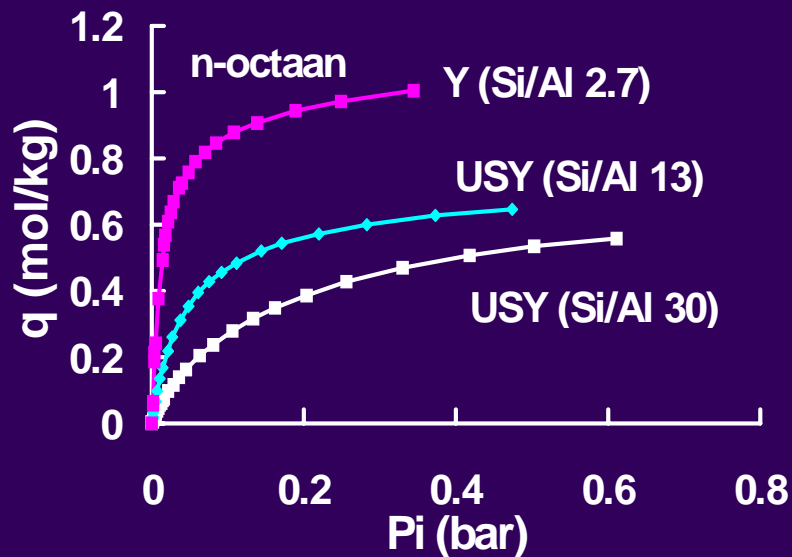
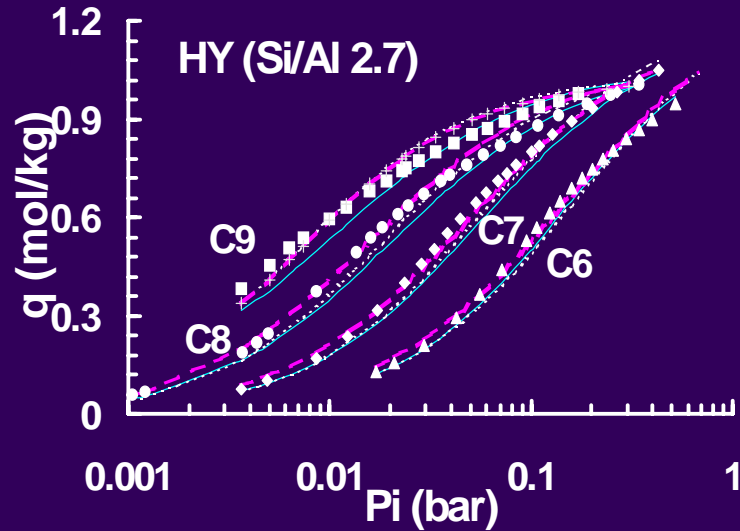
interaction between adsorbed molecules ?

Breakthrough curves



$$-D_{ax}p \frac{\partial^2 x_i}{\partial z^2} - v_f p \frac{\partial x_i}{\partial z} + (\epsilon_{ext} + \epsilon_{macr}) p \frac{\partial x_i}{\partial t} + (1 - \epsilon_{ext} - \epsilon_{macr}) \left(\frac{\partial q_i}{\partial t} \right) = 0 \quad \frac{\partial \bar{q}}{\partial t} = k(q^* - q) = hK(c - c^*)$$

Isotherm fitting



- Langmuir:

$$q(p, T) = \frac{Kp}{1 + Lp}$$

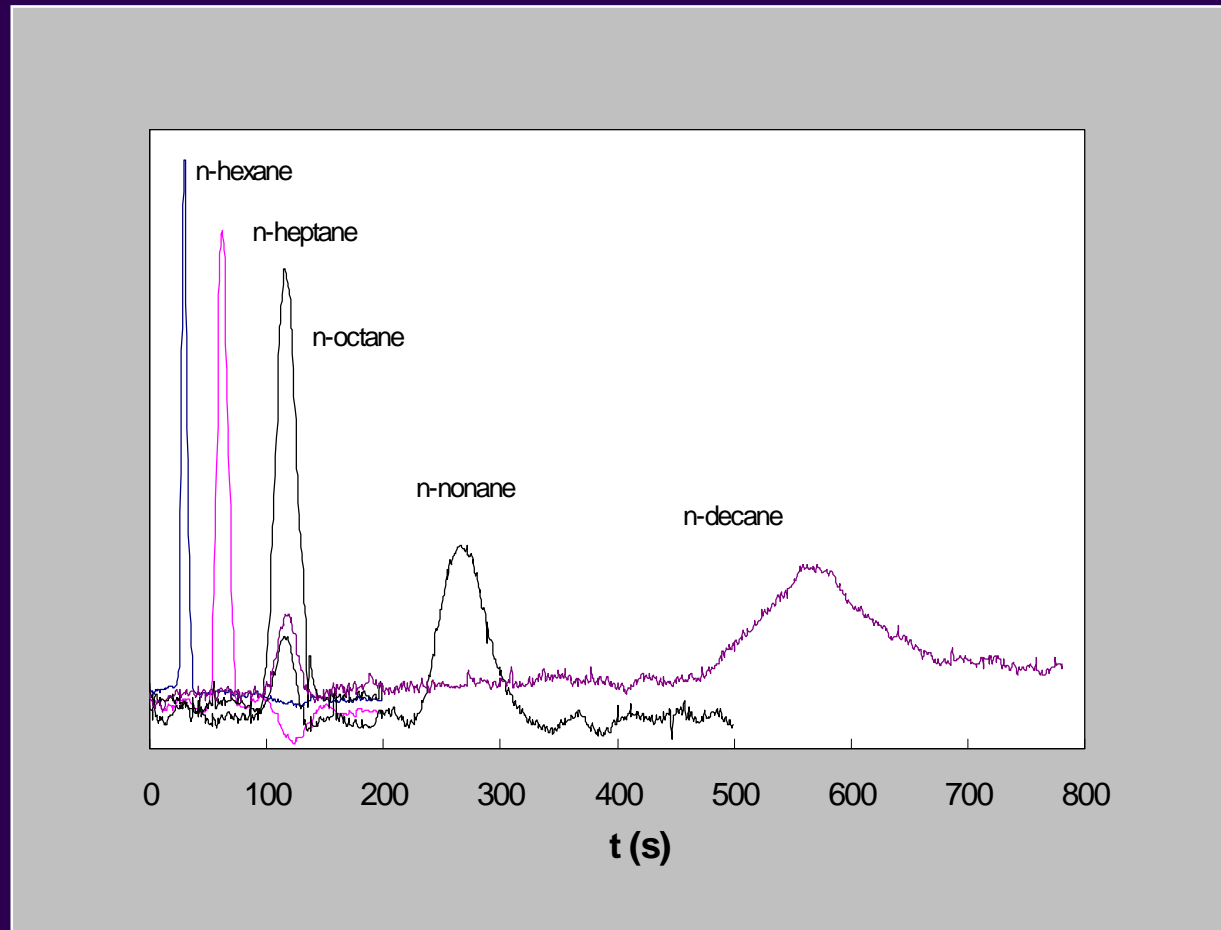
- Langmuir-Freundlich:

$$q(p, T) = \frac{Kp^B}{1 + Lp^B}$$

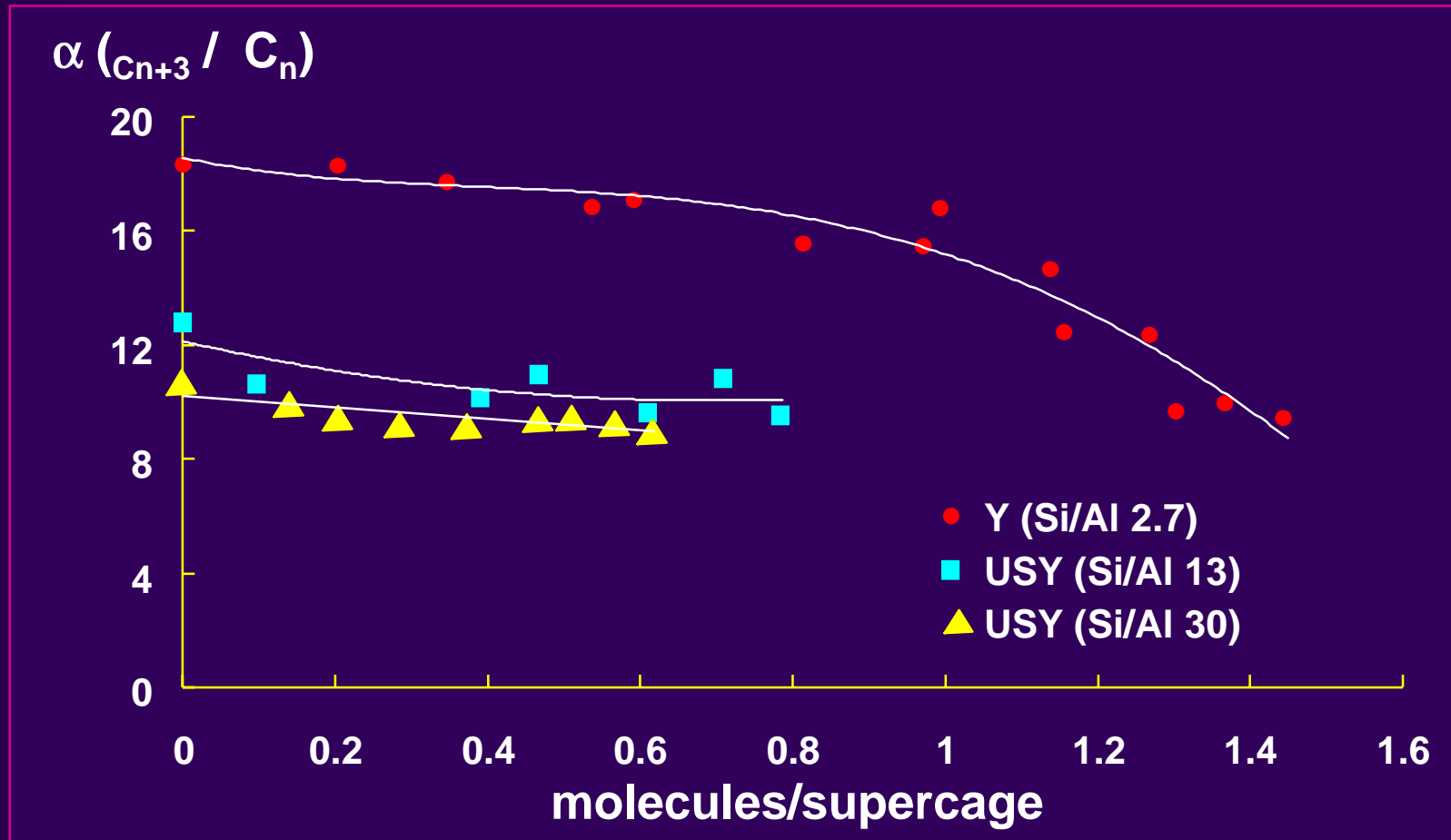
- Langmuir + Interaction:

$$q(p, T) = \frac{Kpe^{\frac{q}{q_s}}}{1 + Lpe^{\frac{q}{q_s}}}$$

Perturbation chromatography

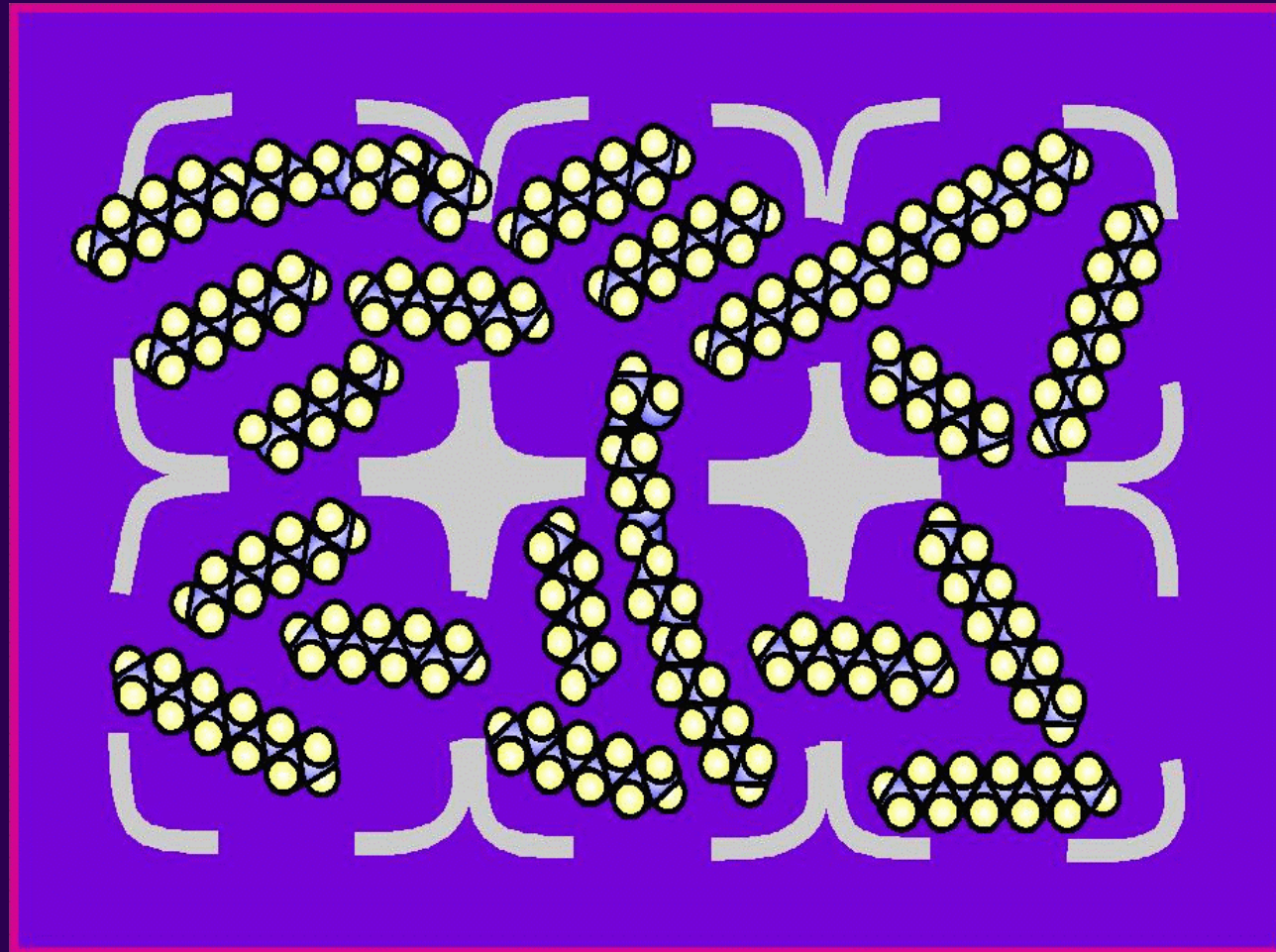


Influence zeolite loading on competition

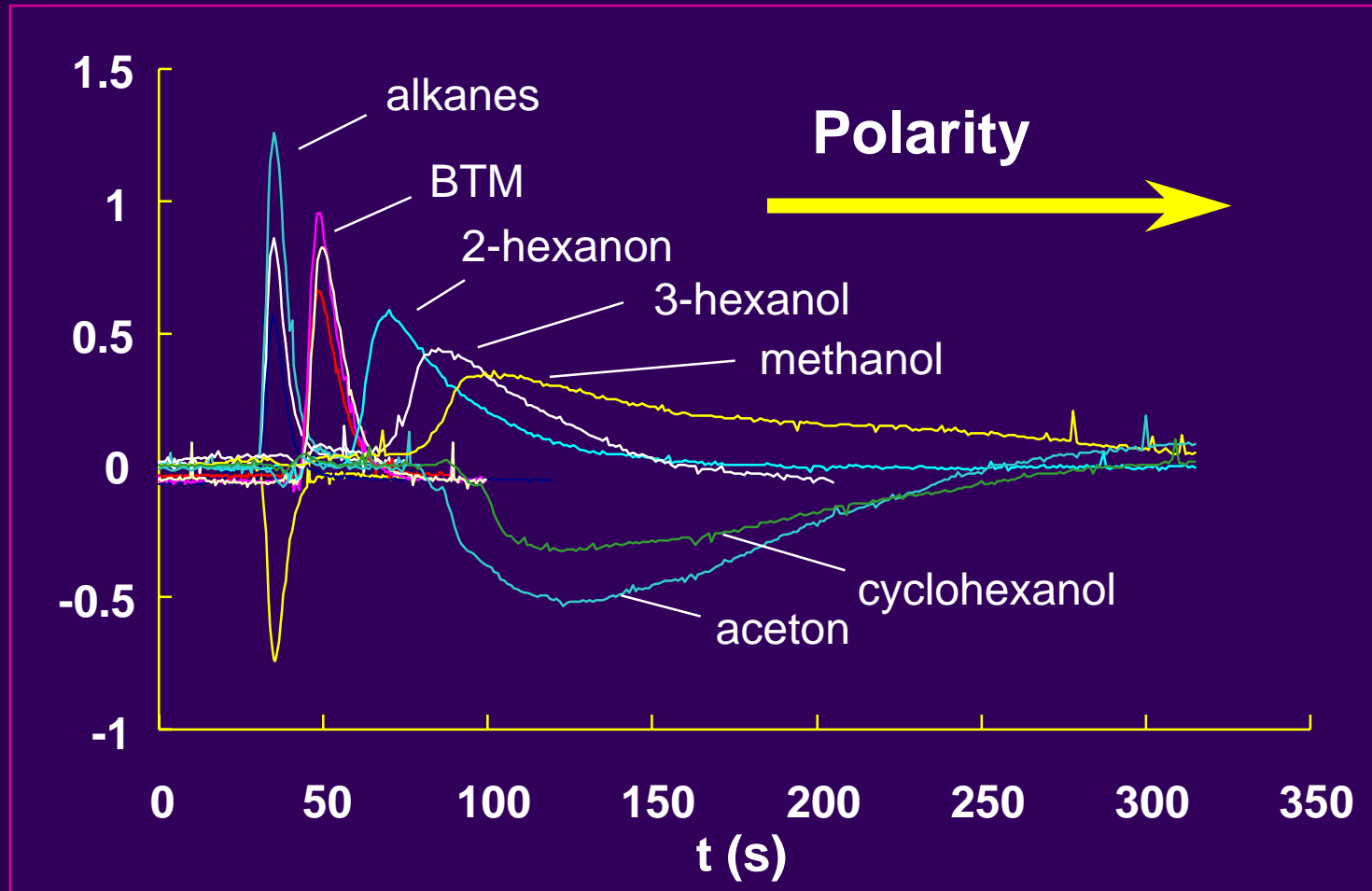


⇒ More than 1 molecule supercage: separation factor decreases strongly

Adsorption at complete pore filling



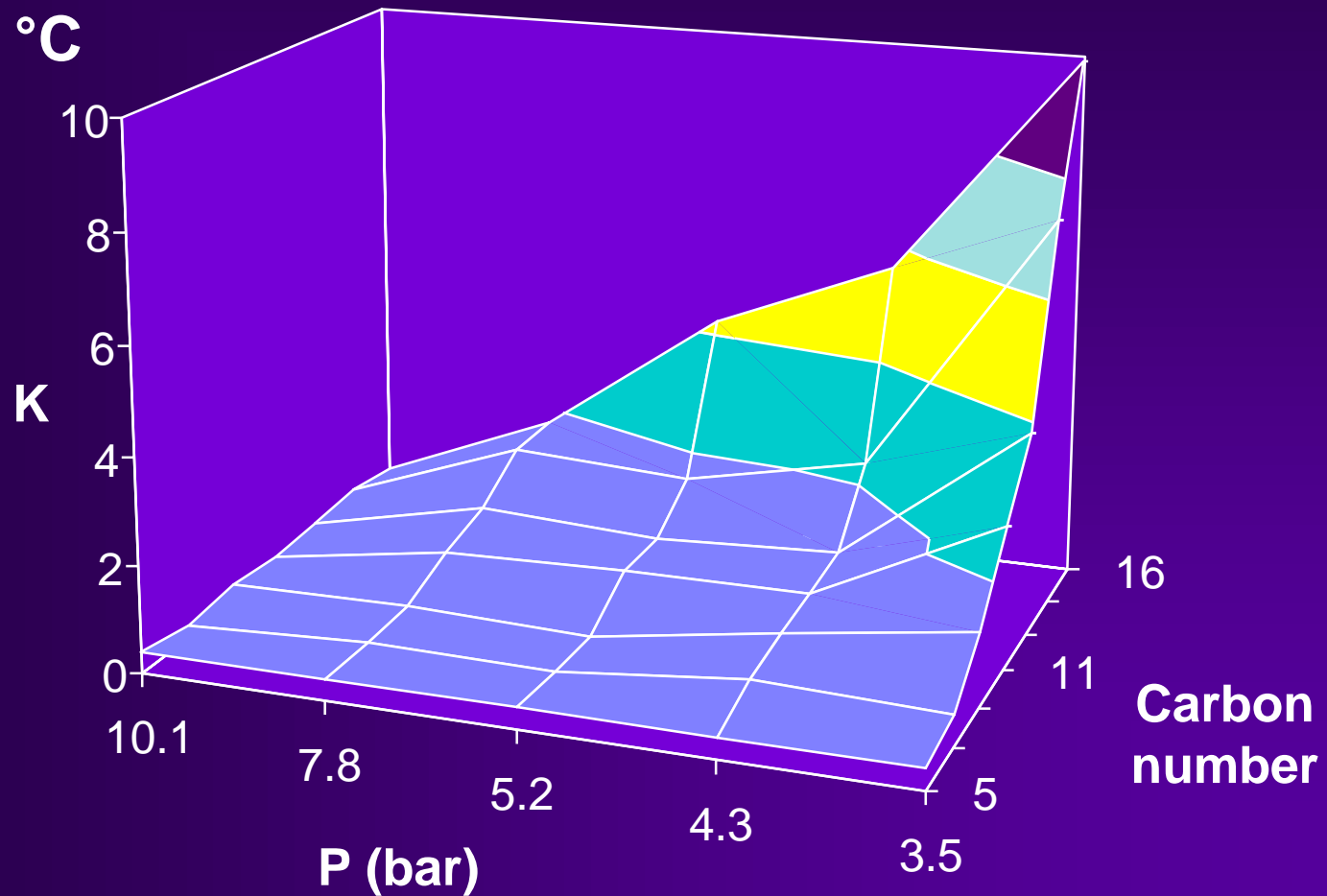
Zeolite Y (Si/Al 30), mobile phase octane



⇒ no pronounced difference between short and long alkanes

Influence fluidum density on competition

USY (Si/Al 30)
210 °C



Liquid phase adsorption

Statistical isotherm

$$q_i = \frac{\overline{N}_i}{M} = \frac{K'_1 p_1 + \sum_j \sum_i \frac{[(K'_1 p_1)^i (K'_2 p_2)^j (1 - i\beta_1/v - j\beta_2/v)^{i+j}]}{(i-1)!j!}}{1 + K'_1 p_1 + K'_2 p_2 + \sum_j \sum_i \frac{[(K'_1 p_1)^i (K'_2 p_2)^j (1 - i\beta_1/v - j\beta_2/v)^{i+j}]}{(i)!j!}}$$

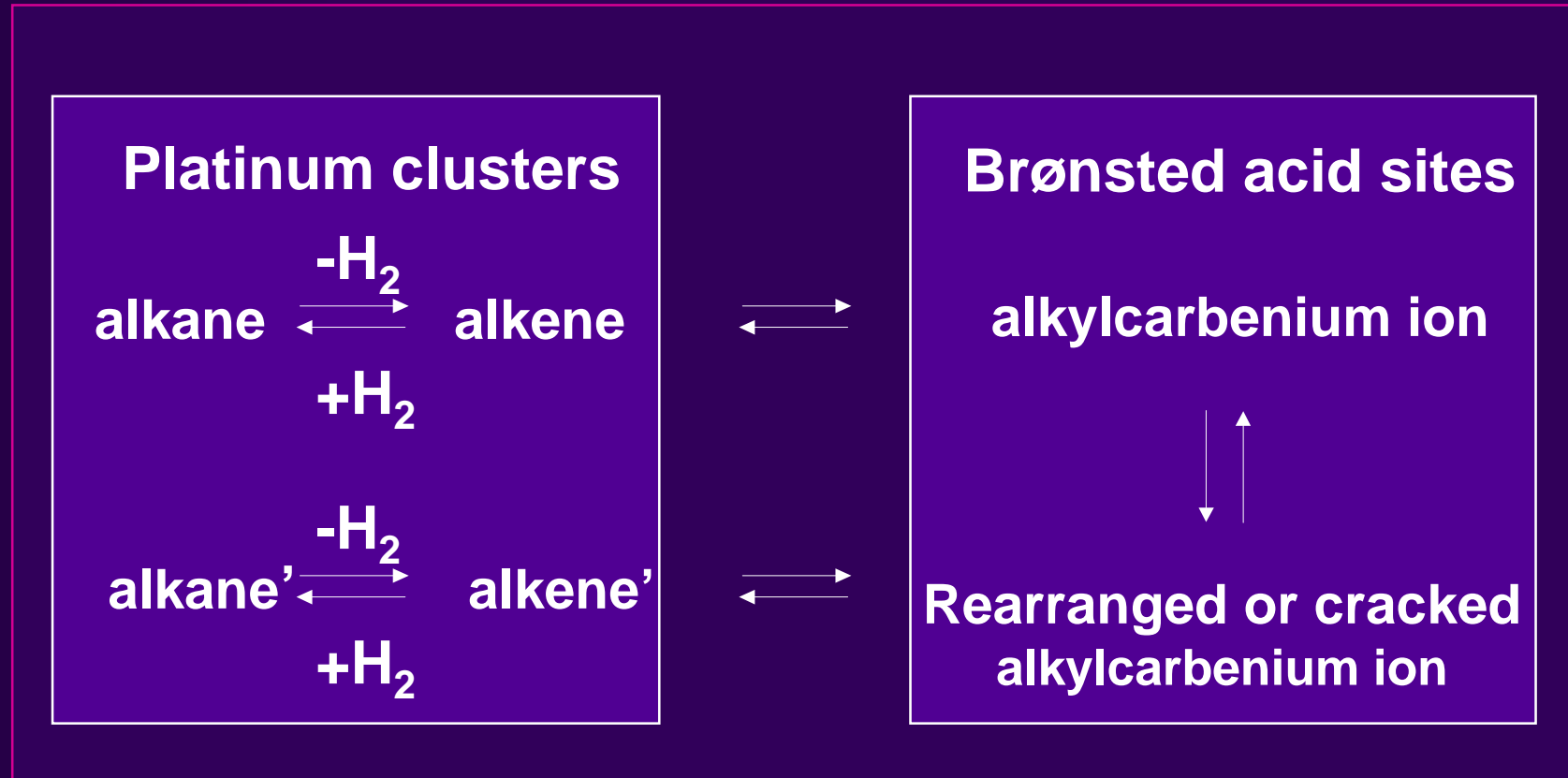
- Consider each supercage as independent system
- β_i : volume component i
- v : volume supercage

Partition coefficient model

$$q_i = K_i c_i$$

$$K_i = \overline{q}_s V_m$$

Catalysis



Decoupling adsorption and reaction properties

Rate equations

Adsorption

Vapor phase

$$q_i(p, T) = \frac{K'_i p_j e^{w_i \frac{q_T}{q_s}}}{1 + \sum_j L_j p_j e^{w_j \frac{q_T}{q_s}}}$$

$$-\Delta H_{0,i} = \alpha CN + \beta$$

$$-\Delta S_{0,local}^\theta = \gamma CN + \delta$$

$$\ln(K'_i) = \frac{-\Delta H_i}{RT_m} + \left[\frac{\Delta S_{0,local,i}^\theta}{R} + \ln\left(\frac{n_T}{2p^\theta}\right) \right]$$

Liquid phase

$$q_i = K_i c_i$$

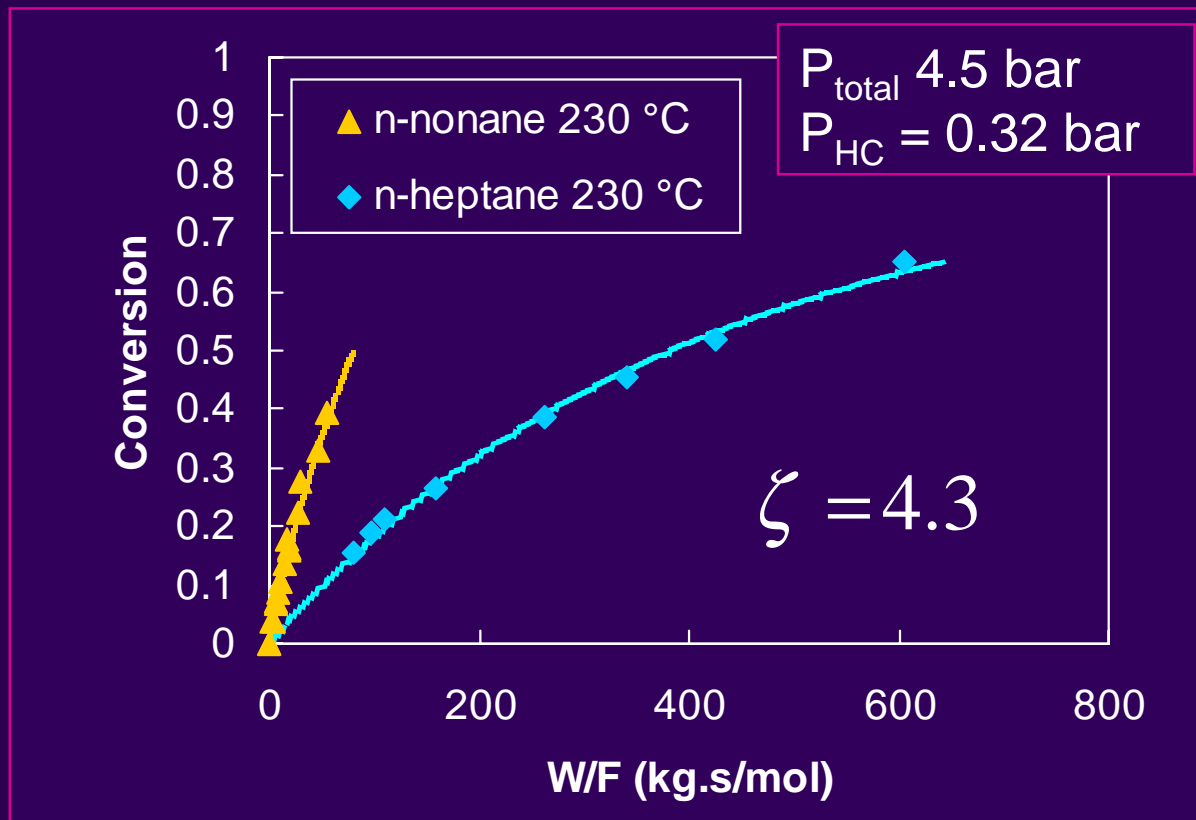
$$K_i = \bar{q}_s V_m$$

Kinetics

$$r_{nC4} = 2f_3 k_c q_{MB} + \left(f_{2,2} k_{B1} + \frac{1}{2} f_{2,4} k_{B2} + 2f_{3,4} k_c \right) q_{DB} + f_{2,2,3} k_{B1} q_{TB}$$

...

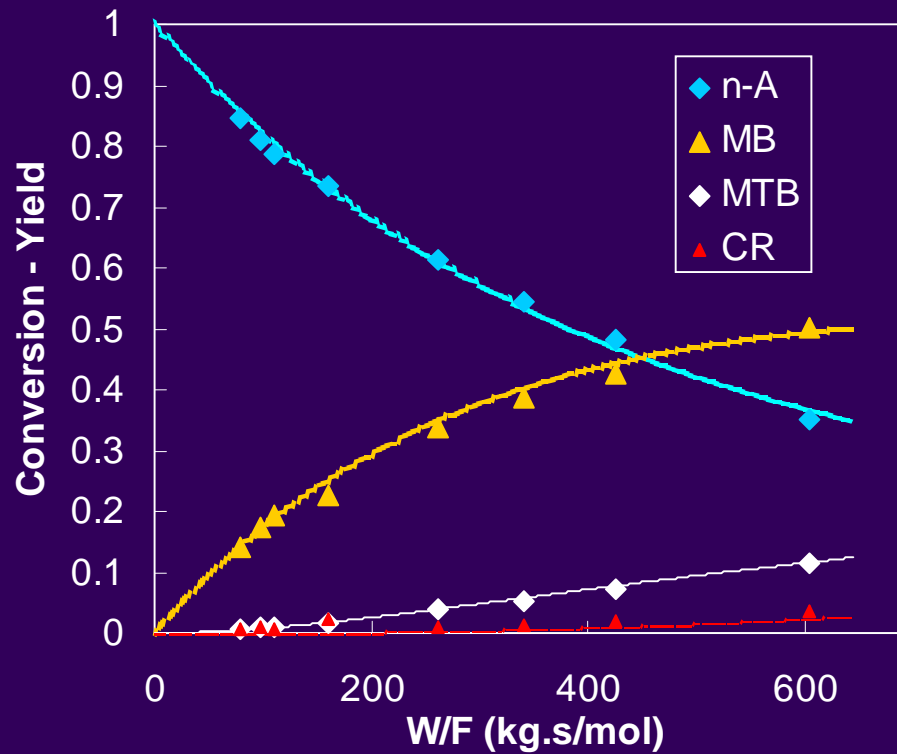
Competition effects in vapor phase



$$\zeta = \frac{r_{\text{nC9}}^0}{r_{\text{nC7}}^0}$$

Molecular competition factor

Lumped reaction model

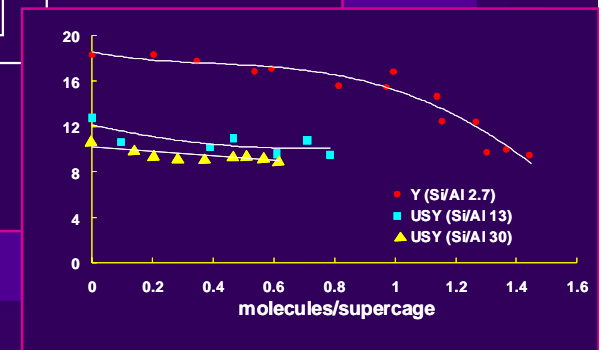
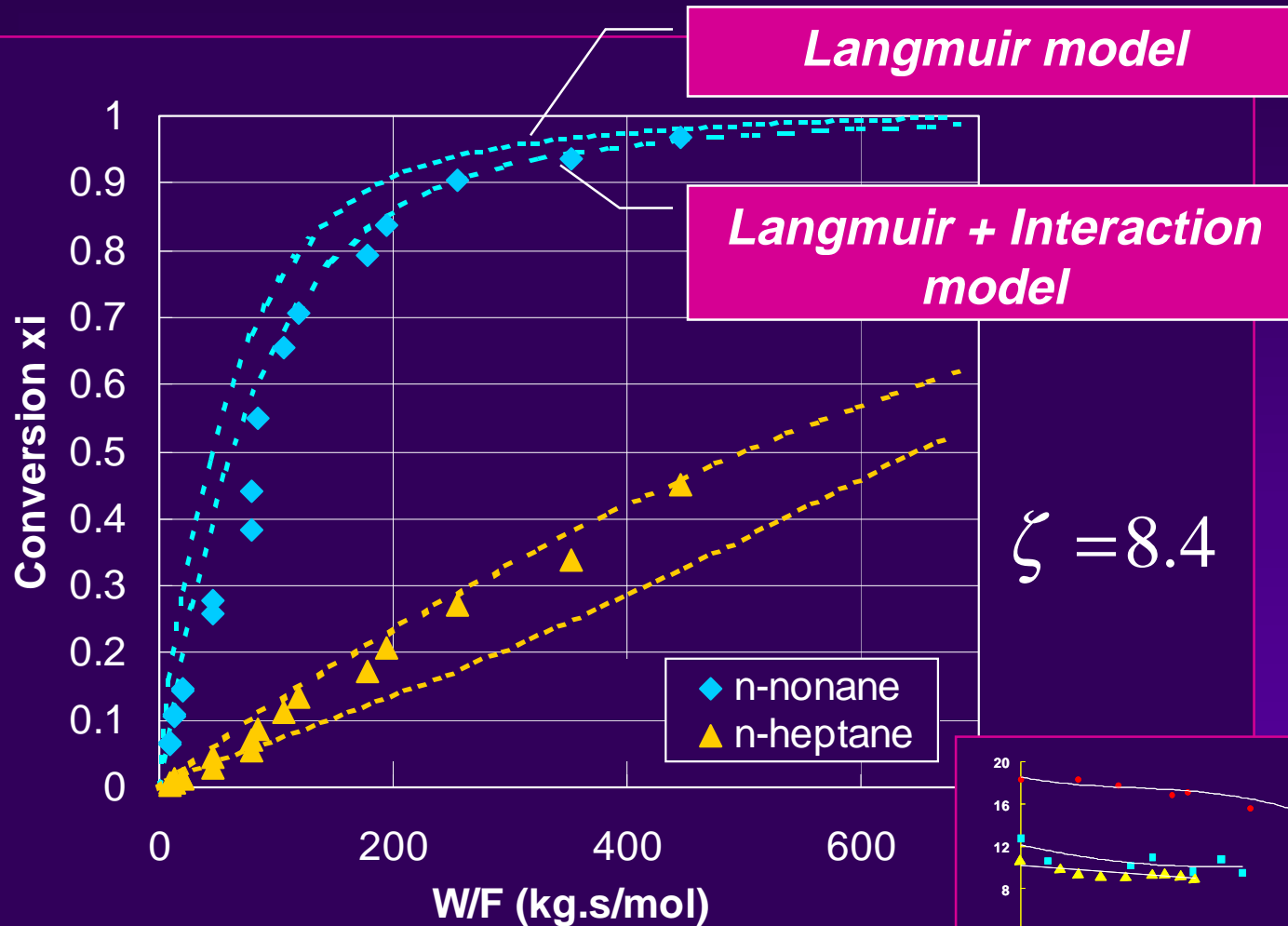


* Froment, G.F., Catalysis Today, 1987, 1, 455

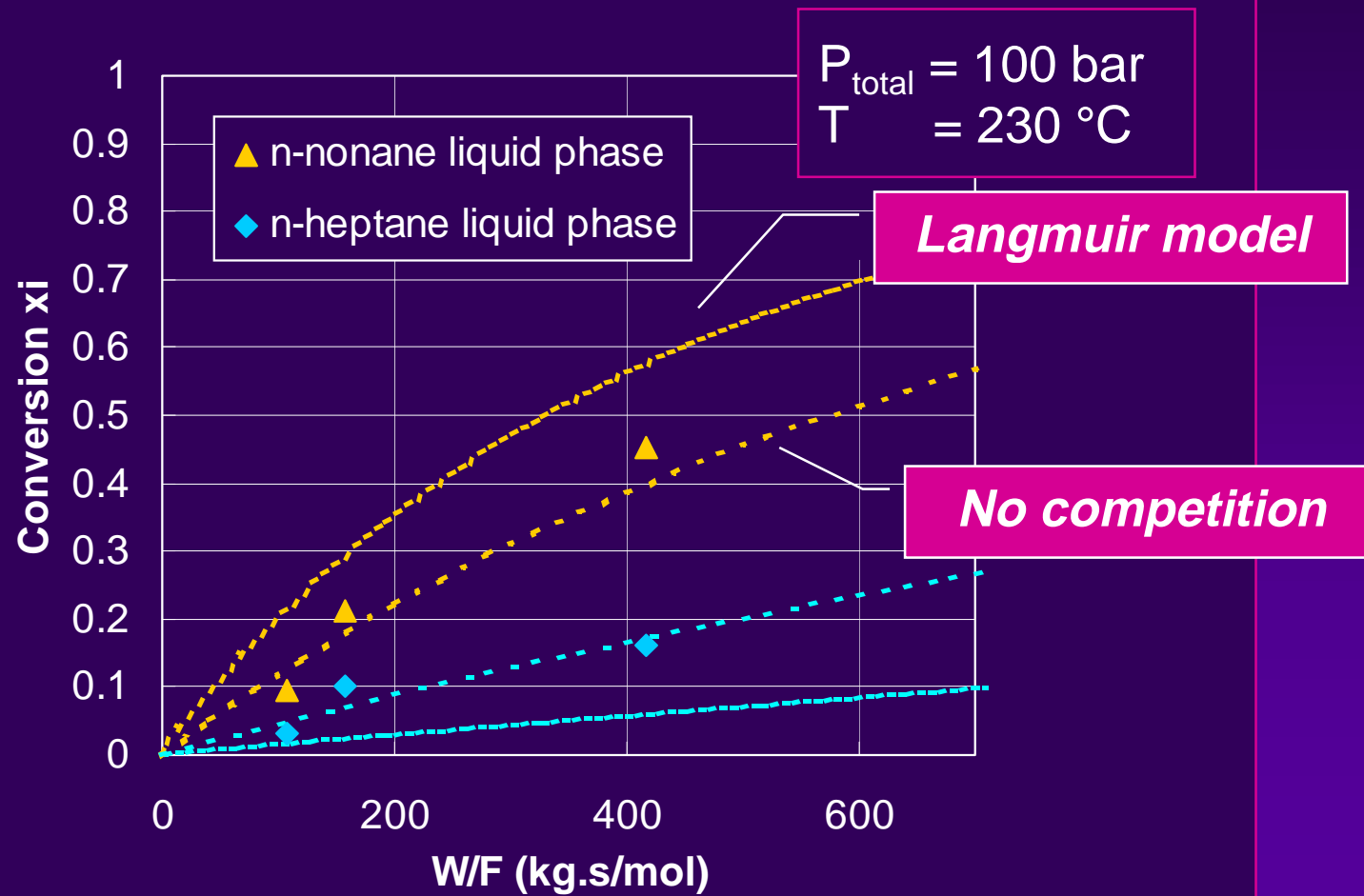
Adsorption & kinetic parameters

	K' (mol/kg/bar)	L (1/bar)	q_s (mol/kg)	$k_{intr} * K_{DH}$ (1/bar/s)
nC7	6.91	9.8	0.7	0.023
nC9	37.4	60.0	0.62	0.063
Ratio	5.4			2.74

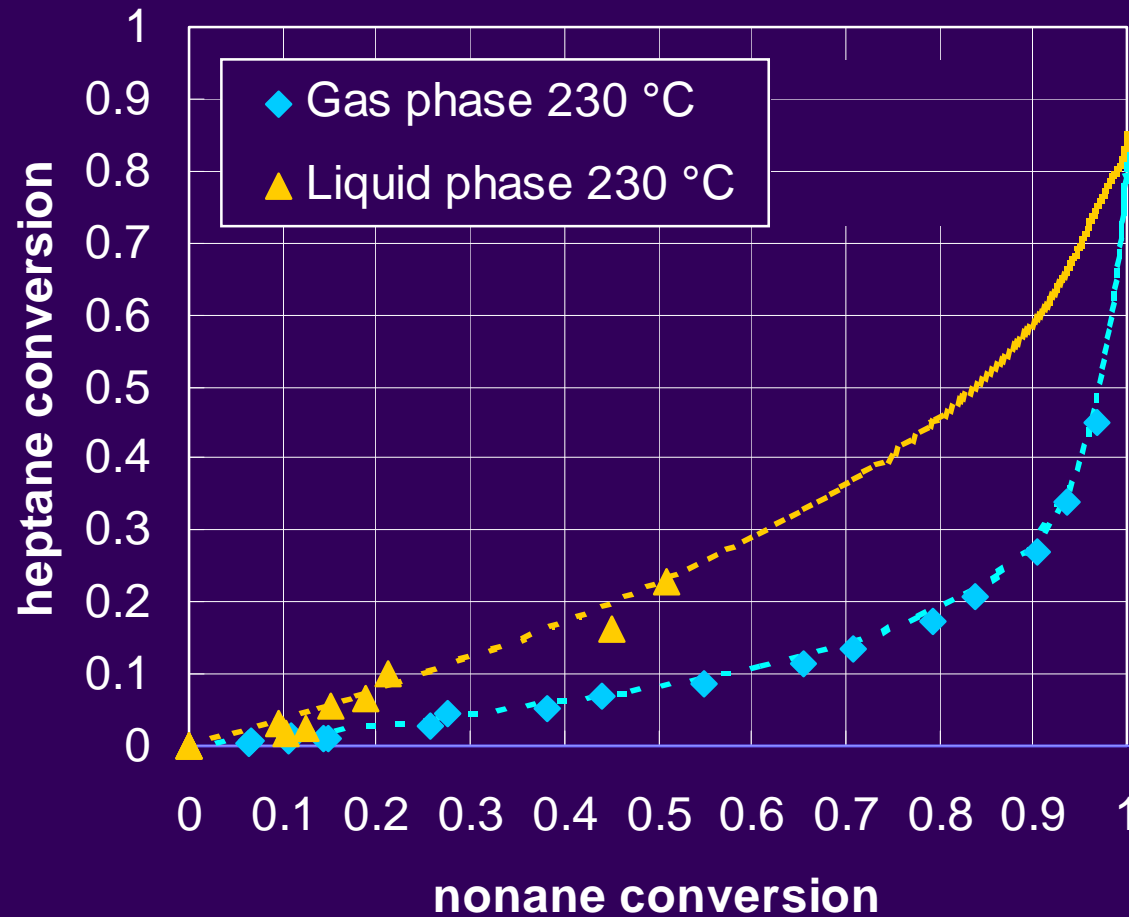
Competition in vapor phase



Competition in liquid phase



Vapor versus Liquid



Pure components

$$\zeta = 4.3$$

Vapor, binary

$$\zeta = 8.4$$

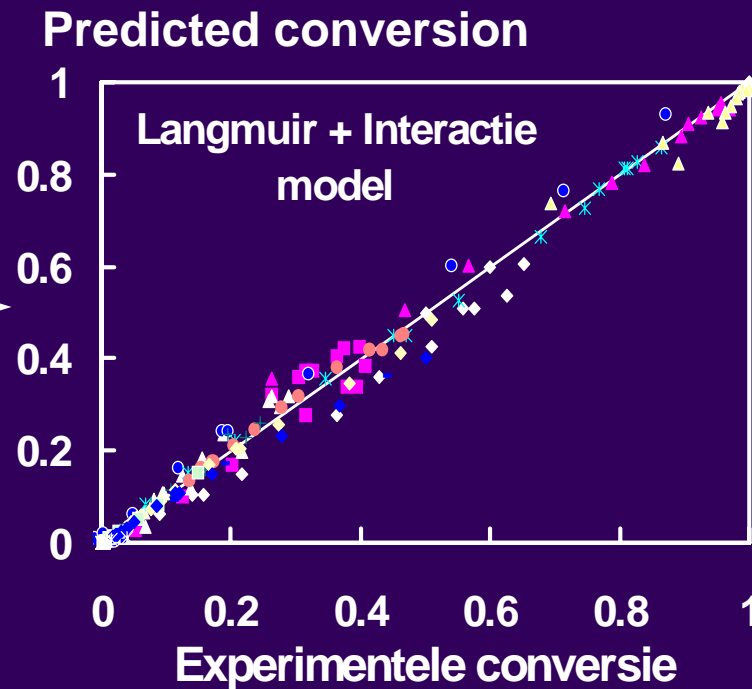
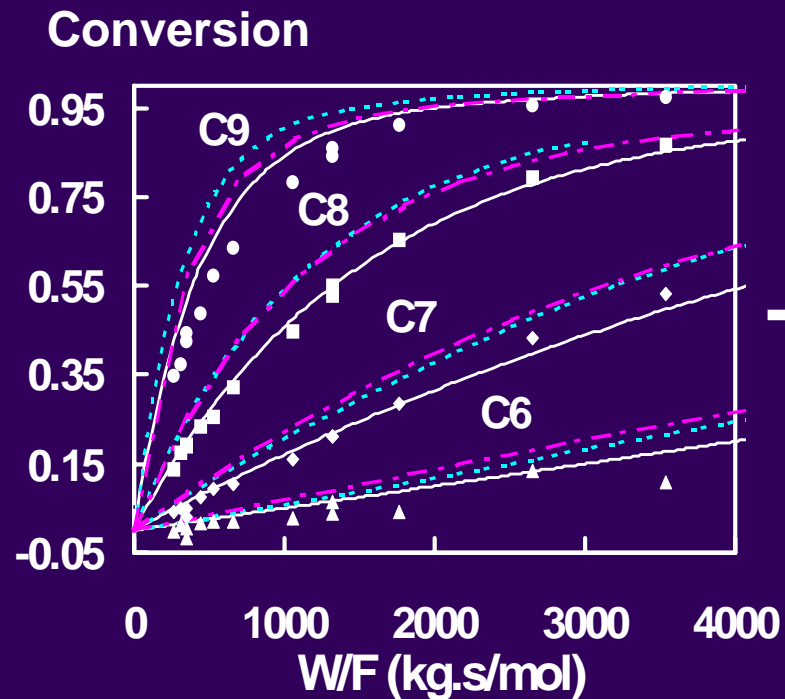
Liquid, binary

$$\zeta = 2.7$$



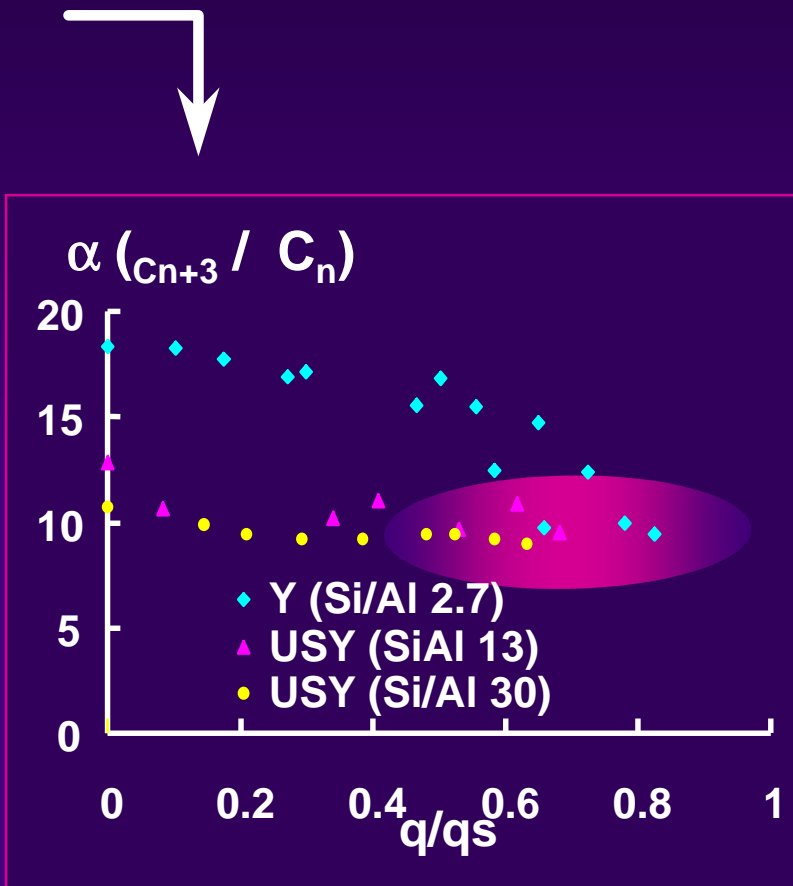
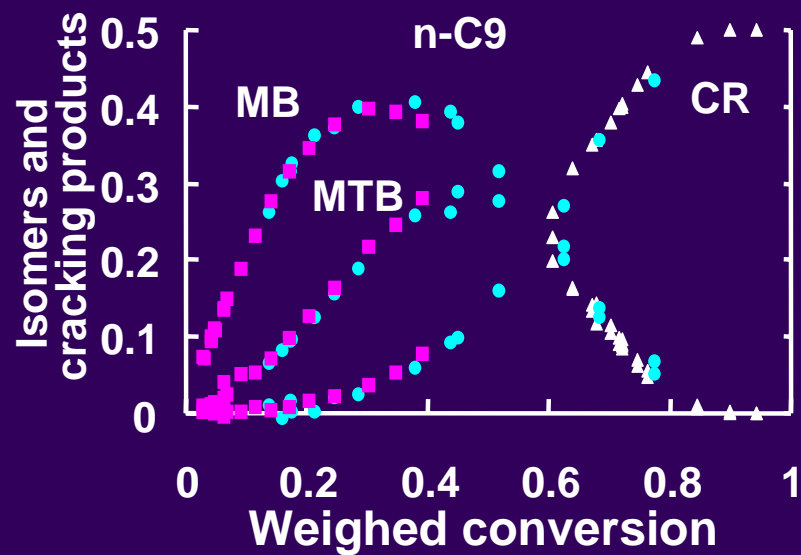
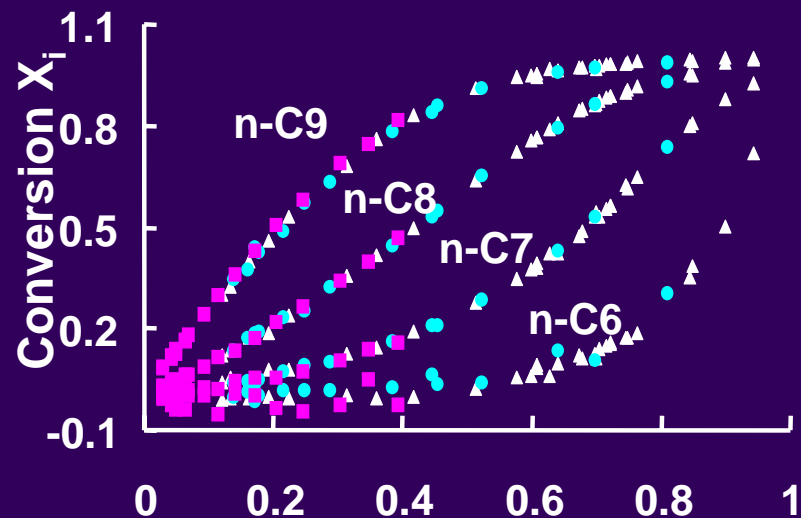
= Ratio of
kinetic constants

Conversion of mixtures

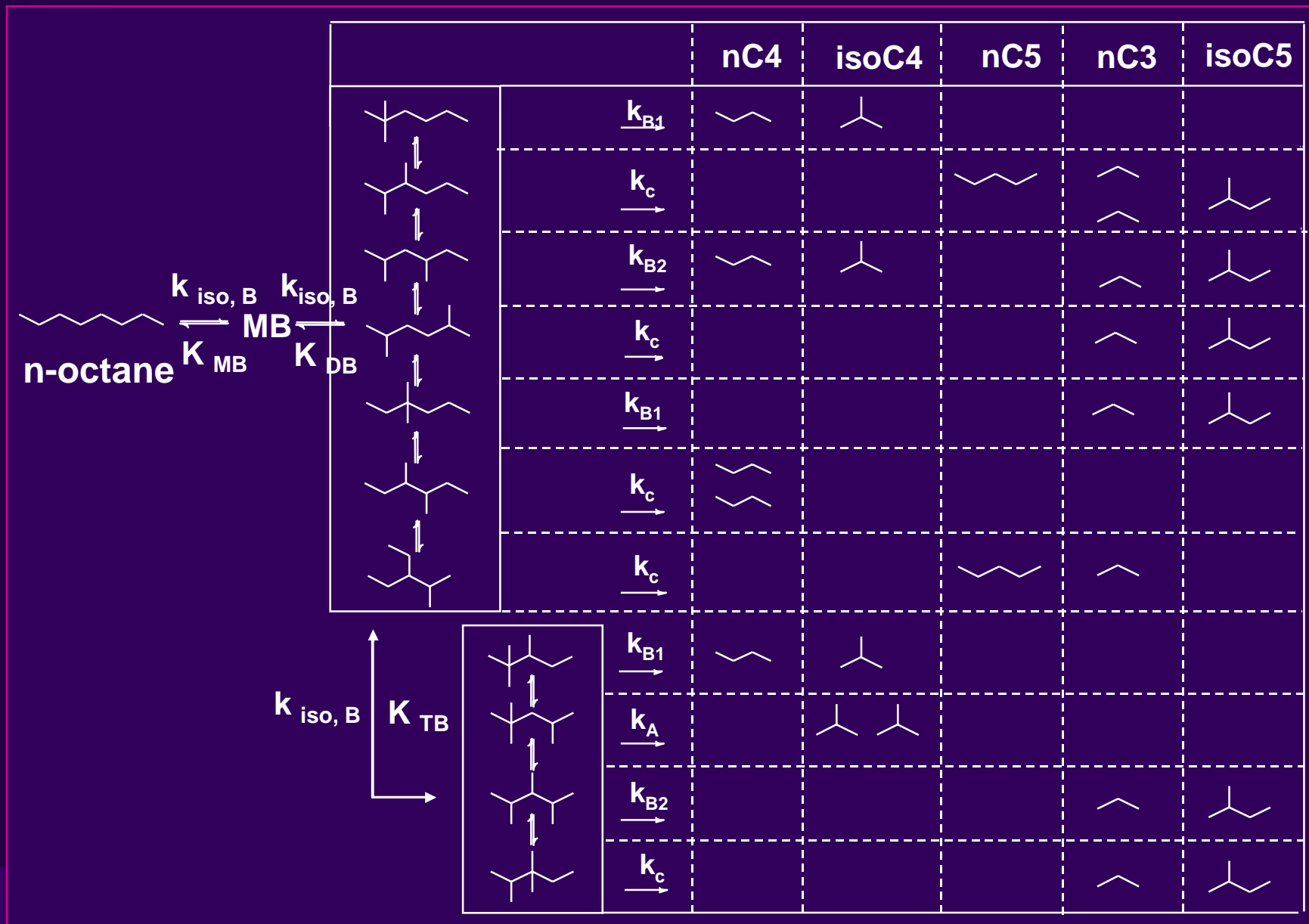


Conversion of mixture very well predicted using single component kinetic parameters and multicomponent adsorption equilibria

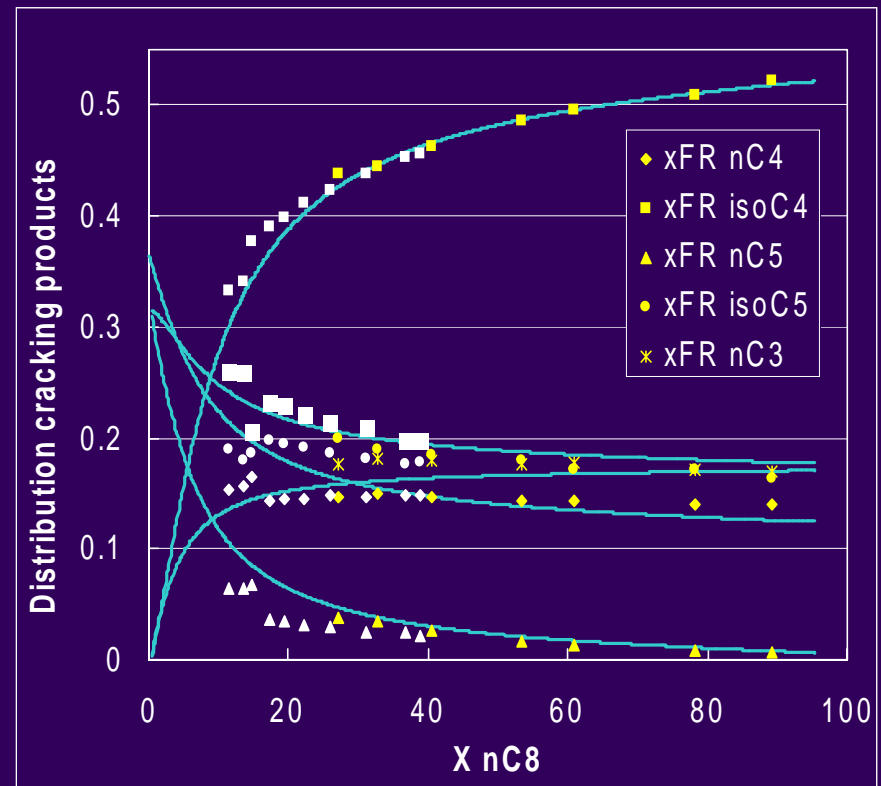
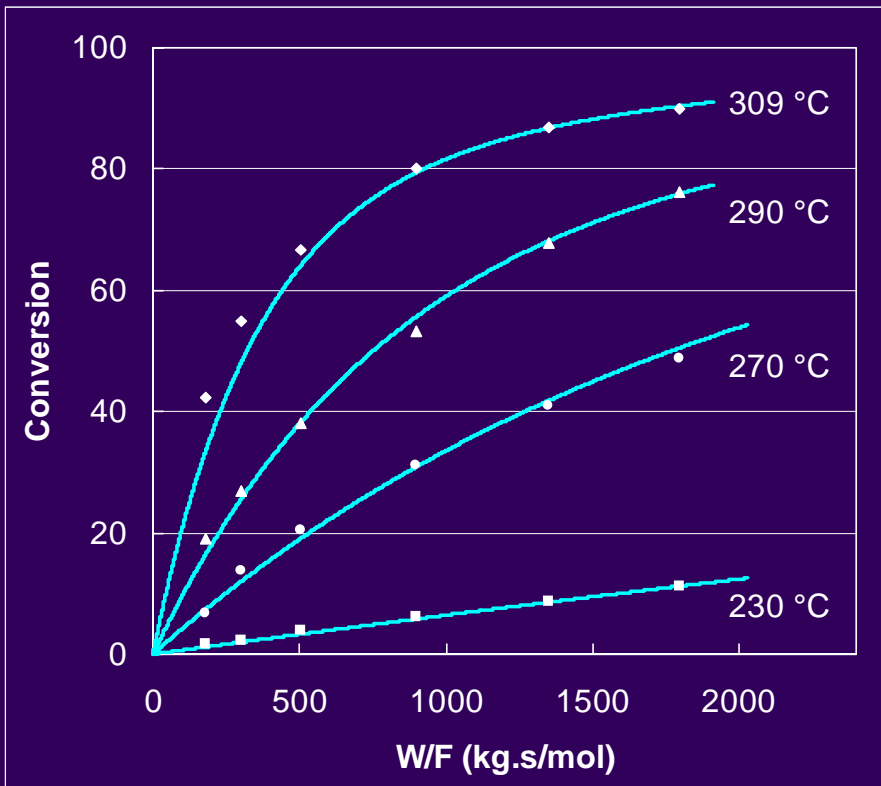
Conversion of mixtures

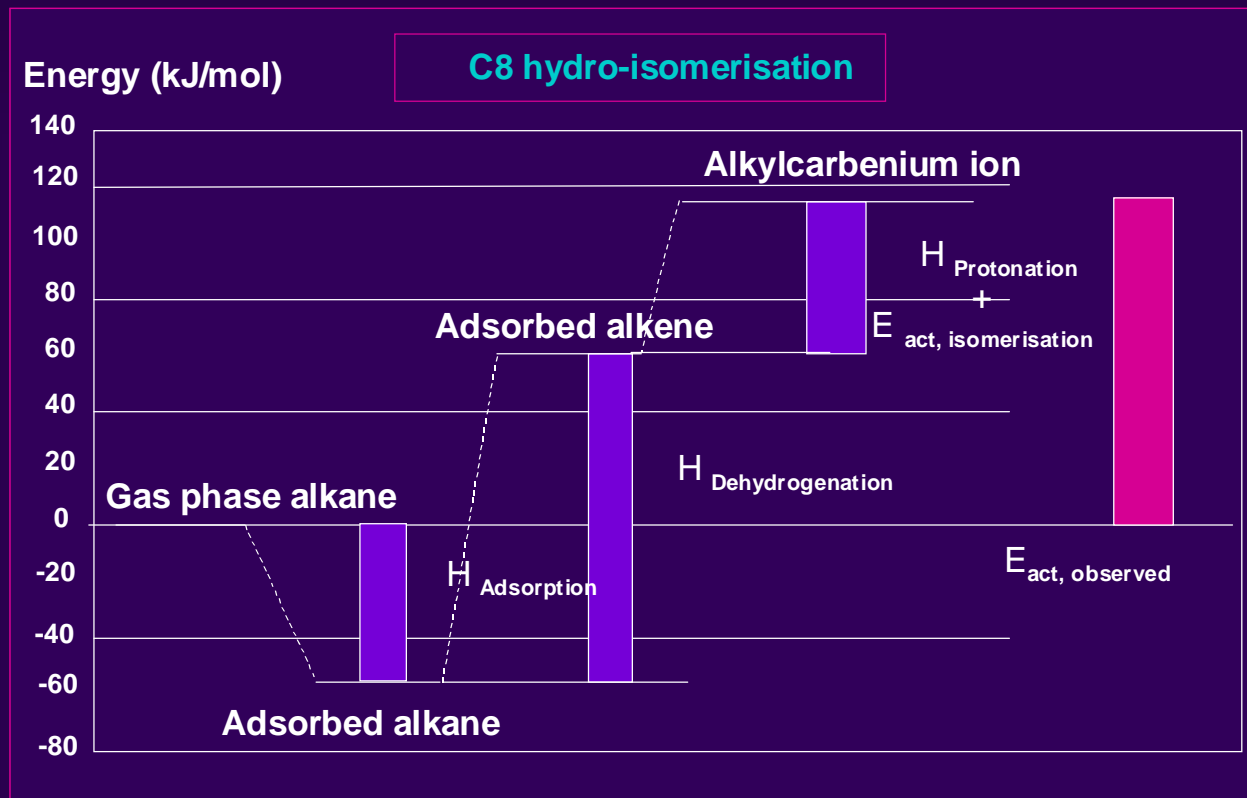


Reaction scheme



n-octane conversion

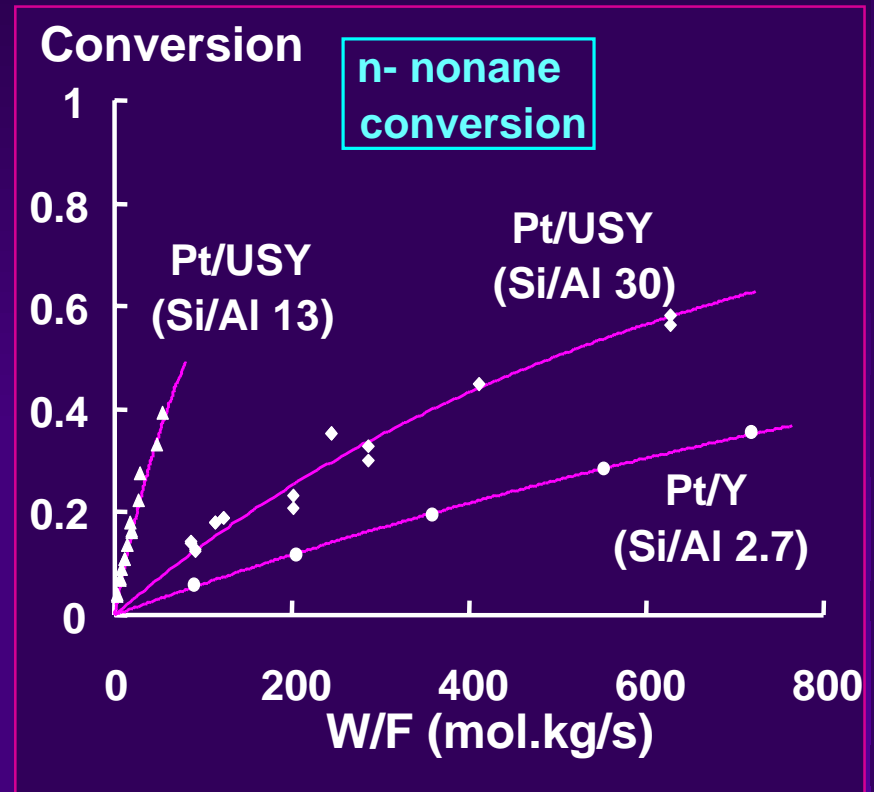
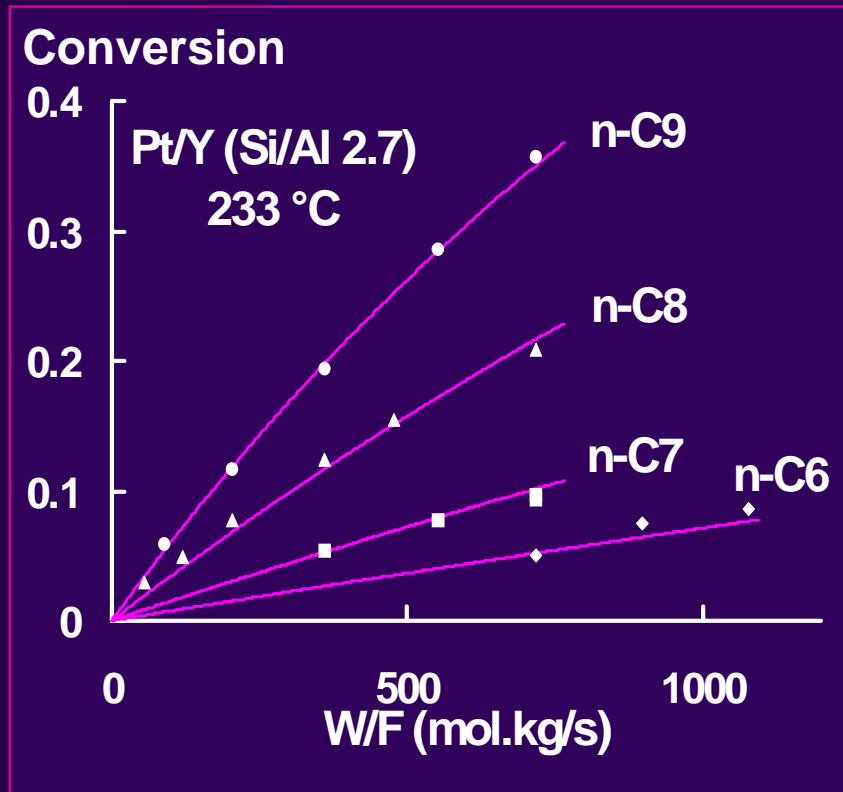




	$k_{270\text{ }^\circ\text{C}}$ (1/s)		$E_{\text{act, global}}$ (kJ/mol)		$\Delta \Delta H_{\text{Prot}}$ (kJ/mol)
	Pt/CBV720	Pt/CBV760	Pt/CBV720	Pt/CBV760	
MB	$3.89 \cdot 10^{-1}$	$5.50 \cdot 10^{-2}$	33.9	38.3	4.4
DB	$2.20 \cdot 10^{-1}$	$3.24 \cdot 10^{-2}$	32.3	38.0	5.7
TB	$5.19 \cdot 10^{-2}$	$7.35 \cdot 10^{-3}$	29.6	35.5	5.8
A	$6.50 \cdot 10^1$	$9.21 \cdot 10^0$	27.5	30.9	3.4
B1	$1.50 \cdot 10^{-1}$	$2.15 \cdot 10^{-2}$	59.2	62.4	3.2
B2	$3.51 \cdot 10^{-1}$	$5.10 \cdot 10^{-2}$	52.2	56.8	4.6
C	$2.10 \cdot 10^{-3}$	$2.83 \cdot 10^{-4}$	71.9	75.7	3.8

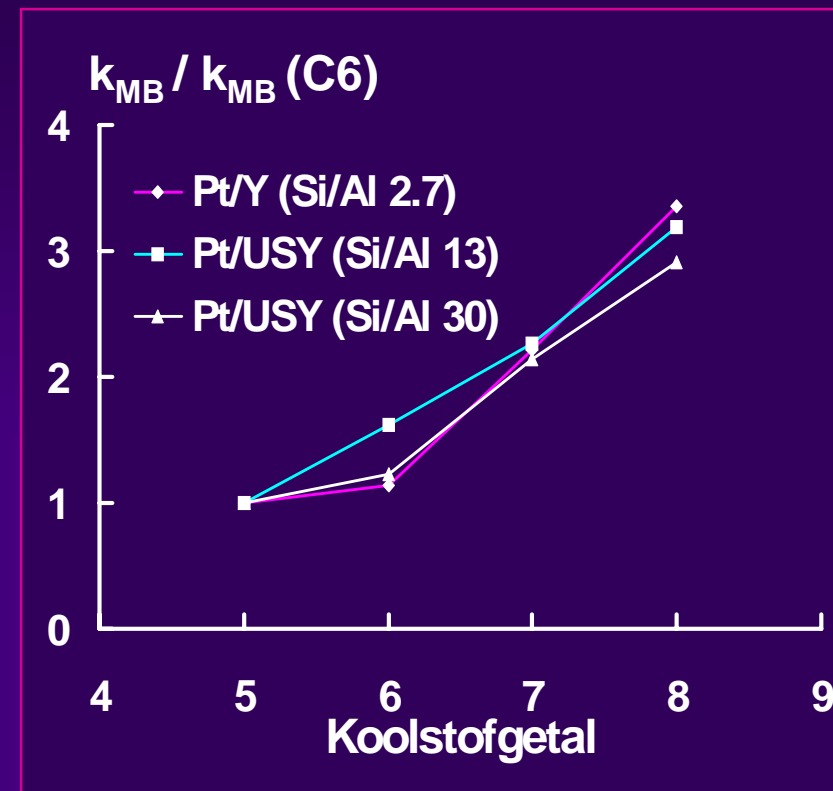
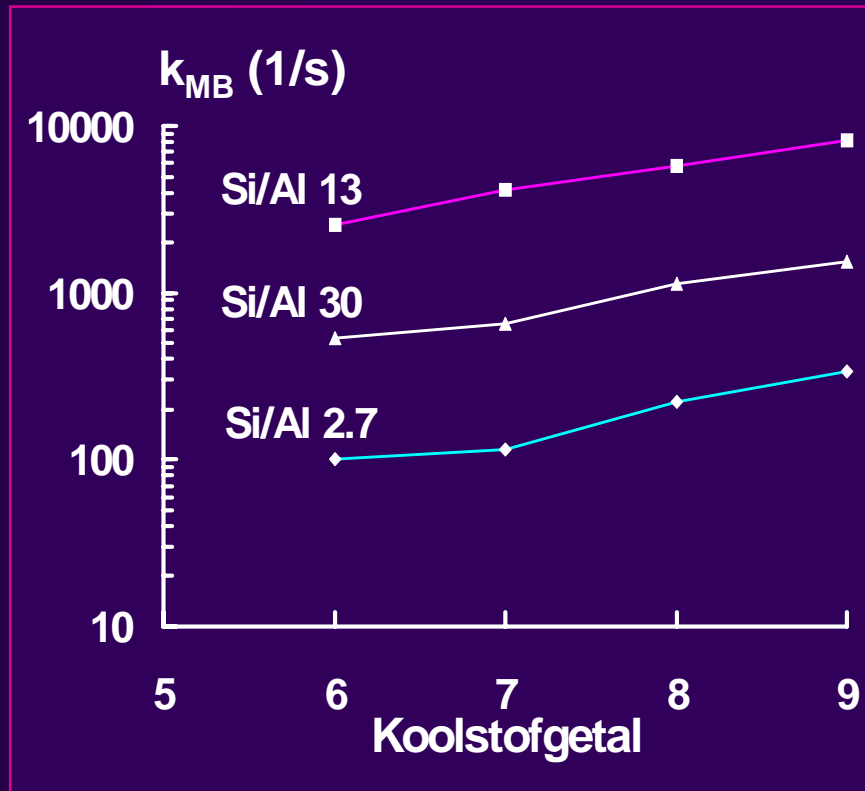
Martens, G.G., Marin, G.B., Martens, J.A., Jacobs, P.A., Baron, G.V. 2000., J. Cat., 195, 253-267.

Influence chain length and Si/Al



- Reactivity ~ Chain length
- Strong influence of Si/Al on observed activity

Kinetic parameters



⇒ Relative reaction rates independent of Si/Al and acidity

Conclusions

- ✓ Several experimental and theoretical techniques to determine adsorption parameters in catalytic conditions
- ✓ Integrated adsorption - reaction study:
 - Deeper insight in relation :
zeolite - reactivity - selectivity - adsorption -
shape selective properties
- ✓ Development and screening new materials, better process control, straightforward modeling

Acknowledgements

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